

Real-Parameter Black-Box Optimization Benchmarking 2009: Experimental Setup

Nikolaus Hansen*, Anne Auger†, Steffen Finck‡ and Raymond Ros§

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Abstract

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<http://coco.gforge.inria.fr/doku.php?id=bbob-2009>.

*NH is with the Microsoft Research–INRIA Joint Centre, 28 rue Jean Rostand, 91893 Orsay Cedex, France

†AA is with the TAO Team, INRIA Saclay, Université Paris Sud, LRI, 91405 Orsay cedex, France

‡SF is with the Research Center PPE, University of Applied Science Vorarlberg, Hochschulstrasse 1, 6850 Dornbirn, Austria

§RR is with the Univ. Paris-Sud, LRI, UMR 8623 / INRIA Saclay, projet TAO, F-91405 Orsay, France.

Contents

1	Introduction	2
1.1	Symbols, Constants, and Parameters	2
2	Benchmarking Experiment	3
2.1	Input to the Algorithm and Initialization	3
2.2	Termination Criteria and Restarts	3
3	Time Complexity Experiment	5
4	Parameter setting and tuning of algorithms	5
5	Data to Provide	7
6	Post-Processing and Data Presentation	7
A	Example Optimizer with Multistarts	9
B	How to Resume an Experiment	9
C	Rationales Behind the Parameter Settings	11
D	Rationale Behind the Data Presentation	11
D.1	Performance Measures	11
D.2	Expected Running Time	11
D.3	Bootstrapping	12
D.4	Fixed-Cost versus Fixed-Target Scenario	12
D.5	Empirical Cumulative Distribution Functions	13
E	Data and File Formats	14
E.1	Introduction	14
E.2	General Settings	15
E.3	Output Files	15
E.3.1	Index File	15
E.3.2	Data Files	16

1 Introduction

This document presents the experimental setup and the data presentation for BBOB. The definition of the benchmark functions [5, 6] and the technical documentation for the provided software is given elsewhere.

1.1 Symbols, Constants, and Parameters

Δf precision to reach, that is, a difference to the optimal function value f_{opt} .

f_{opt} optimal function value is defined for each benchmark function individually

f_{target} target function value to reach. The final, smallest considered target function value is $f_{\text{target}} = f_{\text{opt}} + 10^{-8}$, but also larger values for f_{target} are evaluated.

`Ntrials` = 15 is the number of trials for each single setup, i.e. each function and dimensionality. In each setup three trials are conducted on the same function instance, respectively, using the first five function instances. Performance is evaluated over all `Ntrials` trials.

`D` = 2; 3; 5; 10; 20; 40 search space dimensionalities used for all functions. Dimensionality 40 is optional and can be omitted.

2 Benchmarking Experiment

The real-parameter search algorithm under consideration is run on a testbed of benchmark functions to be minimized. On each function and for each dimensionality `Ntrials` trials are carried out. Different function *instances* are used, each of them three times (the five instantiation numbers 1, 2, ..., 5 are used).¹ A MATLAB example script for this procedure is given in Figure 1. The algorithm is run on *all* functions of the testbed under consideration.

2.1 Input to the Algorithm and Initialization

An algorithm can use the following input.

1. the search space dimensionality D
2. the search domain; all functions are defined everywhere in \mathcal{R}^D and have their global optimum in $[-5, 5]^D$. Most functions have their global optimum in $[-4, 4]^D$ which can also be a reasonable setting for initial solutions.
3. indication of the testbed under consideration, i.e. different algorithms and/or parameter settings might well be used for the noise-free and the noisy testbed
4. the target function value f_{target} is provided for conclusive termination of trials, in order to reduce the overall CPU requirements. The target function value is not intended to be utilized as algorithm input otherwise.

Based on these input parameters, the parameter setting and initialization of the algorithm is entirely left to the participants. As a consequence, the setting shall be identical for all benchmark functions of one testbed (the function identifier or any known characteristics of the function are not meant to be input to the algorithm, see also Section 4).

