

Comparison tables: BBOB 2009 function testbed in 2-D

The BBOBies

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Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2009, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2009>. More than 30 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [14, 9]. The experimental set-up is described in [13].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm. Consequently, the best (smallest) value is 1 and the value 1 appears in each column at least once. See [13] for details on how ERT is obtained. All numbers are computed with no more than two digits of precision.

Table 1: 02-D, running time excess ERT/ERT_{best} on f_1 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1 Sphere										Δf_{target} ERT_{best}/D	Δf_{target} ERT_{best}/D
	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07		
ALPS	1	1	0.9	9.7	56	170	290	440	640	970		ALPS [17]
AMaLGA μ IDEA	1	1.1	2.1	4.4	11	14	23	28	32	46		AMaLGA μ IDEA [4]
avg NEWUOA	1	1	1.9	1.1	1.1	1	1	1	1	1		avg NEWUOA [31]
BayEDA ϵ G	1	1	1.9	4.2	18	79	110	140	160	210		BayEDA ϵ G [10]
BFGS	1	1	3.3	1.2	1.2	1.2	1.2	1.2	1.2	1.2		BFGS [30]
Cauchy EDA	1	1	19	15	27	39	50	63	75	100		Cauchy EDA [24]
BIPOP-CMA-ES	1	1	3.3	3.8	8.5	13	19	24	29	39		BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	3.3	3.6	7.6	11	14	18	22	29		(1+1)-CMA-ES [2]
DASA	1	1	39	23	44	52	62	76	95	120		DASA [19]
DEPSO	1	1	2.1	1.2	27	46	51	96	120	170		DEPSO [12]
DIRECT	1	1	1	1.4	2.5	9.4	15	20	32	56		DIRECT [25]
EDA-PSO	1	1	1.9	5	20	34	53	80	110	210		EDA-PSO [6]
full NEWUOA	1	1	2.7	1.2	1.2	1.2	1.2	1.2	1.2	1.2		full NEWUOA [31]
G3-PCX	1	1	1.9	6	17	19	24	29	34	46		G3-PCX [26]
simple GA	1	1	2.7	7.2	62	310	1100	1800	2600	4500		simple GA [22]
GLOBAL	1	1	1.9	5.7	39	50	54	55	56	58		GLOBAL [23]
iAMaLGA μ IDEA	1	1	2.3	3.8	6.7	12	14	19	22	31		iAMaLGA μ IDEA [4]
LSfmibnd	1	1	7.8	3.2	3.6	4.1	4.1	4.1	4.1	4.1		LSfmibnd [28]
LSstep	1	1	46	34	62	63	68	68	69	69		LSstep [28]
MA-LS-Chain	1	1	2.4	7.4	26	40	67	85	92	100		MA-LS-Chain [21]
MCS (Neum)	1	1	1	1.5	2.2	2.6	2.6	2.6	2.6	2.6		MCS (Neum) [18]
NELDER (Han)	1	1	2.1	1.3	3	3.9	5.1	6.3	7.4	9.8		NELDER (Han) [16]
NELDER (Doe)	1	1	1	1.5	2.9	4.1	5.3	6.5	7.6	10		NELDER (Doe) [5]
NEWUOA	1	1	2.8	1	1	1	1	1	1	1		NEWUOA [31]
(1+1)-ES	1	1	3.5	2.8	6.7	10	14	18	23	30		(1+1)-ES [1]
POEMS	1	1	170	80	110	400	680	1100	1300	2100		POEMS [20]
PSO	1	1	2.1	5.3	20	59	120	200	250	470		PSO [7]
PSO_Bounds	1	1.1	2.4	6	26	89	270	460	770	1200		PSO_Bounds [8]
Monte Carlo	1	1	1.5	9.7	49	540	5900	4.8e4	6.8e5	1.1e-6/1e6		Monte Carlo [3]
Rosenbrock	1	1	5.6	3.1	3.9	4.9	6.2	7.6	8.8	11		Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	3.9	5.9	9.5	14	18	24	28	38		IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.6	8.9	25	33	37	43	48	60		VNS (Garcia) [11]

Table 2: 02-D, running time excess ERT/ERT_{best} on f_2 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

2 Ellipsoid separable											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT_{best}/D	4.93	6.23	8.2	9.47	12.3	12.7	12.9	13.6	14	14.3	ERT_{best}/D
ALPS	11	24	58	120	130	160	200	230	260	330	ALPS [17]
AMaLGA μ IDEA	4.9	4.8	6.2	7.6	7.5	9.1	10	11	13	16	AMaLGA μ IDEA [4]
avg NEWUOA	1.2	1.1	1.9	5.6	8.5	10	14	17	20	27	avg NEWUOA [31]
BayEDA μ C	37	62	80	78	82	87	110	110	140	140	BayEDA μ C [10]
BFGS	1.7	1.6	2.5	4	3.7	3.9	4.1	4.1	4.1	4.4	BFGS [30]
Cauchy EDA	13	17	18	18	18	20	23	24	25	29	Cauchy EDA [24]
BIPOP-CMA-ES	4	5.4	13	19	18	18	20	20	20	22	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.1	5.1	10	13	13	13	14	14	15	16	(1+1)-CMA-ES [2]
DASA	21	19	19	22	21	21	23	25	26	31	DASA [19]
DEPSO	10	16	18	26	27	31	35	40	45	53	DEPSO [12]
DIRECT	5.9	5.1	7.5	8	7.1	8.5	9.4	12	13	46	DIRECT [25]
EDA-PSO	8.8	11	13	19	20	26	39	49	65	88	EDA-PSO [6]
full NEWUOA	1.2	1.2	2.4	5.8	8.3	10	13	15	18	23	full NEWUOA [31]
G3-PCX	8.6	8.4	14	64	69	76	83	82	82	82	G3-PCX [26]
simple GA	11	44	130	320	420	540	780	990	1300	1900	simple GA [22]
GLOBAL	11	19	19	17	13	13	13	13	13	13	GLOBAL [23]
iAMaLGA μ IDEA	2.6	3.8	5.1	9.2	9.1	10	11	12	12	14	iAMaLGA μ IDEA [4]
LSfminbnd	1.4	1.2	1	1	1	1	1	1	1	1	LSfminbnd [28]
LSstep	14	12	9.5	9.9	7.9	7.9	7.8	7.5	7.3	7.3	LSstep [28]
MA-LS-Chain	12	14	17	22	20	24	28	28	29	34	MA-LS-Chain [21]
MCS (Neum)	1.5	1.6	1.4	1.8	1.7	2.6	3.2	3.3	3.7	23	MCS (Neum) [18]
NELDER (Han)	1.9	1.8	1.7	1.8	1.8	2	2.2	2.4	2.6	3	NELDER (Han) [16]
NELDER (Doe)	1.6	1.7	1.6	1.9	1.7	1.9	2.2	2.3	2.5	3	NELDER (Doe) [5]
NEWUOA	1	1	2.2	8.8	12	15	19	23	26	35	NEWUOA [31]
(1+1)-ES	3.2	2400	8700	4.7e4	1.2e5	3.8e5	<i>74e-3/1e6</i>	.	.	.	(1+1)-ES [1]
POEMS	140	250	380	420	400	460	510	570	630	780	POEMS [20]
PSO	7.5	14	56	83	83	98	120	130	160	200	PSO [7]
PSO_Bounds	6.9	24	54	170	310	360	400	440	530	780	PSO_Bounds [8]
Monte Carlo	21	50	240	1200	5600	1e5	<i>94e-4/1e6</i>	.	.	.	Monte Carlo [3]
Rosenbrock	2.6	3.1	2.5	3.7	4.4	5.4	6.3	6.5	6.9	7.9	Rosenbrock [27]
IPOP-SEP-CMA-ES	4.5	5.4	14	19	16	17	18	18	18	20	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	8.4	15	22	27	24	25	26	26	26	29	VNS (Garcia) [11]

Table 3: 02-D, running time excess ERT/ERT_{best} on f_3 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

3 Rastrigin separable												
Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D	
ALPS	1.1	1.6	9.2	6.7	6.4	11	12	15	19	23	ALPS [17]	
AMaLgAM IDEA	1.1	1.1	3.7	4.6	12	12	12	12	13	13	AMaLgAM IDEA [4]	
avg NEWUOA	1	2.7	5.1	1.6	3.2	3.2	3.2	3.2	3.2	3.1	avg NEWUOA [31]	
BayEDAeG	1.1	1.2	4.4	4	9.7	18	41	65	65	64	BayEDAeG [10]	
BFGS	1.2	18	14	3.1	10	10	10	10	10	10	BFGS [30]	
Cauchy EDA	1.1	9.6	9.6	3.3	8.4	33	43	43	43	43	Cauchy EDA [24]	
BIPOP-CMA-ES	1	2.2	3.5	3.5	5.2	6.2	6.4	6.5	6.5	6.7	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1.9	6.9	3.8	7.9	7.9	7.9	7.9	7.9	7.8	(1+1)-CMA-ES [2]	
DASA	6.3	22	18	1.8	6.9	7	7.1	7.2	7.4	7.6	DASA [19]	
DEPSO	1.8	2	5.7	2.3	2.7	4	4.5	5	5.4	6.4	DEPSO [12]	
DIRECT	1	1.1	2.7	1	2.4	2.4	2.5	2.6	2.7	3	DIRECT [25]	
EDA-PSO	1.2	1.4	4.8	6.4	14	19	20	20	21	22	EDA-PSO [6]	
full NEWUOA	1	4	2.3	1.8	2.2	2.2	2.2	2.1	2.1	2.1	full NEWUOA [31]	
G3-PCX	1.1	2	4.1	7.8	40	40	39	39	39	39	G3-PCX [26]	
simple GA	1	2	8.3	13	19	27	40	55	70	110	simple GA [22]	
GLOBAL	1.1	1.6	7	1.8	3.1	3.1	3.1	3.1	3.1	3.1	GLOBAL [23]	
iAMaLgAM IDEA	1.1	1.4	1.8	6.3	17	17	17	17	17	17	iAMaLgAM IDEA [4]	
LSfminbnd	2.1	4.7	17	32	43	64	63	63	63	61	LSfminbnd [28]	
LSstep	28	120	24	1.5	1	1	1	1	1	1	LSstep [28]	
MA-LS-Chain	1	1.5	5.7	1.7	2.5	2.6	2.7	2.7	2.8	2.9	MA-LS-Chain [21]	
MCS (Neum)	1	1.1	1.5	1.1	1.5	1.6	1.6	2.6	2.6	2.6	MCS (Neum) [18]	
NELDER (Han)	1.2	1.8	1.4	4	13	13	13	13	12	12	NELDER (Han) [16]	
NELDER (Doe)	1	1	1	1	1.7	1.8	1.8	1.8	1.8	1.8	NELDER (Doe) [5]	
NEWUOA	1.5	2.4	4.8	1.5	4.2	4.2	4.2	4.1	4.1	4.1	NEWUOA [31]	
(1+1)-ES	1.1	2.4	12	5	15	15	15	15	15	14	(1+1)-ES [1]	
POEMS	31	200	42	11	14	20	24	29	32	41	POEMS [20]	
PSO	1.1	1.6	5.1	3.3	3.4	4.7	6	7.2	8.8	11	PSO [7]	
PSO_Bounds	1.1	1.8	4.8	5.3	8.3	14	18	22	26	34	PSO_Bounds [8]	
Monte Carlo	1.1	1.5	14	67	460	3100	<i>2.1e4</i>	<i>39e-4/1e6</i>	.	.	Monte Carlo [3]	
Rosenbrock	1	16	45	15	26	26	26	26	26	25	Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1.5	2.3	3.4	7.6	8.4	9.2	9.4	9.6	9.8	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1.9	8.8	2.9	4.1	4.2	4.2	4.5	4.7	7.7	VNS (Garcia) [11]	

Table 4: 02-D, running time excess ERT/ERT_{best} on f_4 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