2.2 Termination Criteria and Restarts

Each trial can be conclusively terminated if f_{target} is reached. Otherwise, the choice of termination is considered as part of the algorithm. Algorithms with any budget of function evaluations, small or large, will be considered in the analysis of the results. Reasonable termination criteria are recommended, but exploiting a larger number of function evaluations might increase the chance to

¹If the algorithm does not contain any stochastic elements, such as a random choice of the initial point in the search domain, one trial per instance is sufficient.

Figure 1: `exampleexperiment.m`: example for benchmarking `MY_OPTIMIZER` on the noise-free function testbed in MATLAB/Octave. An example for the function `MY_OPTIMIZER` is given in Appendix A

```

% runs an entire experiment for benchmarking MY_OPTIMIZER
% on the noise-free testbed. fgeneric.m and benchmarks.m
% must be in the path of Matlab/Octave
% CAPITALIZATION indicates code adaptations to be made

addpath('PUT_PATH_TO_BBOB/matlab'); % should point to fgeneric.m etc.
datapath = 'PUT_MY_BBOB_DATA_PATH'; % different folder for each experiment
opt.algName = 'PUT ALGORITHM NAME';
opt.comments = 'PUT MORE DETAILED INFORMATION, PARAMETER SETTINGS ETC';
maxfunevals = '20 * dim'; % SHORT EXPERIMENT, takes overall three minutes

more off; % in octave pagination is on by default

t0 = clock;
rand('state', sum(100 * t0));

for dim = [2,3,5,10,20,40] % small dimensions first, for CPU reasons
    for ifun = benchmarks('FunctionIndices') % or benchmarksnoisy(...)
        for iinstance = [1:5, 1:5, 1:5] % first 5 fct instances, three times
            fgeneric('initialize', ifun, iinstance, datapath, opt);

            MY_OPTIMIZER('fgeneric', dim, fgeneric('ftarget'), eval(maxfunevals));

            disp(sprintf([' f%d in %d-D, instance %d: FEs=%d,' ...
                ' fbest-ftarget=%.4e, elapsed time [h]: %.2f'], ...
                ifun, dim, iinstance, ...
                fgeneric('evaluations'), ...
                fgeneric('fbest') - fgeneric('ftarget'), ...
                etime(clock, t0)/60/60));
            fgeneric('finalize');
        end
        disp(['    date and time: ' num2str(clock, ' %.0f')]);
    end
    disp(sprintf('---- dimension %d-D done ----', dim));
end

```

achieve better function values or solve the function up to the final f_{target} ². We suggest to consider a multistart procedure.

Independent restarts are the most simple meta-heuristic for multistarts. For example, given a fast algorithm with a small success probability, say 5% (or 1%), chances are that not a single trial (out of 15) will be successful. With 10 (or 90) independent restarts, the success probability will increase to 40% and the performance of the algorithm will become visible. At least 4–5 successful trials (out of 15) are desirable to accomplish a stable performance measurement. Generally, independent restarts do not change the main performance measure ERT (see Appendix D.2), they only improve the reliability of the measured value. This reasoning remains valid for any target function value (different values will be considered in the evaluation).

Restarts with different parameter setups, for example with different (increasing) population sizes, might be considered as well, as it has been applied quite successfully [2]. Choosing different setups mimics what will be done in practice. All restart mechanisms are finally considered as part of the algorithm under consideration.

3 Time Complexity Experiment

In order to get a rough measurement of the time complexity of the algorithm, the overall CPU time is measured when running the algorithm on f_8 (Rosenbrock function) for at least a few tens of seconds (and at least a few iterations). The chosen setup should reflect a “realistic average scenario”. If another termination criterion is reached, the algorithm is restarted (like for a new trial). The *CPU-time per function evaluation* is reported for each dimension. The time complexity experiment is conducted in the same dimensions as the benchmarking experiment. The chosen setup, coding language, compiler and computational architecture for conducting these experiments are described. Figure 2 shows a respective MATLAB/Octave code example. For CPU-inexpensive algorithms the timing might mainly reflect the time spent in function `fgeneric`.

4 Parameter setting and tuning of algorithms

The algorithm and the used parameter setting for the algorithm should be described thoroughly. Whether or not all functions were approached with the very same parameter setting (which might well depend on the dimensionality, see Section 2.1) should be stated clearly and the *crafting effort* should be given (see below). The crafting effort is zero, if the setting was identical for all functions. The method of choosing the parameters for the testbed should be described, as well as which parameters were adjusted to the testbed, the number of overall settings evaluated and the number of settings finally used.

In general, we discourage the *a priori* use of function-dependent parameter settings. In other words, we do not consider the function ID or any function characteristics (like separability, multi-modality, ...) as input parameter to the

²We expect that the easiest functions can be solved in less than $10D$ function evaluations, while the most difficult functions might need a budget of more than $1000D^2$ function evaluations to reach the final $f_{\text{target}} = f_{\text{opt}} + 10^{-8}$.

Figure 2: `exampletiming.m`: example for measuring the time complexity of `MY_OPTIMIZER` given in MATLAB/Octave. An example for `MY_OPTIMIZER` is given in Appendix A

```

% runs the timing experiment for MY_OPTIMIZER. fgeneric.m
% and benchmarks.m must be in the path of MATLAB/Octave

addpath('PUT_PATH_TO_BBOB/matlab'); % should point to fgeneric.m etc.

more off; % in octave pagination is on by default

timings = [];
runs = [];
dims = [];
for dim = [2,3,5,10,20,40]
    nbrun = 0;
    ftarget = fgeneric('initialize', 8, 1, 'tmp');
    tic;
    while toc < 30 % at least 30 seconds
        MY_OPTIMIZER(@fgeneric, dim, ftarget, 1e5); % adjust maxfunevals
        nbrun = nbrun + 1;
    end % while
    timings(end+1) = toc / fgeneric('evaluations');
    dims(end+1) = dim; % not really needed
    runs(end+1) = nbrun; % not really needed
    fgeneric('finalize');
    disp([[ 'Dimensions:' sprintf(' %11d ', dims)]; ...
         [ '      runs:' sprintf(' %11d ', runs)]; ...
         [ ' times [s]:' sprintf(' %11.1e ', timings)]]);
end

```

algorithm (see also Section 2.1). Instead, we encourage either using multiple runs with different parameters (for example restarts, see also Section 2.2), or using (other) probing techniques for identifying function-wise appropriate parameters online. The underlying assumption in this experimental setup is that also in practice we do not know in advance whether the algorithm will face f_1 or f_2 , a unimodal or a multimodal function, or... and we cannot adjust algorithm parameters *a priori*³.

In case that, nevertheless, in one dimension $K > 1$ *different* parameter settings were finally used, the following entropy measure (*crafting effort*, see also [4, 8]⁴) needs to be provided for each dimensionality D :

$$\text{CrE} = - \sum_{k=1}^K \frac{n_k}{n} \ln \left(\frac{n_k}{n} \right) \quad (1)$$

³In contrast to most other function properties, the property of having noise can usually be verified easily. Therefore, for noisy functions a *second* testbed has been defined. The two testbeds can be approached *a priori* with different parameter settings or different algorithms.

⁴Our definition differs from [4, 8] in that it is independent of the number of adjusted parameters. Only the number of used different settings is relevant.

where $n = \sum_{k=1}^K n_k$ is the number of functions in the testbed and n_k is the number of functions, where the parameter setting with index k was used, for $k = 1, \dots, K$. When a single parameter setting was used for all functions, as recommended, the crafting effort is $\text{CrE} = \sum_{k=1}^1 \frac{n}{n} \ln\left(\frac{n}{n}\right) = 0$.⁵

5 Data to Provide

The provided implementations of the benchmark functions generate data for reporting and analysis. Since one goal is the comparison of different algorithms, the data from the experiments shall be submitted to <http://coco.gforge.inria.fr/doku.php?id=bbob-2009>. All submitted data will become available to the participants.

6 Post-Processing and Data Presentation

Python scripts are provided to produce tables and figures reporting the outcome of the benchmarking experiment.