4 Skew Rastrigin-Bueche separable

Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS	1	0.5	9	7.1	8.3	9.7	12	15	17	20	ALPS [17]
AMaLGaM IDEA	1	2.5	2.6	5.6	51	48	48	46	47	45	AMaLGaM IDEA [4]
avg NEWUOA	1	4.5	6.2	4	14	13	12	12	12	11	avg NEWUOA [31]
BayEDA _c G	1	2.3	4.5	13	62	120	110	<i>10e-1/2e3</i>	.	.	BayEDA _c G [10]
BFGS	1	13	11	5.7	12	11	11	10	10	9.8	BFGS [30]
Cauchy EDA	1	19	6.8	13	75	410	470	450	450	430	Cauchy EDA [24]
BIPOP-CMA-ES	1	3.8	2.6	6.9	55	97	99	98	99	110	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	2.4	5.2	5.5	27	25	24	23	23	22	(1+1)-CMA-ES [2]
DASA	1	82	15	2	3.6	3.4	3.3	3.3	3.4	3.4	DASA [19]
DEPSO	1	2.4	7.2	4.2	6.5	11	17	17	17	35	DEPSO [12]
DIRECT	1	1	1.8	1.8	6.6	6.1	14	14	16	16	DIRECT [25]
EDA-PSO	1	2.6	4.2	9.9	18	19	19	19	19	20	EDA-PSO [6]
full NEWUOA	1	3.8	5.4	3.9	15	14	13	13	13	12	full NEWUOA [31]
G3-PCX	1	2.1	20	17	76	70	67	65	64	62	G3-PCX [26]
simple GA	1	2.6	10	16	22	28	37	49	60	100	simple GA [22]
GLOBAL	1	2.4	8.5	1.2	5.2	4.8	4.6	4.5	4.5	4.3	GLOBAL [23]
iAMaLGaM IDEA	1	3.8	2.5	9.5	61	57	56	55	55	54	iAMaLGaM IDEA [4]
LSfminbd	1	4.6	1	45	120	230	<i>10e-1/4e3</i>	.	.	.	LSfminbd [28]
LSstep	1	220	19	1.3	1	1	1	1	1	1	LSstep [28]
MA-LS-Chain	1	2.3	5.6	1.8	4.4	4.2	4.1	4	4.1	4.1	MA-LS-Chain [21]
MCS (Neum)	1	1	2	1	2.9	2.7	2.7	2.7	2.7	2.6	MCS (Neum) [18]
NELDER (Han)	1	3.1	5	5.3	27	25	24	23	23	22	NELDER (Han) [16]
NELDER (Doe)	1	2.1	1.9	1.4	3.5	3.2	3.1	3	3	3	NELDER (Doe) [5]
NEWUOA	1	3	5	4.5	18	16	16	15	15	14	NEWUOA [31]
(1+1)-ES	1	3.1	4.5	5.5	23	21	20	20	20	19	(1+1)-ES [1]
POEMS	1	240	36	9.8	22	23	29	32	35	41	POEMS [20]
PSO	1.1	3.2	4	3.3	4.6	5.6	6.4	7.4	8.7	11	PSO [7]
PSO_Bounds	1	3.3	4.4	6.3	9.6	17	21	24	27	33	PSO_Bounds [8]
Monte Carlo	1	3.3	8.6	67	620	8200	2.8e4	5.5e4	<i>11e-3/1e6</i>	.	Monte Carlo [3]
Rosenbrock	1	71	27	15	52	48	46	44	44	42	Rosenbrock [27]
IPOP-SEF-CMA-ES	1	3.5	3	8.7	75	180	270	260	260	250	IPOP-SEF-CMA-ES [29]
VNS (Garcia)	1	2.6	5.1	4.1	8.8	8.2	7.9	8.3	8.8	17	VNS (Garcia) [11]

Table 5: 02-D, running time excess ERT/ERT_{best} on f_5 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

5 Linear slope												
Δf_{target}	ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT_{best}/D		0.5	0.5	1.83	76	100	100	100	100	100	100	ERT_{best}/D
ALPS	ALPS [17]	1	1.1	8.8	76	100	100	100	100	100	100	ALPS [17]
AMaLGA_M IDEA	AMaLGA_M IDEA [4]	1	1.1	5.3	16	18	18	18	18	18	18	AMaLGA_M IDEA [4]
avg NEWUOA	avg NEWUOA [31]	1	1.2	1.1	1.5	1.6	1.6	1.6	1.6	1.6	1.6	avg NEWUOA [31]
BayEDA_cG	BayEDA_cG [10]	1	1	3.3	92	100	100	100	100	100	100	BayEDA_cG [10]
BFGS	BFGS [30]	1	1	1.5	2.8	2.8	2.9	2.9	2.9	2.9	2.9	BFGS [30]
Cauchy EDA	Cauchy EDA [24]	1	1	16	17	17	17	17	17	17	17	Cauchy EDA [24]
BIPOP-CMA-ES	BIPOP-CMA-ES [15]	1	1	3.4	5.3	5.7	5.8	5.8	5.8	5.8	5.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	(1+1)-CMA-ES [2]	1	1	1.9	3.1	3.4	3.4	3.4	3.4	3.4	3.4	(1+1)-CMA-ES [2]
DASA	DASA [19]	1	1.9	19	32	40	46	53	60	66	80	DASA [19]
DEPSO	DEPSO [12]	1	1	6.1	34	35	36	36	36	36	36	DEPSO [12]
DIRECT	DIRECT [25]	1	1	3.4	2.8	4.2	4.2	4.2	4.2	4.2	4.2	DIRECT [25]
EDA-PSO	EDA-PSO [6]	1	1	5	15	16	17	17	17	17	17	EDA-PSO [6]
full_NEWUOA	full_NEWUOA [31]	1	1.3	1	1.2	1.4	1.4	1.4	1.4	1.4	1.4	full_NEWUOA [31]
G3-PCX	G3-PCX [26]	1	1.1	4.1	29	31	31	31	31	31	31	G3-PCX [26]
simple GA	simple GA [22]	1	1	4.2	310	2e3	4200	6300	9800	1.5e4	6.8e5	simple GA [22]
GLOBAL	GLOBAL [23]	1	1.1	4.4	69	70	70	70	70	70	70	GLOBAL [23]
iAMaLGA_M IDEA	iAMaLGA_M IDEA [4]	1	1	4.6	12	13	13	13	13	13	13	iAMaLGA_M IDEA [4]
LSfmnbnd	LSfmnbnd [28]	1	1	4.9	7.3	8.5	9.1	9.1	9.1	9.1	9.1	LSfmnbnd [28]
LSstep	LSstep [28]	1	1.2	59	79	91	91	91	91	91	91	LSstep [28]
MA-LS-Chain	MA-LS-Chain [21]	1	1.1	4.7	81	120	130	130	130	130	130	MA-LS-Chain [21]
MCS (Neum)	MCS (Neum) [18]	1	1	1.2	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	NELDER (Han) [16]	1	1	1.8	2.1	2.2	2.2	2.2	2.2	2.2	2.2	NELDER (Han) [16]
NELDER (Doe)	NELDER (Doe) [5]	1	1	1.3	1.9	1.9	1.9	1.9	1.9	1.9	1.9	NELDER (Doe) [5]
NEWUOA	NEWUOA [31]	1	1	1.1	1.5	1.5	1.5	1.5	1.5	1.5	1.5	NEWUOA [31]
(1+1)-ES	(1+1)-ES [1]	1	1	1.9	2.4	2.5	2.6	2.6	2.6	2.6	2.6	(1+1)-ES [1]
POEMS	POEMS [20]	1	1	1.40	150	170	180	190	190	190	190	POEMS [20]
PSO	PSO [7]	1	1.1	4.2	18	20	21	21	21	21	21	PSO [7]
PSO_Bounds	PSO_Bounds [8]	1	1	6.1	13	16	16	16	16	16	16	PSO_Bounds [8]
Monte Carlo	Monte Carlo [3]	1	1	4.4	530	4.9e4	22e-3/1e6	Monte Carlo [3]
Rosenbrock	Rosenbrock [27]	1	1	3.5	3.4	3.5	3.5	3.5	3.5	3.5	3.5	Rosenbrock [27]
IPOP-SEP-CMA-ES	IPOP-SEP-CMA-ES [29]	1	1	4	6.6	7.1	7.1	7.1	7.1	7.1	7.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	VNS (Garcia) [11]	1	1	6.3	27	27	27	27	27	27	27	VNS (Garcia) [11]

Table 6: 02-D, running time excess ERT/ERT_{best} on f_6 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

6 Attractive sector											
Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS	3.2	3.2	2.2	1.2	31	50	62	73	80	83	ALPS [17]
AMaLGaM IDEA	1.1	1.4	2.1	4.5	4.9	5.5	6.2	6.5	6.7	7	AMaLGaM IDEA [4]
avg NEWUOA	1.4	2.1	3.1	4.7	3.9	4.4	4.4	4.5	4.7	4.6	avg NEWUOA [31]
BayEDA _{cG}	2.8	1.9	1.5	160	640	<i>72e-2/2e3</i>					BayEDA _{cG} [10]
BFGS	4.3	4.4	4.2	3.4	2.7	2.4	2	1.9	1.7	1.6	BFGS [30]
Cauchy EDA	11	10	16	18	17	17	17	17	16	16	Cauchy EDA [24]
BIPOP-CMA-ES	3.9	3	2	2.8	3.6	3.9	4.2	4.2	4.1	4.3	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.2	3.3	2.1	3	2.3	2.2	2.2	2.3	2.2	2.1	(1+1)-CMA-ES [2]
DASA	30	29	23	22	18	19	19	18	18	18	DASA [19]
DEPSO	1.7	1.7	3.8	11	12	14	14	15	16	17	DEPSO [12]
DIRECT	1.4	1	1.4	7.6	5.8	120	800	1500	1200	970	DIRECT [25]
EDA-PSO	3.4	2.4	3.1	12	12	15	19	27	29	34	EDA-PSO [6]
full NEWUOA	1	2.2	3.4	3.7	3.2	3.5	3.7	3.7	4.1	4.5	full NEWUOA [31]
G3-PCX	2.3	1.5	2.3	4.5	3.7	3.9	3.9	3.8	3.8	4.1	G3-PCX [26]
simple GA	4.8	3.4	3.5	14	85	1e3	3100	4100	3600	4900	simple GA [22]
GLOBAL	3.7	2.9	2.3	8.8	7.4	6.2	5.2	4.5	3.9	3.2	GLOBAL [23]
iAMaLGaM IDEA	2.7	1.9	2.4	3.6	3.8	4	4.1	4.2	4.3	4.4	iAMaLGaM IDEA [4]
LSfminbd	19	190	280	370	290	260	210	180	150	120	LSfminbd [28]
LSstep	53	330	910	580	380	330	710	1200	<i>17e-4/1e4</i>	.	LSstep [28]
MA-LS-Chain	4.4	2.9	2.2	13	14	14	12	12	10	10	MA-LS-Chain [21]
MCS (Neum)	1.4	190	52	29	19	42	100	110	100	120	MCS (Neum) [18]
NELDER (Han)	2.1	1.5	1	1	1.1	1.1	1.1	1.1	1.1	1.1	NELDER (Han) [16]
NELDER (Doe)	1.6	2	1.3	1.3	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1.2	2.4	2.4	4.4	3.9	4.4	4.7	4.8	5	4.9	NEWUOA [31]
(1+1)-ES	2.4	2.2	2.5	3.7	3.6	3.6	3.4	3.4	3.3	3.2	(1+1)-ES [1]
POEMS	200	160	99	130	120	140	130	140	180	180	POEMS [20]
PSO	1.5	1.1	2.1	4.6	7.9	18	23	29	32	36	PSO [7]
PSO.Bounds	2.2	1.5	2.6	7	37	77	130	140	140	170	PSO.Bounds [8]
Monte Carlo	3	2.3	2.7	16	53	780	1.3e4	8.1e4	1.5e5	<i>28e-5/1e6</i>	Monte Carlo [3]
Rosenbrock	4	3	2.2	2.1	1.8	1.8	1.8	1.8	1.7	1.5	Rosenbrock [27]
IPOP-SEFP-CMA-ES	4.7	3.1	1.7	4.1	3.8	4.5	4.6	4.7	4.6	4.4	IPOP-SEFP-CMA-ES [29]
VNS (Garcia)	2.6	2.7	1.9	7.2	6.9	6.7	6.3	6.3	6.1	5.7	VNS (Garcia) [11]

Table 7: 02-D, running time excess ERT/ERT_{best} on f_7 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