Given the output data from the experiment are in the folder `my_data` of the current directory,⁶ the following command line needs to be executed⁷.

```
python path_to_postproc_code_folder/bbob_pproc/run.py my_data
```

This will create a folder `ppdata` in the working directory that will contain the output from the post-processing. Finally the command

```
latex templateBBOBarticle
```

executed in the same directory will compile a report template⁸ with tables and figures created from the data in `ppdata`. The folder `ppdata`, the files `templateBBOBarticle.tex` and `acm_proc_article-sp.cls` (ACM SIG proceedings template) have to be in the working directory. For the noisy testbed the template `templateBBOBnoisyarticle.tex` is provided.

⁵We give another example: say, in 5- D all functions were optimized with the same parameter setting. In 10- D the first 14 functions were approached with one parameter setting and the remaining 10 functions with a second one (no matter how many parameters were changed). In 20- D the first 10 functions were optimized with one parameter setting, functions 11–13 and functions 23–24 were optimized with a second setting, and the remaining 9 functions 14–22 were optimized with a third setting. The crafting effort computes independently for each dimension in 5- D to $\text{CrE}_5 = 0$, in 10- D to $\text{CrE}_{10} = -\binom{14}{1}$

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APPENDIX

A Example Optimizer with Dultistarts

The optimizer used in Fig. 1 and 2 is given in Fig. 3.

B How to Resume an Experiment

We give a short description of how to cleanly resume an experiment that was aborted before its completion.

1. Find the last modified `.info` file (see Appendix E). Function number and dimension, where the experiment was aborted, are given in the third to last line of the file. For example:

```
funcId = 13, DIM = 40, Precision = 1.000e-08, algId = 'my optimizer'  
% all default parameters  
data_f13/bbobexp_f13_DIM40.dat, 1:5387|-4.4e-09, 2:5147|-3.9e-09, 3
```

The last line points to the written data file and the last number in the last line contains the function instance number of the unfinished trial (see also Appendix E).

Now, there are two options: either restarting by rerunning all experiments for f_{13} in 40-D, or restarting from the very instance 3, which is more involved.

Option 1 (rerun the complete “line” in info file)

2. (optional) delete the respective two(!) data files, in our example

```
data_f13/bbobexp_f13_DIM40.dat  
data_f13/bbobexp_f13_DIM40.tdat
```

3. delete the last three lines in the info file
4. modify your experiment script (see e.g. Fig. 1) to restart with the respective function and dimension, here f_{13} in 40-D

Option 2 (rerun from the broken trial)

2. remove the last characters, in the above example, “ , 3” from the last line of the info file. If the first entry is already the unfinished one, refer to `.73 -11.933(TJ 0 g 0 G 12.1-)-525(=) 231.4633(TJ 0 Th019(data)-120(th)1(e)]TJ 12.73`

Figure 3: Example optimizer used in Fig. 1 and 2

```
function [x, ilaunch] = MY_OPTIMIZER(FUN, DIM, ftarget, maxfunevals)
% minimizes FUN in DIM dimensions by multistarts of fminsearch.
% ftarget and maxfunevals are additional external termination conditions,
% where at most 2 * maxfunevals function evaluations are conducted.
% fminsearch was modified to take as input variable usual_delta to
% generate the first simplex.

% set options, make sure we always terminate
% with restarts up to 2*maxfunevals are allowed
options = optimset('MaxFunEvals', min(1e8*DIM, maxfunevals), ...
                  'MaxIter', 2e3*DIM, ...
                  'Tolfun', 1e-11, ...
                  'TolX', 1e-11, ...
                  'OutputFcn', @callback, ...
                  'Display', 'off');

% multistart such that ftarget is reached with reasonable prob.
for ilaunch = 1:1e4; % relaunch optimizer up to 1e4 times
    % set initial conditions
    if mod(ilaunch-1, floor(1 + 3 * rand(1,1))) == 0
        xstart = 8 * rand(DIM, 1) - 4; % random start solution
        usual_delta = 2;
    else
        xstart = x; % try to improve found solution
        usual_delta = 0.1 * 0.1^rand(1,1);
    end
    % try fminsearch from Matlab, modified to take usual_delta as arg
    x = fminsearch_mod(FUN, xstart, usual_delta, options);
    if feval(FUN, 'fbest') < ftarget || ...
        feval(FUN, 'evaluations') >= maxfunevals
        break;
    end
    % if useful, modify more options here for next launch
end

function stop = callback(x, optimValues, state)
    stop = false;
    if optimValues.fval < ftarget
        stop = true;
    end
end % function callback

end % function
```