7 Step-ellipsoid											
	$1e+03$	$1e+02$	$1e+01$	$1e+00$	$1e-01$	$1e-02$	$1e-03$	$1e-04$	$1e-05$	$1e-07$	Δf_{target} ERT_{best}/D
ALPS	1.1	1.4	4.1	4.7	12	9.5	11	11	11	13	ALPS [17]
AMaLGaM IDEA	1.1	1.5	3.4	20	8.1	2.7	2.5	2.5	2.5	2.4	AMaLGaM IDEA [4]
avg NEWUOA	1.7	2.7	4	3.7	6.8	5	10	10	10	9	avg NEWUOA [31]
BayEDA-cG	1.5	1.7	4.2	3.1	79	85	76	76	76	110	BayEDA-cG [10]
BFGS	1.6	3.7	10	19	34	<i>76e-2/200</i>	BFGS [30]
Cauchy-EDA	5.5	8.4	19	7.6	5.3	2	1.9	1.9	1.9	2.1	Cauchy-EDA [24]
BIPOP-CMA-ES	1.9	1.9	3.2	2.6	3.4	1.5	1.5	1.5	1.5	1.6	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.5	1.4	2.7	1.8	2.8	1	1	1	1	1	(1+1)-CMA-ES [2]
DASA	30	59	170	170	310	240	440	440	440	390	DASA [19]
DEPSO	1.7	1.7	6.5	4.8	4.9	2.6	3.1	3.1	3.1	3.6	DEPSO [12]
DIRECT	1.4	1	2.1	1.3	1	2.7	3	3	3	2.7	DIRECT [25]
EDA-PSO	1.5	1.8	3.7	3.1	6.2	6.2	9	9	9	14	EDA-PSO [6]
full NEWUOA	1.9	2.7	2	3.7	3.7	1.7	2.9	2.9	2.9	2.7	full NEWUOA [31]
G3-PCX	1.3	1.5	4.5	12	35	19	21	21	21	19	G3-PCX [26]
simple GA	1.6	1.6	5.2	3.9	22	24	47	47	47	67	simple GA [22]
GLOBAL	1.2	1.8	6.8	4.1	7.5	2.7	4.4	4.4	4.4	3.9	GLOBAL [23]
iAMaLGaM IDEA	1.8	1.8	3.9	12	4.7	2.8	2.5	2.5	2.5	2.4	iAMaLGaM IDEA [4]
LSfminbnd	1.3	1.1	6.3	11	66	55	500	500	500	960	LSfminbnd [28]
LStep	28	28	260	250	460	1500	<i>29e-3/1e4</i>	.	.	.	LStep [28]
MA-LS-Chain	1.7	2.3	5.8	3.4	4.7	3.6	4.6	4.6	4.6	4.7	MA-LS-Chain [21]
MCS (Neum)	1.4	1.4	1	4.1	4.5	2.2	6.5	6.5	6.5	6	MCS (Neum) [18]
NELDER (Han)	1.5	1.3	2.5	25	18	6.6	6.5	6.5	6.5	5.9	NELDER (Han) [16]
NELDER (Doe)	1.8	1.6	2.6	1	8.5	5.4	5.2	5.2	5.2	5.4	NELDER (Doe) [5]
NEWUOA	1.7	2	2.5	9.3	9.3	6	14	14	14	12	NEWUOA [31]
(1+1)-ES	2.3	3.3	5.6	4.1	4.3	1.8	3.3	3.3	3.3	3	(1+1)-ES [1]
POEMS	220	210	180	45	41	21	23	23	23	28	POEMS [20]
PSO	1.5	1.3	4.1	3.5	4.8	3.2	3.6	3.6	3.6	4.4	PSO [7]
PSO_Bounds	1.3	1.6	6.2	3.4	5.8	5	6.7	6.7	6.7	14	PSO_Bounds [8]
Monte Carlo	1.7	1.5	4.6	4.5	43	87	150	150	150	950	Monte Carlo [3]
Rosenbrock	16	42	150	120	170	78	190	190	190	170	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	2.1	5.5	2.7	2.8	1.2	1.3	1.3	1.3	1.5	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	2.4	3.9	3.8	5.1	2.1	2	2	2	2	VNS (Garcia) [11]

Table 8: 02-D, running time excess ERT/ERT_{best} on f_8 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS		0.6	1.6	2.7	6	18.3	23.1	43.2	46.1	47	56	ALPS [17]
AMaLgAM IDEA		2.9	2.8	4.7	19	31	66	54	74	94	130	AMaLgAM IDEA [4]
avg NEWUOA		2.4	4.1	6.2	10	6.8	7	4.4	4.7	5.1	5	avg NEWUOA [31]
BayEDAacG		3.9	2.5	2.6	4.6	2.4	2.4	1.4	1.4	1.4	1.3	BayEDAacG [10]
BFGS		2.3	2.9	5.6	11	48	350	<i>53e-3/2e3</i>				BFGS [30]
Cauchy EDA		7.5	4.9	4.1	5.1	2.4	2.2	1.3	1.3	1.3	1.1	Cauchy EDA [24]
BIPOP-CMA-ES		15	11	10	24	19	21	12	13	14	13	BIPOP-CMA-ES [15]
(1+1)-CMA-ES		3.1	3.3	3.5	7.1	9.2	11	6.4	6.5	6.7	6.2	(1+1)-CMA-ES [2]
DASA		6.4	4.3	3.8	11	6.9	7	4.2	4.1	4.3	4	DASA [19]
DEPSO		31	33	110	520	480	680	520	580	700	820	DEPSO [12]
DIRECT		4	3.3	3.6	14	15	25	28	42	65	<i>76e-7/2e3</i>	DIRECT [25]
EDA-PSO		1	1	1.4	5	4.4	8.7	10	16	17	21	EDA-PSO [6]
full NEWUOA		1.9	3	5.4	11	50	98	97	140	180	220	full NEWUOA [31]
G3-PCX		6.6	3.9	7	7	3.2	2.8	1.6	1.5	1.5	1.3	G3-PCX [26]
simple GA		2.8	4	5	24	16	18	11	11	11	9.6	simple GA [22]
GLOBAL		2	2.9	8.4	34	87	170	1300	8900	<i>61e-5/1e5</i>		GLOBAL [23]
iAMaLgAM IDEA		4.4	4.5	14	19	8.2	7.2	4.1	3.9	3.9	3.4	iAMaLgAM IDEA [4]
LSfminbd		2.3	2.8	4.4	12	8	8.4	5	5.2	5.5	5.2	LSfminbd [28]
LSstep		16	7	420	1500	2300	6300	<i>90e-2/1e4</i>				LSstep [28]
MA-LS-Chain		67	51	37	1500	3600	6100	<i>32e-2/1e4</i>				MA-LS-Chain [21]
MCS (Neum)		2.7	3.6	7.2	16	10	15	9	8.8	9	8.5	MCS (Neum) [18]
NELDER (Han)		1	1.2	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)		1.9	1.4	2.1	3.7	2	2	1.1	1.2	1.2	1.2	NELDER (Doe) [5]
NEWUOA		3	3.2	4.6	6.2	2.9	2.7	1.6	1.5	1.6	1.5	(1+1)-ES [1]
(1+1)-ES		3.8	2.8	4.3	7	3.5	3.2	1.9	1.8	1.8	1.6	POEMS [20]
POEMS		2.3	2.2	47	59	23	34	35	51	70	95	POEMS [20]
PSO		230	2.6	6.5	11	16	27	26	37	49	67	PSO [7]
PSO.Bounds		3.7	4.3	6	19	24	61	69	120	150	200	PSO.Bounds [8]
Monte Carlo		2.7	3.2	5.8	19	72	670	2200	3.9e4	3.1e5	<i>17e-5/1e6</i>	Monte Carlo [3]
Rosenbrock		5.8	3.4	4.9	10	5.2	4.8	2.8	2.7	2.8	2.5	Rosenbrock [27]
IPOP-SEF-CMA-ES		6.4	3.9	5.2	19	17	17	9.5	9.3	9.6	8.7	IPOP-SEF-CMA-ES [29]
VNS (Garcia)		9.5	4.8	8.1	16	10	11	6.9	6.8	7.2	6.7	VNS (Garcia) [11]

Table 9: 02-D, running time excess ERT/ERT_{best} on f_9 , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS	3.3	7.2	33	0.5	8.9	15	21.9	33.8	81	40.7	46.2	ALPS [17]
AMaLGaM IDEA	4.2	13	22	6.3	6.3	9.5	9.5	7.5	7.4	7.7	7.6	AMaLGaM IDEA [4]
avg NEWUOA	7.7	10	22	4.7	4	3.2	2.3	2.3	2.1	2	1.9	avg NEWUOA [31]
BayEDAacG	3.8	11	29	10	99	600	<i>66e-3/2e3</i>	<i>1.4</i>	1.3	1.2	1.1	BayEDAacG [10]
BFGS	4.2	9.2	16	2.4	2.3	1.9	1.4	1.4	1.3	1.2	1.1	BFGS [30]
Cauchy EDA	16	37	59	14	20	19	14	14	14	14	14	Cauchy EDA [24]
BIPOP-CMA-ES	2.6	10	19	4.6	7.1	7.5	5.8	5.6	5.6	5.8	5.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	3.5	9.9	26	8.8	8	7.3	5.4	5	5	5	4.9	(1+1)-CMA-ES [2]
DASA	65	110	320	250	290	330	320	380	380	550	740	DASA [19]
DEPSO	2.7	12	58	12	12	20	19	25	25	45	97	DEPSO [12]
DIRECT	1	1	1	2	5	5.8	8.3	14	18	18	25	DIRECT [25]
EDA-PSO	3.8	12	47	8.5	27	51	78	120	150	150	200	EDA-PSO [6]
full NEWUOA	7.1	12	24	2.7	2.2	1.8	1.3	1.2	1.1	1.1	1.1	full NEWUOA [31]
G3-PCX	4.1	10	28	15	20	18	14	13	13	13	11	G3-PCX [26]
simple GA	5	15	44	22	90	190	2200	2200	2200	1e4	1.5e4	simple GA [22]
GLOBAL	3.5	11	30	9.1	11	7.9	5.2	4.7	4.7	4.5	4.2	GLOBAL [23]
iAMaLGaM IDEA	3.1	7.9	29	6	20	210	3100	4100	3600	5.1	5.3	iAMaLGaM IDEA [4]
LSfminbd	6.2	15	20	20	670	670	1800	2100	3800	<i>76e-3/1e4</i>	<i>76e-3/1e4</i>	LSfminbd [28]
LSstep	270	610	750	230	670	1800	1800	2100	3800	<i>76e-3/1e4</i>	<i>76e-3/1e4</i>	LSstep [28]
MA-LS-Chain	5	9.5	35	8.6	13	13	11	10	10	10	11	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	2.7	3.6	10	1.6	2	1.8	1.3	1.3	1.2	1.2	1.2	NELDER (Han) [16]
NELDER (Doe)	4.1	6.9	11	2.3	2.6	2.1	1.5	1.4	1.4	1.4	1.4	NELDER (Doe) [5]
NEWUOA	5.2	8.3	24	3.6	3.3	2.7	1.9	1.8	1.8	1.8	1.7	NEWUOA [31]
(1+1)-ES	4.4	8.1	19	81	120	120	100	110	110	130	160	(1+1)-ES [1]
POEMS	360	450	560	65	78	110	98	98	110	130	160	POEMS [20]
PSO	4	15	37	8.7	12	24	28	38	38	49	67	PSO [7]
PSO_Bounds	3.9	9	48	11	27	96	120	160	200	200	240	PSO_Bounds [8]
Monte Carlo	3	10	47	17	110	900	3600	6.9e4	3.7e5	<i>16e-5/1e6</i>	<i>16e-5/1e6</i>	Monte Carlo [3]
Rosenbrock	8.9	12	22	2.6	3.1	2.9	2.2	2.2	2.2	2.2	2.2	Rosenbrock [27]
IPOP-SEF-CMA-ES	3.1	9.5	16	7.6	15	14	10	9.3	9.4	9.4	9	IPOP-SEF-CMA-ES [29]
VNS (Garcia)	4.8	21	45	14	15	12	9.8	9.4	9.8	9.8	10	VNS (Garcia) [11]

Table 10: 02-D, running time excess ERT/ERT_{best} on f_{10} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT _{best} /D	2.9	5.7	14.9	22.9	26.9	30.4	34.2	37.9	40.9	48.8	ERT _{best} /D
ALPS	22	25	47	69	160	350	780	1600	2100	3200	ALPS [17]
AMaLGaM IDEA	6.7	5.7	3	3	3.8	4	4.1	4.1	4.3	4.4	AMaLGaM IDEA [4]
avg NEWUOA	2.6	3.6	3.8	4.8	6.9	7.6	8.8	9.5	9.9	11	avg NEWUOA [31]
BayEDA _c G	17	13	60	190	310	<i>33e-1/2e3</i>	·	·	·	·	BayEDA _c G [10]
BFGS	2.3	1.5	1	1.4	1.4	1.4	1.4	2.6	6.3	24	BFGS [30]
Cauchy EDA	14	13	7.4	6.4	7	7	7.4	7.7	8	8.4	Cauchy EDA [24]
BIPOP-CMA-ES	12	12	7.9	9	8.5	7.9	7.7	7.4	7.3	6.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	7.3	5.8	7.2	6.6	6.3	5.8	5.5	5.3	5.2	4.8	(1+1)-CMA-ES [2]
DASA	22	15	8900	5.2e4	6.1e4	9.5e4	1.2e5	1.1e5	1e5	8.6e4	DASA [19]
DEPSO	16	26	80	110	330	310	<i>51e-2/2e3</i>	·	·	·	DEPSO [12]
DIRECT	3.9	4.3	3.9	9.5	20	68	120	190	220	460	DIRECT [25]
EDA-PSO	17	26	43	140	330	640	1100	2100	3e3	8600	EDA-PSO [6]
full NEWUOA	2	3	3.8	4.5	6	6.4	7.1	7.7	8.2	9	full NEWUOA [31]
G3-PCX	11	9.5	26	39	39	37	34	31	29	25	G3-PCX [26]
simple GA	27	51	77	700	2800	4300	4.2e4	3.8e4	<i>23e-3/1e5</i>	·	simple GA [22]
GLOBAL	18	19	11	7.4	6.4	5.8	5.3	4.9	4.6	4	GLOBAL [23]
iAMaLGaM IDEA	5.5	4	3.3	3.7	4.1	4.1	4	4.1	4.2	4.1	iAMaLGaM IDEA [4]
LSfminbd	1.8	1	770	6300	<i>15e+0/1e4</i>	·	·	·	·	·	LSfminbd [28]
LSstep	2.1	1.2	770	2800	<i>15e+0/1e4</i>	·	·	·	·	·	LSstep [28]
MA-LS-Chain	16	20	13	18	19	20	19	18	18	17	MA-LS-Chain [21]
MCS (Neum)	1	1.2	1.7	8.7	47	130	520	1100	1300	3700	MCS (Neum) [18]
NELDER (Han)	3	2.2	1.2	1.1	1.1	1.1	1.1	1.1	1.1	1	NELDER (Han) [16]
NELDER (Doe)	3.2	2.2	1.2	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	2.3	1.9	3.1	4.3	6.5	7.3	8.5	9.6	10	11	NEWUOA [31]
(1+1)-ES	6.3	5.3	8700	2.4e4	7.7e4	1.5e5	4.3e5	<i>13e-2/1e6</i>	·	·	(1+1)-ES [1]
POEMS	110	90	300	540	1400	2100	2400	3200	3700	6400	POEMS [20]
PSO	23	26	180	280	480	650	850	990	1100	1900	PSO [7]
PSO_Bounds	21	24	530	770	740	830	1500	1900	1900	2100	PSO_Bounds [8]
Monte Carlo	23	55	110	690	3900	4.4e4	1.3e5	3.8e5	<i>61e-4/1e6</i>	·	Monte Carlo [3]
Rosenbrock	4.8	2.8	3.1	3.4	3.2	3	2.9	2.8	3.2	3	Rosenbrock [27]
IPOP-SEFP-CMA-ES	8.3	12	16	14	16	15	13	12	12	11	IPOP-SEFP-CMA-ES [29]
VNS (Garcia)	22	25	17	12	12	11	10	9.4	9.1	8.3	VNS (Garcia) [11]

Table 11: 02-D, running time excess ERT/ERT_{best} on f_{11} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT _{best} /D	ERT_{best}/D
ALPS	17	40	35	80	200	410	30.8	33.7	1200	1700	3400	ALPS [17]
AMaLGaM IDEA	4.8	5.4	3	3.5	4.2	3.9	3.9	4.2	4.4	4.4	4.6	AMaLGaM IDEA [4]
avg NEWUOA	1.3	1.5	1.5	3.3	5.1	5.4	5.4	6.8	7.3	8	8.8	avg NEWUOA [31]
BayEDAacG	9.3	18	31	150	1100	<i>14e-1/2e3</i>	<i>14e-1/2e3</i>	BayEDAacG [10]
BFGS	1.6	1.7	1.2	1.6	2	1.7	1.7	1.9	2.7	5.7	36	BFGS [30]
Cauchy EDA	13	15	6.7	7.4	8.1	8	8	8.3	8.1	8.9	9	Cauchy EDA [24]
BIPOP-CMA-ES	4.7	8.7	7.9	8.8	9.2	8.2	8.2	8	7.6	7.5	6.8	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.8	5.9	5.8	6.4	6.6	5.7	5.7	5.6	5.4	5.1	4.7	(1+1)-CMA-ES [2]
DASA	15	15	9e3	4e4	5.4e4	5.7e4	5.7e4	5.3e4	5e4	4.7e4	4.2e4	DASA [19]
DEPSO	24	34	34	110	<i>45e-2/2e3</i>	DEPSO [12]
DIRECT	3.3	5.1	2.6	5.2	28	49	49	58	190	270	460	DIRECT [25]
EDA-PSO	8.6	27	96	260	460	990	990	1900	2900	6500	<i>36e-6/1e5</i>	EDA-PSO [6]
full NEWUOA	1.6	3.5	2.7	4.4	6.2	6.2	6.2	7	7.7	8	8.6	full NEWUOA [31]
G3-PCX	9.5	9.1	9.7	25	28	36	36	35	33	32	27	G3-PCX [26]
simple GA	20	57	53	220	5e3	4.6e4	4.6e4	<i>14e-2/1e5</i>	.	.	.	simple GA [22]
GLOBAL	17	23	9.2	7.5	6.9	5.8	5.8	5.4	4.9	4.6	4	GLOBAL [23]
iAMaLGaM IDEA	4.5	6	2.8	3.3	4	3.8	3.8	4	3.9	3.9	4	iAMaLGaM IDEA [4]
LSfminbnd	2.1	1.8	500	2900	5500	<i>96e-1/1e4</i>	<i>96e-1/1e4</i>	LSfminbnd [28]
LSstep	1	1	380	1800	2600	<i>81e-1/1e4</i>	<i>81e-1/1e4</i>	LSstep [28]
MA-LS-Chain	12	15	11	18	23	21	21	20	20	20	17	MA-LS-Chain [21]
MCS (Neum)	1	1.1	87	120	170	300	300	920	1300	2e3	<i>91e-5/3e4</i>	MCS (Neum) [18]
NELDER (Han)	2	2.1	1	1.1	1.1	1	1	1.1	1.1	1.1	1	NELDER (Han) [16]
NELDER (Doe)	2.2	2.4	1	1	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1.2	1.5	1.5	3.2	5.5	6.1	6.1	6.9	7.7	8.4	11	NEWUOA [31]
(1+1)-ES	4.2	850	7700	2.1e4	6e4	2.3e5	2.3e5	4.4e5	<i>63e-3/1e6</i>	.	.	(1+1)-ES [1]
POEMS	55	83	1e3	1400	2100	2800	2800	4e3	6500	7900	7100	POEMS [20]
PSO	10	23	480	530	660	670	670	860	1e3	1300	1900	PSO [7]
PSO_Bounds	11	21	3200	5200	6300	5500	5500	6700	6300	6100	5500	PSO_Bounds [8]
Monte Carlo	16	51	94	870	6300	4.3e4	4.3e4	2.1e5	<i>97e-4/1e6</i>	.	.	Monte Carlo [3]
Rosenbrock	2.3	2.9	2.4	2.7	3	2.7	2.7	2.6	2.5	2.6	2.5	Rosenbrock [27]
IPOP-SEP-CMA-ES	5.4	6.9	13	17	17	14	14	13	13	12	11	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	8.4	14	12	12	12	11	11	10	9.7	9.4	8.6	VNS (Garcia) [11]

Table 12: 02-D, running time excess ERT/ERT_{best} on f_{12} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS		5	9.17	16.9	23	37.6	47	52.4	62.7	76.3	97.4	ALPS [17]
AMaLgAM IDEA	5.4	19	37	40	51	76	94	130	210	230	370	AMaLgAM IDEA [4]
avg NEWUOA	1.7	1.7	1.1	1	1.6	1.5	1.5	1.5	1.5	1.4	1.4	avg NEWUOA [31]
BayEDAacG	40	26	69	69	87	<i>67e-2/2e3</i>						BayEDAacG [10]
BFGS	1.8	1.8	1.1	1.2	3.2	3.1	2.9	2.8	2.6	2.4	4.2	BFGS [30]
Cauchy EDA	11	9.9	14	14	24	19	18	18	17	15	14	Cauchy EDA [24]
BIPOP-CMA-ES	6	6.1	7.9	12	12	9.9	9.1	9	11	9.6	8.2	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	4.9	7	9.4	13	13	10	8.9	8.7	7.6	6.5	5.6	(1+1)-CMA-ES [2]
DASA	16	64	2700	6800	6100	8800	1.4e4	1.2e4	9700	7900	45	DASA [19]
DEPSO	17	16	41	55	51	48	45	40	40	35	290	DEPSO [12]
DIRECT	3	3.3	6.2	35	80	70	160	270	250	250	290	DIRECT [25]
EDA-PSO	11	24	40	98	160	300	790	1e3	1e3	1e3	820	EDA-PSO [6]
full NEWUOA	1.4	1.9	4.6	5.2	3.8	3.4	3.3	3	2.7	2.4	2.4	full NEWUOA [31]
G3-PCX	9.1	6.1	12	29	34	34	32	31	29	29	28	G3-PCX [26]
simple GA	23	39	93	170	580	1e3	2400	2700	2200	1900	1900	simple GA [22]
GLOBAL	11	11	8.1	8.3	7.2	6.4	6.4	5.9	5	5	4.4	GLOBAL [23]
iAMaLgAM IDEA	4.1	2.5	4.5	7	6.4	6.4	6.4	6	5.8	5.4	5.4	iAMaLgAM IDEA [4]
LSfminbd	1.7	1	590	1200	770	630	570	490	410	410	330	LSfminbd [28]
LSstep	500	280	300	230	230	350	720	600	820	820	640	LSstep [28]
MA-LS-Chain	13	13	12	15	13	12	13	13	12	12	10	MA-LS-Chain [21]
MCS (Neum)	1	1.1	62	49	32	26	24	28	39	39	30	MCS (Neum) [18]
NELDER (Han)	1.9	1.4	1	1	1	1	1	1	1	1	1	NELDER (Han) [16]
NELDER (Doe)	2	1.4	1.1	1.6	1.6	1.6	1.7	1.6	1.4	1.4	1.3	NELDER (Doe) [5]
NEWUOA	1.5	1.1	1.9	2.9	2.3	2.1	2	1.8	1.8	1.6	1.4	NEWUOA [31]
(1+1)-ES	3.8	1500	6800	1.7e4	2.3e4	5.5e4	1.3e5	2.3e5	1.9e5	25e-3/1e6	1.5e4	(1+1)-ES [1]
POEMS	64	79	83	650	1100	1200	1600	2100	2900	2900	300	POEMS [20]
PSO	11	12	19	57	110	130	160	180	220	220	300	PSO [7]
PSO.Bounds	12	19	230	440	390	510	690	630	560	560	560	PSO.Bounds [8]
Monte Carlo	18	27	97	580	3200	1.6e4	1.4e5	38e-4/1e6				Monte Carlo [3]
Rosenbrock	3.3	2.9	2.5	3.6	3	5.4	5.1	4.5	3.9	3.9	3.3	Rosenbrock [27]
IPOP-SEFP-CMA-ES	7.4	9.2	7.6	9.5	9.6	8.8	8.5	8.1	7	7	6.3	IPOP-SEFP-CMA-ES [29]
VNS (Garcia)	17	17	15	13	8.8	7.5	7.1	6.4	5.6	5.6	4.9	VNS (Garcia) [11]