C Rationales Behind the Parameter Settings

Rationale for the choice of N_{trials} Parameter N_{trials} determines the minimal measurable success rate and influences the overall necessary CPU time. Compared to a typical standard setup, we have chosen a comparatively small value for N_{trials} . Consequently, within the same CPU-time budget, single trials can conduct more function evaluations, if needed or desired (only needed as long as f_{target} is not reached). For algorithms with a small success probability, say smaller than 20%, this setup leaves the burden to implement an automated multistart procedure, as it will be necessary in practice (see also Section 2.2).

Rationale for the choice of f_{target} The initial search domain and the target function value are an essential part of the benchmark function definition. Different target function values might lead to a different characteristics of the problem to be solved, besides that larger target values are invariably less difficult to reach. Functions might be easy to solve up to a function value of 1 and become intricate for smaller target values. The actually chosen value for the final f_{target} is somewhat arbitrary and could be changed by simple modifications in the function definition. The performance evaluation will consider a wide range of different target function values to reach, all being larger or equal to the final f_{target} .

D Rationale Behind the Data Presentation

D.1 Performance Measures

We advocate performance measures that are

- quantitative, ideally with a ratio scale (rather than interval or ordinal scale)⁹ and with a wide variation (i.e. for example not with values usually ranging between 0.98 and 1)
- as simple as possible
- well-interpretable, having a meaning and semantics attached to the numbers
- relevant with respect to the “real world”

D.2 Expected Running Time

We use the *expected running time* (ERT) as most prominent performance measure, more precisely, the expected number of function evaluations to reach a target function value for the first time. For $p_s > 0$ the ERT computes to [1]

⁹See <http://web.uccs.edu/lbecker/SPSS/scalemeas.htm> or http://en.wikipedia.org/w/index.php?title=Level_of_measurement&oldid=261754099 for an introduction to scale types.

$$\text{ERT}(f_{\text{target}}) = \text{RT}_{\text{S}} + \frac{1 - p_{\text{s}}}{p_{\text{s}}} \text{RT}_{\text{US}} \quad (2)$$

$$\frac{\text{RT}_{\text{S}} + (1 - p_{\text{s}}) \text{RT}_{\text{US}}}{p_{\text{s}}} \quad (3)$$

$$= \frac{f_{\text{best}} \geq f_{\text{target}}}{\#\text{succ}} \quad (4)$$

where the *running times* RT_{S} and RT_{US} denote the average number of function evaluations for successful and unsuccessful trials, respectively (zero for none), and p_{s} denotes the fraction of successful trials, where successful trials are those that reached f_{target} . The $\#\text{FEs}(f_{\text{best}} \geq f_{\text{target}})$ is the number of function evaluations conducted in all trials, while the best function value was not smaller than f_{target} during the trial, i.e. the sum over all trials of

$$\max\{\text{FE s.t. } f_{\text{best}}(\text{FE}) \geq f_{\text{target}}\} .$$

The $\#\text{succ}$ denotes the number of successful trials. ERT estimates the expected running time to reach f_{target} [1]. ERT is a function of f_{target} , as in particular RT_{S} and p_{s} depend on the chosen value for f_{target} .

D.3 Bootstrapping

The ERT computes a single measurement from a data sample set (in our case from `Ntrials` optimization runs). Bootstrapping [3] can provide a dispersion measure for such a measurement: a “new” data sample is derived from the original data sample, in that s values are drawn with replacement, where s is the size of the original set. For each new data set ERT can be computed. The distribution of the bootstrapped ERT is, besides its displacement, a good approximation of the true distribution of ERT (because our sample size is finite, ERT is liable to stochastic aberrations). We provide some percentiles of the bootstrapped distribution.