Table 13: 02-D, running time excess ERT/ERT_{best} on f_{13} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$1e+03$	$1e+02$	$1e+01$	$1e+00$	$1e-01$	$1e-02$	$1e-03$	$1e-04$	$1e-05$	$1e-07$	Δf_{target} ERT_{best}/D
ALPS	0.5	2.3	11.3	17.6	23.2	30	35.4	41.5	47.4	61.1	Δf_{target} ERT_{best}/D
AMaLgAM IDEA	1.3	3.2	13	47	100	170	300	1300	3700	2.9e4	ALPS [17]
avg NEWUOA	1.1	3.4	2.6	3.2	3.6	3.7	3.9	4	3.9	4.1	AMaLgAM IDEA [4]
BayEDAeG	1.8	6.7	6.7	17	38	54	73	130	140	770	avg NEWUOA [31]
BFGS	1.4	2.4	52	140	570	950	<i>11e-1/2e3</i>				BayEDAeG [10]
Cauchy EDA	1.2	5	6.8	15	45	74	160	660	580	<i>67e-5/5e3</i>	BFGS [30]
BIPOP-CMA-ES	4.1	15	7.3	7.7	7.7	8.2	8.5	8.6	8.5	8.5	Cauchy EDA [24]
(1+1)-CMA-ES	1.3	4.3	3.2	5.4	5.7	5.9	6.4	6.1	6.6	7	BIPOP-CMA-ES [15]
DASA	13	90	540	850	2600	4900	1.6e4	4.7e4	1.4e5	<i>62e-5/1e6</i>	(1+1)-CMA-ES [2]
DEPSO	1.1	6.1	8.4	25	63	120	<i>18e-3/2e3</i>				DASA [19]
DIRECT	1	1	2.5	4.2	5.1	8.7	24	49	74	120	DEPSO [12]
full NEWUOA	1.4	3.5	6.4	42	180	270	710	4e3	3.1e4	<i>27e-5/1e5</i>	DIRECT [25]
G3-PCX	1.5	5.2	8.5	12	31	76	140	290	760	1800	EDA-PSO [6]
simple GA	1.2	3.9	13	30	36	47	50	55	70	61	full NEWUOA [31]
GLOBAL	1.3	3.7	25	170	1100	2.2e4	<i>25e-3/1e5</i>				G3-PCX [26]
iAMaLgAM IDEA	1.3	2.8	9.2	9.3	7.3	6	13	<i>67e-5/400</i>			simple GA [22]
LSfminbnd	1	16	52	110	170	470	850	3.6	3.6	3.7	GLOBAL [23]
LSstep	28	420	280	570	1e3	1500	<i>35e-2/1e4</i>				iAMaLgAM IDEA [4]
MA-LS-Chain	1.1	3.3	8.7	17	18	21	23	21	19	22	LSfminbnd [28]
MCS (Neum)	1	4.7	23	20	170	960	2200	2500	<i>75e-4/3e4</i>		LSstep [28]
NELDER (Han)	1.7	1.6	1	1	1	1	1	1	1.1	1	MA-LS-Chain [21]
NELDER (Doe)	1.3	2.2	1.1	1.1	1	1	1	1	1.1	1	MCS (Neum) [18]
(1+1)-ES	1.6	2.8	6.3	10	22	25	72	62	91	150	NELDER (Han) [16]
POEMS	1.9	31	37	94	210	370	790	4200	8100	3.7e4	NELDER (Doe) [5]
PSO	170	110	48	93	140	330	1100	2300	6300	2.4e4	NEWUOA [31]
PSO_Bounds	1.1	3.8	9.2	43	120	260	620	1200	2900	1.1e4	(1+1)-ES [1]
Monte Carlo	1.6	5.4	18	280	1.2e4	1.1e5	<i>32e-3/1e6</i>				POEMS [20]
Rosenbrock	3.2	4.8	5.6	7	7.5	18	28	43	70	170	PSO [7]
IPOP-SEP-CMA-ES	1.1	3.7	13	20	18	15	14	14	13	11	PSO_Bounds [8]
VNS (Garcia)	1.4	3.9	8.8	9.7	9.6	8.8	9.2	9.1	8.6	8.4	Monte Carlo [3]
											Rosenbrock [27]
											IPOP-SEP-CMA-ES [29]
											VNS (Garcia) [11]

Table 14: 02-D, running time excess ERT/ERT_{best} on f_{14} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

14 Sum of different powers													
	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}	
	ERT_{best}/D	0.5	0.5	0.7	3.7	8.1	12.2	18.9	27.8	33.7	45.1	ERT_{best}/D	
ALPS	1	1	1	1.6	2.4	14	60	75	83	130	530	ALPS [17]	
AMaLgAM IDEA	1	1.2	1.6	3.3	3.3	3.9	4.7	4.2	3.9	3.8	4.2	AMaLgAM IDEA [4]	
avg NEWUOA	1	1.4	3.4	2.2	2.2	1.4	1.3	1.6	1.8	2.2	6.8	avg NEWUOA [31]	
BayEDA-cG	1	1	1.9	1.8	1.8	10	25	67	98	180	<i>12e-5/2e3</i>	BayEDA-cG [10]	
BFGS	1	1.4	2.1	2.8	1.8	1.7	1.4	1.1	1.1	1	6	BFGS [30]	
Cauchy-EDA	1	4.6	13	13	13	12	11	10	8.6	8.9	8.5	Cauchy-EDA [24]	
BIPOP-CMA-ES	1	1.1	1.9	2.5	2.5	3	4.2	4.6	5.3	5.5	7.1	BIPOP-CMA-ES [15]	
(1+1)-CMA-ES	1	1.4	1.7	3.1	3.4	3.6	4	3.9	4.4	4.4	4.7	(1+1)-CMA-ES [2]	
DASA	1	18	22	22	22	16	18	33	590	9300	<i>3.1e5</i>	DASA [19]	
DEPSO	1	1	1.4	5.2	10	16	17	18	18	55	<i>17e-7/2e3</i>	DEPSO [12]	
DIRECT	1	1	1	1	1.3	2.1	2.8	6	8.6	12	32	DIRECT [25]	
EDA-PSO	1	1.2	1.4	2.9	8.2	12	15	74	160	1100	1100	EDA-PSO [6]	
full NEWUOA	1	1.4	3.2	1.4	1	1	1	1.1	1.1	1.5	3.7	full NEWUOA [31]	
G3-PCX	1	1.2	1.8	6.3	6.3	5.9	6.6	7.6	9.1	9.1	11	G3-PCX [26]	
simple GA	1	1.1	1	1	4	41	200	280	630	3200	<i>58e-7/1e5</i>	simple GA [22]	
GLOBAL	1	1.1	1.7	5.5	13	13	13	8.8	6.2	8.2	<i>34e-7/300</i>	GLOBAL [23]	
iAMaLgAM IDEA	1	1.5	1.6	3.7	3.9	4	3.9	3.4	3.4	3.5	3.6	iAMaLgAM IDEA [4]	
LSfminbd	1	1.3	4.7	5.4	5.4	3	6.2	76	1500	<i>23e-5/1e4</i>	.	LSfminbd [28]	
LSstep	1	55	40	73	73	50	120	1600	5100	<i>23e-4/1e4</i>	.	LSstep [28]	
MA-LS-Chain	1	1.3	1.7	3.1	3.1	9.6	15	13	12	12	17	MA-LS-Chain [21]	
MCS (Neum)	1	1	1	1	1.4	1.7	2.8	3.1	23	23	8200	MCS (Neum) [18]	
NELDER (Han)	1	1.5	2.1	1.4	1.4	1.4	1.4	1.2	1	1	1.1	NELDER (Han) [16]	
NELDER (Doe)	1	1.1	1.3	1.4	1.3	1.3	1.1	1.1	1	1	1	NELDER (Doe) [5]	
NEWUOA	1	1.1	3.7	2.4	1.6	1.5	1.6	1.8	1.8	2.1	5.4	NEWUOA [31]	
(1+1)-ES	1	1.7	2.3	2.5	2.5	2.5	3.4	9.2	160	3400	<i>22e-7/1e6</i>	(1+1)-ES [1]	
POEMS	1	140	190	86	73	160	180	180	330	3300	3300	POEMS [20]	
PSO	1	1.1	1.4	4.8	13	25	36	48	85	1700	1700	PSO [7]	
PSO-Bounds	1	1.1	1.5	2.7	14	45	72	110	180	180	1200	PSO-Bounds [8]	
Monte Carlo	1	1	1.8	2.6	31	560	7200	1.1e5	4.2e5	4.2e5	<i>15e-5/1e6</i>	Monte Carlo [3]	
Rosenbrock	1	2.2	4	1.9	1.6	1.6	1.9	1.8	2.4	2.4	3	Rosenbrock [27]	
IPOP-SEP-CMA-ES	1	1.2	1.6	1.8	4.4	4.9	7.4	9.7	10	10	11	IPOP-SEP-CMA-ES [29]	
VNS (Garcia)	1	1	2.1	6.2	10	9.4	9	8.1	8.6	8.6	9.3	VNS (Garcia) [11]	

Table 15: 02-D, running time excess ERT/ERT_{best} on f_{15} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D											ERT_{best}/D
ALPS	1.1	1.6	1.6	2.7	6.8	3.4	4.8	5.7	7.1	7.9	9.1	ALPS [17]
AMaLGaM IDEA	1.1	2.8	1.1	4.3	2.7	2.8	2.8	2.8	2.7	2.6	2.3	AMaLGaM IDEA [4]
avg NEWUOA	1	2.6	2.5	3.3	3.2	3.1	3.1	3.1	2.9	2.8	2.4	avg NEWUOA [31]
BayEDA-cG	1	2.2	2.1	2.1	8.2	7.6	26	<i>16e-2/2e3</i>				BayEDA-cG [10]
BFGS	1.2	17	4.2	4.6	7.9	7.7	7.3	7.3	7	6.6	5.8	BFGS [30]
Cauchy EDA	9.1	38	4.9	2.9	3.2	11	14	14	14	13	12	Cauchy EDA [24]
BIPOP-CMA-ES	1.2	2.9	1.1	1.8	2.1	2.2	2.2	2.2	2.1	2.1	1.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1.2	2.8	2.2	7.7	7.6	7.4	7.1	7.1	6.8	6.5	5.7	(1+1)-CMA-ES [2]
DASA	4.6	22	64	84	64	62	62	60	57	54	48	DASA [19]
DEPSO	1.1	1.6	2.9	3.8	1.7	2.2	2.5	2.5	2.6	3	6.3	DEPSO [12]
DIRECT	1	1	1	1	1	1	1	1	1	1	1	DIRECT [25]
EDA-PSO	1	3.3	2	9.3	6.1	8.3	8.3	8.3	8.5	8.4	8.1	EDA-PSO [6]
full NEWUOA	1.2	3.1	1.5	1.4	3.5	3.4	3.4	3.3	3.1	3	2.6	full NEWUOA [31]
G3-PCX	1.1	2.3	7.8	13	22	21	20	20	19	18	16	G3-PCX [26]
simple GA	1.2	2.3	4.2	18	13	34	34	96	98	100	120	simple GA [22]
GLOBAL	1.1	2.6	3	1.6	2.6	2.5	2.4	2.4	2.3	2.2	2	GLOBAL [23]
iAMaLGaM IDEA	1.1	2.5	1	4.2	5.1	5.1	5.1	5	4.8	4.6	4.1	iAMaLGaM IDEA [4]
LSfminbnd	1.1	6.2	3.7	20	36	51	51	66	210	<i>71e-2/9e3</i>		LSfminbnd [28]
LSstep	1.1	47	170	200	80	79	77	77	74	71	63	LSstep [28]
MA-LS-Chain	1.1	2	1.7	1.9	1.6	1.5	1.5	1.5	1.5	1.4	1.3	MA-LS-Chain [21]
MCS (Neum)	1	1	2.1	3.5	1.4	1.4	1.3	1.3	1.3	1.2	1.1	MCS (Neum) [18]
NELDER (Han)	1	1.9	8.4	7.3	9.7	9.4	9.4	9	8.6	8.2	7.1	NELDER (Han) [16]
NELDER (Doe)	1	3.2	1.1	4.1	3.4	3.3	3.2	3	2.9	2.7	2.4	NELDER (Doe) [5]
NEWUOA	1.1	11	11	4.1	3.4	3.3	3.2	3	2.9	2.7	2.4	NEWUOA [31]
(1+1)-ES	1.4	3.7	1.1	5.3	8.4	8.2	8.2	7.9	7.5	7.1	6.3	(1+1)-ES [1]
POEMS	28	120	16	19	18	20	20	21	21	22	22	POEMS [20]
PSO	1.1	2.4	1.9	4.1	16	16	16	16	16	16	15	PSO [7]
PSO-Bounds	1.2	2.3	1.7	6.6	3.9	7.3	9.2	11	11	11	12	PSO-Bounds [8]
Monte Carlo	1.1	2.1	2.4	64	150	1500	5800	1.264	<i>50e-4/1e6</i>			Monte Carlo [3]
Rosenbrock	1.3	19	15	9.7	9.5	9.2	8.9	8.5	8.5	8	7	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	3.8	1.5	2.9	2.1	2.2	2.2	2.1	2.1	2.1	1.9	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.3	3.4	1.9	2.4	2.4	2.4	2.3	2.4	2.7	3.7	VNS (Garcia) [11]