D.4 Fixed-Cost versus Fixed-Target Scenario

There exist two different approaches for collecting data and making measurements from experiments, as schematically depicted in Figure 4.

Fixed-cost scenario (vertical cuts). Fixing a number of function evaluations (this corresponds to fixing a cost) and measuring the function values reached for this given number of function evaluations. Fixing search costs can be pictured as drawing a vertical line on the convergence graphs (see Figure 4 where the line is depicted in red).

Fixed-target scenario (horizontal cuts). Fixing a target function value (i.e. drawing an horizontal line in the convergence graphs, see Figure 4 where the line is depicted in blue) and measuring the number of function evaluations needed to reach this target function value.

It is often argued that the fixed-cost approach is close to what is needed for real word applications where the total number of function evaluations is limited. On

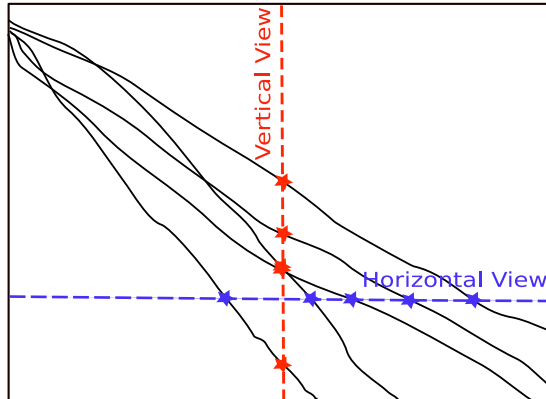


Figure 4: Illustration of fixed-cost (vertical cuts) and fixed-target (horizontal cuts) view. Black lines depict the best function value plotted versus number of function evaluations.

the other hand, also a minimum target requirement needs to be achieved in real world applications, for example, getting (noticeably) better than the currently available best solution or than a competitor.

For benchmarking algorithms we prefer the fixed-target scenario over the fixed-cost scenario since it gives *quantitative and interpretable* data: the fixed-target scenario (horizontal cut) *measures a time* needed to reach a target function value and allows therefore conclusions of the type: Algorithm A is two/ten/hundred times faster than Algorithm B in solving this problem (i.e. reaching the given target function value). The fixed-cost scenario (vertical cut) does not give *quantitatively interpretable* data: there is no interpretable meaning to the fact that Algorithm A reaches a fitness value that is two/ten/hundred times smaller than the one reached by Algorithm B, mainly because there is no *a priori* evidence *how much* more difficult it is to reach a fitness value that is two/ten/hundred times smaller. Furthermore, for algorithms invariant under transformations of the function value (for example order-preserving transformations for algorithms based on comparisons like DE, ES, PSO), fixed-target measures can be made invariant to these transformations by simply transforming the target function value while for fixed-cost measures all results need to be transformed.

D.5 Empirical Cumulative Distribution Functions

We exploit the “horizontal and vertical” viewpoints introduced in the last Section D.4. In Figure 5 we plot the empirical cumulative distribution function¹⁰ (ECDF) of the intersection point values (stars in Figure 4). A cutting line in Figure 4 corresponds to a “data” line in Figure 5, where 450 (30×15) convergence graphs are evaluated. For example, the thick red graph in Figure 5 shows on the left the distribution of the running length (number of function evaluations) [7] for reaching precision $\Delta f = 10^{-8}$ (horizontal cut). The graph

¹⁰ The empirical (cumulative) distribution function $F : \mathcal{R} \rightarrow [0, 1]$ is defined for a given set of real-valued data S , such that $F(x)$ equals the fraction of elements in S which are smaller than x . The function F is monotonous and a lossless representation of the (unordered) set S .