Table 16: 02-D, running time excess ERT/ERT_{best} on f_{16} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

16 Weierstrass															
Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D				
ALPS	1	1.3	4.57	5.6	9.1	14	19	25	34	37	ALPS [17]				
AMaLgAM IDEA	1	1.2	3.2	3.4	5.1	4.6	4.5	4.2	4.1	3.3	AMaLgAM IDEA [4]				
avg NEWUOA	1	1.2	1.5	9.1	5.5	6.8	13	21	37	73	avg NEWUOA [31]				
BayEDAacG	1	1.4	1.5	9.8	24	39	76	71	68	110	BayEDAacG [10]				
BFGS	1	1.1	40	150	170	270	<i>27e-2/6e3</i>	.	.	.	BFGS [30]				
Cauchy EDA	1	4.2	4.5	4.4	6.1	15	29	31	35	27	Cauchy EDA [24]				
BIPOP-CMA-ES	1	1	3.1	3.5	3.5	2.5	2.4	2.3	2.3	1.9	BIPOP-CMA-ES [15]				
(1+1)-CMA-ES	1	1.2	6	2.3	2.3	5.2	8.8	12	11	12	(1+1)-CMA-ES [2]				
DASA	1	9	29	150	180	130	210	250	340	530	DASA [19]				
DEPSO	1	1.5	3.9	10	10	9.6	26	38	72	<i>16e-4/2e3</i>	DEPSO [12]				
DIRECT	1	1.4	1.6	1	1	1	1	1.5	2	1.9	DIRECT [25]				
EDA-PSO	1	1.8	2.6	4.8	15	200	290	370	410	320	EDA-PSO [6]				
full NEWUOA	1	2.5	8.1	5.9	3.9	3.2	5.5	7.6	10	16	full NEWUOA [31]				
G3-PCX	1	1.4	2.8	8.9	3.1	4.5	4.8	5	5.3	11	G3-PCX [26]				
simple GA	1	1.2	2	4.1	16	42	180	450	690	690	simple GA [22]				
GLOBAL	1	1.7	3.9	5.1	2.4	1.4	1.5	1.4	1.7	1.5	GLOBAL [23]				
iAMaLgAM IDEA	1	1.1	1	6.9	7.4	9.1	9.2	8.6	8.3	7	iAMaLgAM IDEA [4]				
LSfminbd	1	3.6	5.6	5.7	5.4	8.3	14	33	38	110	LSfminbd [28]				
LSstep	1	1.5	1.6	11	23	63	70	150	200	150	LSstep [28]				
MA-LS-Chain	1	1.2	1.3	3.6	4.2	6.4	10	11	10	8.3	MA-LS-Chain [21]				
MCS (Neum)	1	1.1	5.1	6.7	2.7	6.8	6.8	10	29	120	MCS (Neum) [18]				
NELDER (Han)	1	1.3	1.2	7.6	4.4	4.7	4.3	4	3.8	2.9	NELDER (Han) [16]				
NELDER (Doe)	1	1.1	1.6	3.5	1.8	1.1	1.1	1	1	1	NELDER (Doe) [5]				
NEWUOA	1	2.4	9	10	6.8	6.9	22	37	44	77	NEWUOA [31]				
(1+1)-ES	1	1.7	35	38	35	33	56	73	84	120	(1+1)-ES [1]				
POEMS	1	98	71	650	200	110	110	110	110	88	POEMS [20]				
PSO	1	1.7	2.5	3.8	6.1	100	94	88	86	69	PSO [7]				
PSO_Bounds	1	1.2	2.8	6.4	11	110	120	120	120	100	PSO_Bounds [8]				
Monte Carlo	1	1.2	2.3	5	20	140	1200	2.4e4	7.2e4	<i>18e-5/1e6</i>	Monte Carlo [3]				
Rosenbrock	1	10	33	36	33	27	79	290	<i>19e-4/8e3</i>	.	Rosenbrock [27]				
IPOP-SEFP-CMA-ES	1	1.8	3.2	4.1	2.4	2.9	4	3.8	3.9	3.3	IPOP-SEFP-CMA-ES [29]				
VNS (Garcia)	1	1.2	4.6	5	4.8	4.9	4.7	4.7	5.6	6.8	VNS (Garcia) [11]				

Table 17: 02-D, running time excess ERT/ERT_{best} on f_{17} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

17 Schaffer F7, condition 10

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D											ERT_{best}/D
ALPS	1	0.5	1.2	1.5	2.8	16	15	17	12	12	11	ALPS [17]
AMaLGaM IDEA	1	1.5	1.5	1.3	1.3	4.8	2.7	4.5	3.3	2.9	2.1	AMaLGaM IDEA [4]
avg NEWUOA	1.1	1.3	12	4.6	13	8	33	120	<i>75e-4/5e3</i>	.	.	avg NEWUOA [31]
BayEDAacG	1	1.1	1	2	8	7	7	8.7	8.8	27	<i>87e-6/2e3</i>	BayEDAacG [10]
BFGS	1	6.4	15	15	16	90	<i>24e-2/2e3</i>	BFGS [30]
Cauchy EDA	1	7.9	18	18	120	56	28	20	11	16	13	Cauchy EDA [24]
BIPOP-CMA-ES	1	1.2	4.1	1.8	1.5	1	1	1	1	1.3	1.1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	12	3.1	3.1	5.9	14	14	14	16	10	(1+1)-CMA-ES [2]
DASA	1	1	21	29	37	52	33	93	340	220	220	DASA [19]
DEPSO	1	1.3	2.7	1.1	4.3	3.7	3.7	3.7	2.8	2.4	2.8	DEPSO [12]
DIRECT	1	1	1.4	1	1	1	1	1.4	1.2	1	1	DIRECT [25]
EDA-PSO	1.1	1.1	2.6	2	3.9	7.4	7.4	9.9	8.2	8	7.1	EDA-PSO [6]
full NEWUOA	1	1.4	8.2	4.4	4.4	14	21	53	48	<i>30e-4/6e3</i>	.	full NEWUOA [31]
G3-PCX	1	1.1	2.5	4.5	6.2	6.2	3.9	3.2	2.6	4.4	3	G3-PCX [26]
simple GA	1	1.2	2.1	5.1	47	61	61	91	120	150	150	simple GA [22]
GLOBAL	1	1.2	2.6	4	4.1	3.9	3.9	4.4	9.6	<i>75e-4/500</i>	.	GLOBAL [23]
iAMaLGaM IDEA	1	1.2	1.3	8.8	8.8	6.2	4.2	5.1	4.2	4	2.8	iAMaLGaM IDEA [4]
LSfminbnd	1	1.2	5.4	1.2	7.3	55	55	<i>16e-3/5e3</i>	.	.	.	LSfminbnd [28]
LSstep	1.1	2	42	40	35	35	44	82	390	<i>10e-4/1e4</i>	.	LSstep [28]
MA-LS-Chain	1.1	1.3	1.3	2.2	5.3	4.3	4.3	4.8	2.8	3.1	2.9	MA-LS-Chain [21]
MCS (Neum)	1	1	1.3	4.3	4.8	5.4	5.4	9.2	44	140	130	MCS (Neum) [18]
NELDER (Han)	1	1.5	130	28	20	20	14	11	12	12	6.3	NELDER (Han) [16]
NELDER (Doe)	1	1.5	1.4	1.5	3.3	3	3	3.1	7	5.9	4	NELDER (Doe) [5]
NEWUOA	1	1.9	7.7	6.8	18	33	33	120	<i>75e-4/5e3</i>	.	.	NEWUOA [31]
(1+1)-ES	1	1.1	2.7	5.9	6.7	4.8	4.8	8.5	13	23	15	(1+1)-ES [1]
POEMS	4.5	110	110	18	35	31	31	32	23	24	21	POEMS [20]
PSO	1.1	1.2	1.9	1.6	5	6.2	6.2	8.1	6.2	5.5	5.5	PSO [7]
PSO_Bounds	1	1.3	1.9	1.7	5.2	220	4900	22	15	21	30	PSO_Bounds [8]
Monte Carlo	1	1.1	1.7	5.2	83	140	500	7.4e4	<i>79e-4/1e6</i>	.	.	Monte Carlo [3]
Rosenbrock	1	20	45	83	140	500	500	350	<i>24e-2/5e3</i>	.	.	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.9	4	2.2	2.8	2.3	2.3	1.8	1.6	1.5	1.4	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2.5	5.7	4.7	4.7	2.7	2.9	2.6	6.7	32	VNS (Garcia) [11]

Table 18: 02-D, running time excess ERT/ERT_{best} on f_{18} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS	1.1	1.3	1.6	6.6	5.5	5.4	6.7	8.1	9.6	13	ALPS [17]
AMaLGaM IDEA	1.1	1.3	1.3	4.1	1	1	1.1	1.2	1.1	1.1	AMaLGaM IDEA [4]
avg NEWUOA	1.7	7.9	5.4	9	6.1	62	<i>58e-3/6e3</i>	.	.	.	avg NEWUOA [31]
BayEDAacG	1.4	1.5	2.3	19	19	48	<i>59e-2/2e3</i>	.	.	.	BayEDAacG [10]
BFGS	5.4	11	14	30	110	<i>74e-2/2e3</i>	BFGS [30]
Cauchy EDA	2.6	2200	380	55	11	6.4	5	7	7.4	6.7	Cauchy EDA [24]
BIPOP-CMA-ES	1.6	2.4	2.2	6.5	1.9	1.1	1	1	1	1	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	22	6.6	13	17	38	83	140	<i>32e-3/1e4</i>	.	(1+1)-CMA-ES [2]
DASA	3.3	27	26	91	86	740	1800	4200	5900	5e3	DASA [19]
DEPSO	1.3	1	2.7	3.1	2.1	3.3	11	9.4	8.3	75e-4/2e3	DEPSO [12]
DIRECT	1.4	1.9	1	1	1.1	1.2	3.4	4.8	4.9	11	DIRECT [25]
EDA-PSO	1.3	1.3	2.4	5.4	7.1	9.1	11	12	13	15	EDA-PSO [6]
full NEWUOA	1.2	5	3	16	19	71	<i>58e-3/6e3</i>	.	.	.	full NEWUOA [31]
G3-PCX	1.9	1.1	2	10	21	41	48	72	99	85	G3-PCX [26]
simple GA	1.1	1.5	4.3	15	23	110	280	680	1200	<i>24e-4/1e5</i>	simple GA [22]
GLOBAL	1.3	1.2	2	3.1	2.2	4.8	7.6	<i>58e-3/1e3</i>	.	.	GLOBAL [23]
iAMaLGaM IDEA	1.2	1.8	1.4	12	2.9	1.8	2.3	2	2	1.8	iAMaLGaM IDEA [4]
LSfminbnd	2.1	3.6	1.3	2.1	7	33	<i>58e-3/4e3</i>	.	.	.	LSfminbnd [28]
LSstep	28	18	12	79	60	110	<i>24e-2/1e4</i>	.	.	.	LSstep [28]
MA-LS-Chain	1.7	1.5	1.6	3.2	2.5	3.2	4	3.9	5.8	7	MA-LS-Chain [21]
MCS (Neum)	1.4	3	1.3	2.8	1.7	8.4	140	350	<i>30e-4/3e4</i>	.	MCS (Neum) [18]
NELDER (Han)	1.2	1.3	2.1	44	18	20	38	47	40	34	NELDER (Han) [16]
NELDER (Doe)	1.3	1.3	1.2	3.1	2.4	4.3	5.8	8.7	25	21	NELDER (Doe) [5]
NEWUOA	1.3	13	5.6	12	14	62	<i>98e-3/6e3</i>	.	.	.	NEWUOA [31]
(1+1)-ES	1.5	2.4	63	230	620	1500	4900	1.4e4	<i>75e-4/1e6</i>	.	(1+1)-ES [1]
POEMS	100	72	28	120	29	28	23	31	45	42	POEMS [20]
PSO	1.3	1.3	1.7	3.4	2.8	3.2	3.5	5.6	6.5	7.2	PSO [7]
PSO_Bounds	1.4	1.5	1.5	5.3	6.7	8.8	10	12	17	23	PSO_Bounds [8]
Monte Carlo	1.1	1.2	2.2	21	270	1.1e4	<i>24e-3/1e6</i>	.	.	.	Monte Carlo [3]
Rosenbrock	26	54	61	56	200	<i>53e-2/5e3</i>	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.5	4.9	2.1	6.2	2.1	1.3	1.1	1	1.1	1.1	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.6	3.8	16	5.4	3.6	4.8	8.1	18	150	VNS (Garcia) [11]