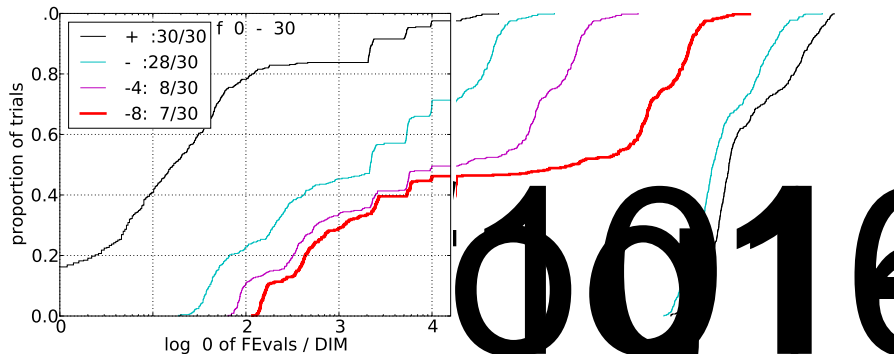


Figure 5: Illustration of empirical (cumulative) distribution functions (ECDF) of running length (left) and precision (right) arising respectively from the fixed-target and the fixed-cost scenarios in Fig. 4. In each graph the data of 450 trials are shown. Left subplot: ECDF of the running time (number of function evaluations), divided by search space dimension D , to fall below $f_{\text{opt}} + \Delta f$ with $\Delta f = 10^k$, where $k = 1, -1, -4, -8$ is the first value in the legend. Right subplot: ECDF of the best achieved precision Δf divided by 10^k (thick red and upper left lines in continuation of the left subplot), and best achieved precision divided by 10^{-8} for running times of $D, 10D, 100D$ and $1000D$ function evaluations (from the rightmost line to the left cycling through black-cyan-magenta-black).

continues on the right as a vertical cut for the maximum number of function evaluations, showing the distribution of the best achieved Δf values, divided by 10^{-8} . Run length distributions are shown for different target precisions Δf on the left (by moving the horizontal cutting line up- or downwards). Precision distributions are shown for different fixed number of function evaluations on the right. Graphs never cross each other. The y -value at the transition between left and right subplot corresponds to the success probability. In the example, just under 50% for precision 10^{-8} (thick red) and just above 70% for precision 10^{-1} (cyan).

E Data and File Formats

E.1 Introduction

This section specifies the format for the output data files and the content of the files, as they are written by the provided benchmark functions implementations. The goal is to obtain format-identical files which can be analyzed with the provided post-processing tools. The first section explains the general settings. Afterwards the format for the different output files will be given in detail and with examples.

```

↳ container_folder
    ↳ fileprefix_f1.info
    ↳ data_f1
        ↳ fileprefix_f1_DIM5.dat
        ↳ fileprefix_f1_DIM5.tdat
        ↳ fileprefix_f1_DIM10.dat
        ↳ fileprefix_f1_DIM10.tdat
    ↳ fileprefix_f2.info
    ↳ data_f2
        ↳ fileprefix_f2_DIM5.dat
        ↳ fileprefix_f2_DIM5.tdat

↳ container_folder2

↳ ...

```

Figure 6: Example data file structures obtained with the BBOB experiment software.

E.2 General Settings

The output from one *experiment*, consisting of `Ntrials` optimization runs on a given objective function, will be contained in a folder which path will be decided by the user and will consist of one index file (or more) and two data files (or more). The output files contain all necessary data for post-processing. The extensions are `*.info` for the index file and `*.dat`, `*.tdat` for the data files. An example of the folder/file structure can be found in Fig 6. After performing all simulations, the user can use the data files with the provided post-processing tool to obtain \LaTeX files, including tables and figures of the results.

E.3 Output Files

E.3.1 Index File

The index file contains meta information on the optimization runs and the location of the corresponding data files. The user is free to choose any prefix for the index file name. The function identifier will be appended to it and the extension will be `.info`. The contents of the index file are the concatenation of 3-line index entries (output format is specified in brackets):

- *1st* line - function identifier (`%d`), search space dimension (`%d`), precision to reach (`%4.3e`) and the identifier of the used algorithm (`%s`)
- *2nd* line - comments of the user (e.g. important parameter or used internal methods)
- *3rd* line - relative location and name of data file(s) followed by a colon and information on a single run: the instance of the test function, final

number of function evaluations, a vertical bar and the final best function value minus target function value.

All entries in the *1st* line and the *3rd* line are separated by commas.