Table 19: 02-D, running time excess ERT/ERT_{best} on f_{19} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
	0.5	0.5	0.5	0.5	13.2	108	114	30	126	138	
ALPS	1	1.1	5.5	5.5	17	12	22	30	41	54	ALPS [17]
AMaLGaM IDEA	1	1.1	6.3	40	6.2	18	18	17	17	16	AMaLGaM IDEA [4]
avg NEWUOA	1	1.3	8	110	13	22	21	20	19	18	avg NEWUOA [31]
BayEDA _c G	1	1.1	3.9	44	9.9	13	57	<i>35e-4/2e3</i>			BayEDA _c G [10]
BFGS	1	1.1	37	310	61	30	29	27	26	24	BFGS [30]
Cauchy EDA	1	1.1	16	110	51	170	860	1300	2800	<i>18e-4/5e4</i>	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	6	31	32	12	12	15	14	14	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	5.6	87	33	32	31	29	28	26	(1+1)-CMA-ES [2]
DASA	1	7.5	42	760	97	250	250	250	260	270	DASA [19]
DEPSO	1	1	4.4	59	17	18	35	36	69	67	DEPSO [12]
DIRECT	1	1	1	1	4.6	10	9.6	9.1	8.9	59	DIRECT [25]
EDA-PSO	1	1.1	5.2	37	13	17	30	57	62	72	EDA-PSO [6]
full NEWUOA	1	1.3	6.7	88	17	17	17	16	15	14	full NEWUOA [31]
G3-PCX	1	1	5.3	52	37	49	47	45	43	40	G3-PCX [26]
simple GA	1	1.2	4.5	51	20	21	110	360	640	4900	simple GA [22]
GLOBAL	1	1.3	4.3	50	9.4	11	10	10	9.6	8.8	GLOBAL [23]
iAMaLGaM IDEA	1	1.1	5.5	25	63	50	48	48	46	42	iAMaLGaM IDEA [4]
LSfminbd	1	1.1	9.4	49	10	29	70	120	310	<i>59e-5/5e3</i>	LSfminbd [28]
LSstep	1	1.9	140	440	27	63	140	580	<i>11e-4/1e4</i>		LSstep [28]
MA-LS-Chain	1	1.1	6.7	60	7.2	15	15	14	14	13	MA-LS-Chain [21]
MCS (Neum)	1	1	1	1	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1	1	3.1	380	64	32	30	29	27	25	NELDER (Han) [16]
NELDER (Doe)	1	1.1	4.6	52	10	8.1	7.8	7.4	7.1	6.5	NELDER (Doe) [5]
NEWUOA	1	1.5	6.2	130	16	27	26	25	24	22	NEWUOA [31]
(1+1)-ES	1	1.6	6.2	100	22	23	25	27	30	38	(1+1)-ES [1]
POEMS	1	130	340	550	57	210	200	200	190	190	POEMS [20]
PSO	1	1.1	5.3	34	9.1	4.7	6	8.7	9.9	16	PSO [7]
PSO.Bounds	1	1.5	5.1	40	7.8	11	20	36	47	71	PSO.Bounds [8]
Monte Carlo	1	1.2	4.5	64	16	36	110	310	720	3.2e4	Monte Carlo [3]
Rosenbrock	1	6.9	42	160	34	30	29	28	26	24	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1.5	4.3	29	6.8	19	20	19	19	18	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1.2	2.2	43	12	19	19	20	20	21	VNS (Garcia) [11]

Table 20: 02-D, running time excess ERT/ERT_{best} on f_{20} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

20 Schwefel $x^* \sin(x)$											
Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS	2.1	2.8	3.1	1.4	6.2	9.2	12	16	20	26	ALPS [17]
AMaLGaM IDEA	2.2	2.5	2.6	26	37	38	38	38	38	38	AMaLGaM IDEA [4]
avg NEWUOA	3	2.2	2.1	9.8	4	4	4	4	4	3.9	avg NEWUOA [31]
BayEDAacG	3.2	4	3.6	9.2	32	<i>25e-2/2e3</i>	BayEDAacG [10]
BFGS	2.5	2.2	2.1	6	2.7	2.7	2.7	2.7	2.7	2.6	BFGS [30]
Cauchy EDA	26	20	18	9.9	31	150	1300	2e3	2e3	1900	Cauchy EDA [24]
BIPOP-CMA-ES	2.9	2.8	2.7	1.3	9.9	10	11	11	11	11	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	2.2	2	2.1	7.5	8.5	8.6	8.6	8.6	8.6	8.6	(1+1)-CMA-ES [2]
DASA	59	52	49	81	44	45	45	45	45	45	DASA [19]
DEPSO	1.4	1	1	9.9	4.9	5.6	6.4	6.8	8	9.2	DEPSO [12]
DIRECT	5.7	5.9	6.1	1	2.9	3	3.1	3.3	3.7	3.9	DIRECT [25]
EDA-PSO	1.7	3.3	3.2	9	13	21	25	25	26	27	EDA-PSO [6]
full NEWUOA	2.9	2.1	1.8	18	8.3	8.3	8.3	8.3	8.2	8.1	full NEWUOA [31]
G3-PCX	2.9	2.8	2.9	38	7.8	7.8	8	8.1	8.1	8.2	G3-PCX [26]
simple GA	2.7	2.4	2.8	14	15	27	45	65	85	130	simple GA [22]
GLOBAL	1.8	1.9	2.4	11	4.5	4.5	4.5	4.5	4.5	4.5	GLOBAL [23]
iAMaLGaM IDEA	2.1	2.4	2.2	51	26	26	27	27	27	27	iAMaLGaM IDEA [4]
LSfminbd	6.5	6.7	6.6	150	<i>68e-2/1e4</i>	LSfminbd [28]
LSstep	94	210	180	120	25	27	30	37	40	50	LSstep [28]
MA-LS-Chain	1.5	1.9	2.4	4.2	1.8	2	2.1	2.2	2.3	2.4	MA-LS-Chain [21]
MCS (Neum)	2.9	6.2	5.7	2.2	1	1	1	1	1	1	MCS (Neum) [18]
NELDER (Han)	1.5	1.3	1.3	36	28	28	28	28	28	27	NELDER (Han) [16]
NELDER (Doe)	1.6	1.7	1.5	3.9	2.8	2.8	2.9	2.9	2.9	2.9	NELDER (Doe) [5]
NEWUOA	3	2.2	2.1	7	5.9	5.9	5.9	5.9	5.8	5.8	NEWUOA [31]
(1+1)-ES	4.1	3.7	3.3	13	9	9.1	9.2	9.2	9.2	9.2	(1+1)-ES [1]
POEMS	190	140	130	25	30	35	42	46	52	61	POEMS [20]
PSO	2.5	2.2	2.5	8.3	5	6.3	8.7	10	12	15	PSO [7]
PSO_Bounds	2.5	2.9	3.7	11	6	13	20	25	30	36	PSO_Bounds [8]
Monte Carlo	2.2	2.8	3.6	21	67	680	5800	8.2e4	<i>80e-5/1e6</i>	.	Monte Carlo [3]
Rosenbrock	5	4	4	6.8	4.1	4.2	4.2	4.2	4.2	4.2	Rosenbrock [27]
IPOP-SEP-CMA-ES	1.6	1.8	1.8	9.4	15	16	17	18	18	18	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	3.8	4.3	18	9.3	9.6	9.7	9.9	10	13	VNS (Garcia) [11]

Table 21: 02-D, running time excess ERT/ERT_{best} on f_{21} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.5	0.5	0.833	25.3	87.2	138	145	153	162	165	ERT_{best}/D
ALPS	1	1	1.2	2.2	1.8	2.6	4.9	6.4	7.8	12	12	ALPS [17]
AMaLGaM IDEA	1	1	1.3	28	17	11	11	10	10	10	10	AMaLGaM IDEA [4]
avg NEWUOA	1	1	6.1	6.5	4.6	2.9	2.8	2.7	2.7	2.6	2.7	avg NEWUOA [31]
BayEDAacG	1	1	1.7	1.6	9.3	1.4	3.9	57	86	85	85	BayEDAacG [10]
BFGS	1	1	2.6	4.8	3	2	1.9	1.8	1.7	1.7	1.8	BFGS [30]
Cauchy EDA	1	1	6	310	93	62	65	62	81	80	80	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1.4	11	10	8.2	9.7	9.3	8.9	8.9	8.9	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	1.2	12	9.6	6.1	5.9	5.6	5.3	5.3	5.3	(1+1)-CMA-ES [2]
DASA	1	1	1.3	150	140	88	84	80	77	76	76	DASA [19]
DEPSO	1	1	2.1	2.5	1.5	1.8	2.4	2.6	2.9	2.9	5.6	DEPSO [12]
DIRECT	1	1	1.3	1	1	1	1	2	2	2	2.3	DIRECT [25]
EDA-PSO	1	1	1	1.8	83	54	53	52	51	52	52	EDA-PSO [6]
full NEWUOA	1	1	2.2	3.6	3	1.9	1.8	1.7	1.7	1.7	1.7	full NEWUOA [31]
G3-PCX	1	1	1.4	2.7	2.9	1.9	1.9	1.8	1.8	1.8	1.8	G3-PCX [26]
simple GA	1	1	1.4	1	1.7	4.1	7.7	18	120	270	270	simple GA [22]
GLOBAL	1	1	1.5	1.1	1.1	1	1	1	1	1	1	GLOBAL [23]
iAMaLGaM IDEA	1	1	1.6	21	12	7.9	7.8	7.5	7.2	7.1	7.1	iAMaLGaM IDEA [4]
LSfminbd	1	1	2.1	39	20	26	46	60	73	170	170	LSfminbd [28]
LSstep	1	1	18	370	150	100	100	100	120	120	190	LSstep [28]
MA-LS-Chain	1	1	1.4	1.1	1.5	1.5	1.7	1.9	1.9	1.9	2	MA-LS-Chain [21]
MCS (Neum)	1	1	1.6	22	14	8.8	8.4	8	7.6	7.5	7.5	MCS (Neum) [18]
NELDER (Han)	1	1	1.8	19	20	13	12	12	11	11	11	NELDER (Han) [16]
NELDER (Doe)	1	1	1.4	2.6	2.6	1.7	1.6	1.5	1.5	1.5	1.5	NELDER (Doe) [5]
NEWUOA	1	1	3.5	3.9	4	2.5	2.4	2.3	2.2	2.3	2.3	NEWUOA [31]
(1+1)-ES	1	1	2.8	14	19	12	11	11	10	10	10	(1+1)-ES [1]
POEMS	1	1	1.30	93	890	560	540	520	490	490	490	POEMS [20]
PSO	1	1	1.2	1.4	83	53	51	48	46	47	47	PSO [7]
PSO_Bounds	1	1	1.5	33	300	190	180	170	170	170	170	PSO_Bounds [8]
Monte Carlo	1	1	2	1.8	1.2	3.5	8.8	28	42	640	640	Monte Carlo [3]
Rosenbrock	1	1	2.3	5.5	3.9	2.5	2.4	2.3	2.2	2.1	2.1	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1.3	9.6	6.4	6.3	8.5	8.7	8.6	9.2	9.2	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1.1	6.1	14	9.1	8.8	8.5	8.4	8.4	8.4	VNS (Garcia) [11]

21 Gallagher 101 peaks

Table 22: 02-D, running time excess ERT/ERT_{best} on f_{22} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

22 Gallagher 21 peaks											
Δf_{target}	$1e+03$	$1e+02$	$1e+01$	$1e+00$	$1e-01$	$1e-02$	$1e-03$	$1e-04$	$1e-05$	$1e-07$	Δf_{target}
ERT_{best}/D	0.5	0.5	2.53	13.4	83.9	109	125	142	144	153	ERT_{best}/D
ALPS	1	1	1.2	1.3	1	3	5.2	7.1	9.2	15	ALPS [17]
AMaLgAM IDEA	1	1	1.3	51	18	19	17	15	15	15	AMaLgAM IDEA [4]
avg NEWUOA	1	1	3	3.8	1.3	1.1	1.1	1.1	1.1	1.3	avg NEWUOA [31]
BayEDA _{cG}	1	1	1.3	3.3	7.6	11	34	59	200	<i>37e-4/2e3</i>	BayEDA _{cG} [10]
BFGS	1	1	5.4	5	1.5	1.2	1.1	1	1	1	BFGS [30]
Cauchy EDA	1	1	27	610	190	270	390	450	540	510	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1	7.3	11	8.7	10	9.2	9.1	8.7	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	14	26	7.2	5.7	5	4.5	4.4	4.3	(1+1)-CMA-ES [2]
DASA	1	1	11	80	22	21	22	28	40	63	DASA [19]
DEPSO	1	1	2.3	4.7	2.4	4	4.6	5	6.6	9.8	DEPSO [12]
DIRECT	1	1	1.5	2.1	1.3	1.3	1.4	2.2	4.8	5.1	DIRECT [25]
EDA-PSO	1	1	1.1	4	1.7	4.2	4.9	8.4	11	25	EDA-PSO [6]
full_NEWUOA	1	1	6.5	6.8	1.5	1.2	1.1	1.1	1.1	1.2	full_NEWUOA [31]
G3-PCX	1	1	2.1	2.2	1.1	1.1	1.1	1.3	1.4	1.6	G3-PCX [26]
simple GA	1	1	1.2	3	1.3	3.3	7.1	17	280	1900	simple GA [22]
GLOBAL	1	1	1.7	2.9	1.3	1.5	1.5	1.3	1.4	1.3	GLOBAL [23]
iAMaLgAM IDEA	1	1	1.5	14	9.9	8.9	8	7.2	7.1	7.3	iAMaLgAM IDEA [4]
LSfmnbnd	1	1	1.4	4.7	5.1	53	49	61	69	460	LSfmnbnd [28]
LSstep	1	1	1	80	140	140	150	280	970	920	LSstep [28]
MA-LS-Chain	1	1	1	2.8	1.6	1.9	2.2	2.3	2.4	2.4	MA-LS-Chain [21]
MCS (Neum)	1	1	2.4	40	7.4	6	5.3	4.7	4.8	5.2	MCS (Neum) [18]
NELDER (Han)	1	1	7.7	39	9.8	7.6	6.6	5.9	5.8	5.5	NELDER (Han) [16]
NELDER (Doe)	1	1	1.3	8.1	1.8	1.4	1.2	1.1	1.1	1.1	NELDER (Doe) [5]
NEWUOA	1	1	1.9	6.3	1.2	1	1	1	1	1	NEWUOA [31]
(1+1)-ES	1	1	1.6	46	11	9.8	9.4	9.4	10	12	(1+1)-ES [1]
POEMS	1	1	64	940	230	190	160	150	150	150	POEMS [20]
PSO	1	1	1.5	2.7	1	1.8	1.9	2.3	3.8	6.5	PSO [7]
PSO_Bounds	1	1	1.2	540	87	67	60	56	58	64	PSO_Bounds [8]
Monte Carlo	1	1	1.3	2.8	1.5	3.1	7.2	24	93	760	Monte Carlo [3]
Rosenbrock	1	1	12	17	4.5	3.5	3.1	2.7	2.7	2.6	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	1	7.7	4.4	4.1	3.9	3.6	3.8	3.8	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	2	1	2.8	3.8	4.8	4.7	5	5.3	VNS (Garcia) [11]

Table 23: 02-D, running time excess ERT/ERT_{best} on f_{23} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.5	0.5	3.9	96.5	117	131	150	157	174	190	ERT_{best}/D
ALPS	1	1	1.4	1.4	14	86	140	200	640	4100	2.8e4	ALPS [17]
AMaLGaM IDEA	1	1	1.3	7.5	7.5	10	9.8	9	8.9	8.4	8.1	AMaLGaM IDEA [4]
avg NEWUOA	1	1	4.2	6.7	25	25	100	260	<i>4.9e-3/6e3</i>	.	.	avg NEWUOA [31]
BayEDAacG	1	1	2	11	<i>56e-2/2e3</i>	BayEDAacG [10]
BFGS	1	1	4.8	4.9	28	28	120	480	460	410	<i>73e-3/5e3</i>	BFGS [30]
Cauchy EDA	1	1	1.8	16	860	860	<i>14e-2/5e4</i>	Cauchy EDA [24]
BIPOP-CMA-ES	1	1	1.8	8.3	15	14	13	13	13	12	12	BIPOP-CMA-ES [15]
(1+1)-CMA-ES	1	1	2.1	5.1	8.4	8.4	8.6	7.7	7.6	6.9	6.6	(1+1)-CMA-ES [2]
DASA	1	1	5.7	17	170	170	1800	8600	9600	8700	7900	DASA [19]
DEPSO	1	1	2.2	24	<i>96e-2/2e3</i>	DEPSO [12]
DIRECT	1	1	1.5	4.2	290	290	270	240	230	210	200	DIRECT [25]
EDA-PSO	1	1	2.3	18	1400	1400	<i>13e-2/1e5</i>	EDA-PSO [6]
full NEWUOA	1	1	6	1.5	24	46	81	81	79	71	65	full NEWUOA [31]
G3-PCX	1	1	1.9	1.6	6.1	6.1	6	5.8	5.8	5.5	7.4	G3-PCX [26]
simple GA	1	1	1.4	6.6	330	330	840	3300	<i>41e-4/1e5</i>	.	.	simple GA [22]
GLOBAL	1	1	1	2.6	97	97	<i>21e-2/2e3</i>	GLOBAL [23]
iAMaLGaM IDEA	1	1	1.3	5.3	5.5	5.5	5.3	4.9	5	4.7	4.6	iAMaLGaM IDEA [4]
LSfminbnd	1	1	1.3	2.1	30	30	120	200	190	<i>25e-3/7e3</i>	.	LSfminbnd [28]
LSstep	1	1	2.6	18	1300	1300	<i>24e-2/1e4</i>	LSstep [28]
MA-LS-Chain	1	1	1.8	5.5	7.4	7.4	7.1	6.6	6.7	6.4	7	MA-LS-Chain [21]
MCS (Neum)	1	1	3.4	2.8	6.3	6.3	23	210	500	1e3	1900	MCS (Neum) [18]
NELDER (Han)	1	1	1.3	1.6	2.2	2.2	2.2	2	1.9	1.8	1.7	NELDER (Han) [16]
NELDER (Doe)	1	1	4.7	1	1	1	1	1	1	1	1	NELDER (Doe) [5]
NEWUOA	1	1	7.8	3.2	32	32	89	130	170	500	460	NEWUOA [31]
(1+1)-ES	1	1	2.6	3.7	19	19	55	240	1e3	2100	6700	(1+1)-ES [1]
POEMS	1	1	1.4	28	190	190	180	180	190	180	190	POEMS [20]
PSO	1	1	1.3	9	42	42	59	73	79	88	95	PSO [7]
PSO_Bounds	1	1	1.7	9.4	260	260	460	500	690	660	860	PSO_Bounds [8]
Monte Carlo	1	1	1.5	8	1900	1900	<i>46e-3/1e6</i>	Monte Carlo [3]
Rosenbrock	1	1	1.9	2.2	9.9	9.9	15	17	23	29	66e-7/5e3	Rosenbrock [27]
IPOP-SEP-CMA-ES	1	1	2.6	8.1	14	14	16	14	14	13	12	IPOP-SEP-CMA-ES [29]
VNS (Garcia)	1	1	1.8	8.3	38	38	67	65	62	56	52	VNS (Garcia) [11]

Table 24: 02-D, running time excess ERT/ERT_{best} on f_{24} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS [17]		0.5	1	1	6.5	4	2.8	2.9	2.9	3	3.2	ALPS [17]
AMaLGaM IDEA [4]		1	1	1.2	35	11	6.7	6.7	6.6	6.6	6.7	AMaLGaM IDEA [4]
avg NEWUOA [31]		1	1	3.3	1.9	1.4	6.2	6	5.9	5.9	5.9	avg NEWUOA [31]
BayEDAeG [10]		1	1	1.9	68	<i>22e-1/2e3</i>						BayEDAeG [10]
BFGS [30]		1	1	3.4	5.1	2.9	<i>42e-2/3e3</i>					BFGS [30]
Cauchy EDA [24]		1	1	3.9	33	170	<i>49e-2/5e4</i>					Cauchy EDA [24]
BIPOP-CMA-ES [15]		1	1	4.6	19	17	13	22	22	22	22	BIPOP-CMA-ES [15]
(1+1)-CMA-ES [2]		1	1	2.7	6.1	4.8	2.9	2.8	2.7	2.7	3.6	(1+1)-CMA-ES [2]
DASA [19]		1	1	10	140	110	61	59	58	58	58	DASA [19]
DEPSO [12]		1	1	3.3	67	<i>24e-1/2e3</i>						DEPSO [12]
DIRECT [25]		1	1	1.9	79	8.7	5	4.9	4.7	4.7	4.8	DIRECT [25]
EDA-PSO [6]		1	1	1.6	100	12	9	9	8.8	8.8	8.9	EDA-PSO [6]
full NEWUOA [31]		1	1	2.8	1	1	1.1	1	1	1	1	full NEWUOA [31]
G3-PCX [26]		1	1	1.2	37	20	<i>10e-2/5e4</i>					G3-PCX [26]
simple GA [22]		1	1	1.6	67	<i>79e-2/1e5</i>						simple GA [22]
GLOBAL [23]		1	1	2.7	3.3	7	<i>51e-2/2e3</i>					GLOBAL [23]
iAMaLGaM IDEA [4]		1	1	1.4	28	9.1	5.4	5.3	5.2	5.3	5.3	iAMaLGaM IDEA [4]
LSfminbd [28]		1	1	2.8	8.3	<i>37e-2/8e3</i>						LSfminbd [28]
LStep [28]		3	3	4.8	29	33	12	12	<i>11e-1/1e4</i>			LStep [28]
MA-LS-Chain [21]		1	1	2.5	31	34	<i>11e-1/1e4</i>					MA-LS-Chain [21]
MCS (Neum) [18]		1	1	2.5	5.7	1.6	2.7	2.7	2.6	2.6	2.6	MCS (Neum) [18]
NELDER (Han) [16]		1	1	16	7.4	5	6.6	6.4	6.2	6.2	6.2	NELDER (Han) [16]
NELDER (Doe) [5]		1	1	1.5	1.9	1.5	3.2	3.1	3	3	3	NELDER (Doe) [5]
NEWUOA [31]		1	1	3.1	2.8	1.9	2	1.9	1.9	1.9	1.9	NEWUOA [31]
(1+1)-ES [1]		1	1	8	12	11	21	20	19	19	19	(1+1)-ES [1]
POEMS [20]		1	1	28	1500	170	<i>20e-1/1e5</i>					POEMS [20]
PSO [7]		1	1	2.4	470	49	18	17	17	17	17	PSO [7]
PSO_Bounds [8]		1	1	1.3	1500	150	57	55	54	54	54	PSO_Bounds [8]
Monte Carlo [3]		1	1	2.5	14	150	570	<i>49e-3/1e6</i>				Monte Carlo [3]
Rosenbrock [27]		1	1	19	35	15	11	11	11	11	11	Rosenbrock [27]
IPOP-SEP-CMA-ES [29]		1	1	1.7	7.2	3.9	3.7	3.7	3.6	3.6	3.6	IPOP-SEP-CMA-ES [29]
VNS (Garcia) [11]		1	1	1.2	5.3	1.7	1	1	1.1	1.9	4.7	VNS (Garcia) [11]

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