For each experiment the provided data-writing tools generate one index file with the respective entries. All index files have to be included in the archive for the submission and will contain the *relative* location of the data files *within* the archive. Thus, it is necessary to archive all files in the same folder-subfolder structure as obtained. An example of an index file is given in Fig 7. An entry of

```
funcId = 12, DIM = 5, Precision = 1.000e-08, algId = 'ALG-A'
% parameterA = 2, parameterB = 3.34, ...
data_f12\test_f12.DIM5.dat, 1:387|-2.9e-009, 2:450|-2.8e-009, 3:422|-2.1e-009, data_f12\test-01_f12.DIM5.dat, 1:5000000|1.8e-008,
...
funcId = 12, DIM = 10, Precision = 1.000e-08, algId = 'ALG-A'
% parameterA = 2, parameterB = 3.34, ...
data_f12\test1_f12.DIM10.dat, 1:307|-8.6e-008, 2:321|-3.5e-008, ...
...
```

Figure 7: Example of an index file

the index file is written at the start of the first sample run for a given function and dimension.

E.3.2 Data Files

A data file contains the numerical output of an optimization run on a given objective function. The content of the data file is given in the following. Data files will be placed in subfolders at the location of their corresponding index file. At the start of each sample run the header for the data file is written. The header is one line with the titles for each data column:

- function evaluation
- noise-free fitness - Fopt (and its value)
- best noise-free fitness - Fopt
- measured fitness
- best measured fitness
- x1, x2, ... (one column for each dimension)

Fopt is the optimum of the test function considered. In the header, each of these entries are separated by the |-symbol. Each data line in the data file contains the following information:

- *1st* column - recent number of function evaluation in format %d
- *2nd* column - recent noise-free function value in format %+10.9e
- *3rd* column - best noise-free function value so far in format %+10.9e
- *4th* column - recent measured (noisy) function value in format %+10.9e
- *5th* column - best measured (noisy) function value so far in format %+10.9e
- (*5+d*)*th* column - value of the *d*th ($d = 1, 2, \dots, DIM$) object parameter of the best so far noise-free function value (*3rd* column) in format %+5.4e


```

% function evaluation | noise-free fitness - Fopt (6.671000000000e+01) | best noise-free fitness - Fopt | measured fitness | best
measured fitness | x1 | x2 |...
1 +9.324567891e+05 +9.324567891e+05 +1.867342122e+06 +1.867342122e+06 +4.2345e+01 ...
2 +9.636565611e+05 +9.324567891e+05 +8.987623162e+05 +8.987623162e+05 +3.8745e+01 ...
...
31623 9.232667823e+01 9.576575761e+01 -6.624783627e+01 -1.657621581e+02 +5.1234e-02 ...
32478 1.000043784e+02 9.576575761e+01 -4.432869272e+01 -1.657621581e+02 +3.8932e-02 ...
35481 ...
...

```

Figure 8: Example of a data file

An example is given in Fig 8.

Each entry in the index files is associated to at least two data files: one for the function value-aligned data and another for the number of function evaluations-aligned data. The data file names are identical except for the file extension being '*.dat' and '*.tdata' respectively.

The writing to the function value aligned data file happens only each time the noise-free function value minus the optimum function value is less than $10^{i/5}$, for all integer i , for the first time (note, that the provided software does not return this difference to the algorithm).

The writing to the number of function evaluations aligned data file happens:

- in the first file each time the function evaluation number is equal to $\lceil 10^{i/20} \rceil$ for at least one $i = 1, 2, \dots$. This means, that writing happens after about 12.2% additional function evaluations have been conducted. In particular the first 8 evaluations are written and also evaluations $\dots, 89, 100, 112, 125, 141, \dots, 707, 794, 891, 1000, 1122, \dots$
- when any termination criterion is fulfilled (writing the recent evaluation and the current best so far values)

The prefix for the data file names of one experiment will be the same as the prefix of the corresponding index file. The function identifier and the dimension of the object parameters will be appended to this prefix. All data files will be saved in subfolders `data_fX`, where X is the function identifier, located at the same location as their index file.