

Comparison tables: BBOB 2009 noisy testbed in 10-D

The BBOBies

November 20, 2009

Abstract

This document provides tabular results of the workshop for Black-Box Optimization Benchmarking at GECCO 2009, see <http://coco.gforge.inria.fr/doku.php?id=bbob-2009>. More than 30 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 40. A description of the used objective functions can be found in [13, 8]. The experimental set-up is described in [12].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm. Consequently, the best (smallest) value is 1 and the value 1 appears in each column at least once. See [12] for details on how ERT is obtained. All numbers are computed with no more than two digits of precision.

Table 1: 10-D, running time excess ERT/ERT_{best} on f_{101} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS		0.1	0.1	2.6	4	18	18.5	19.4	20	21	22.6	ALPS [15]
AMaLGaM IDEA		1	4.5	70	130	51	72	89	110	120	160	AMaLGaM IDEA [4]
avg NEWUOA		1	6.4	17	30	11	15	19	22	24	28	avg NEWUOA [23]
BayEDAeG		1	20	2.9	3.4	1	1.2	1.2	1.3	1.3	1.4	BayEDAeG [9]
BFGS		1	7.1	53	81	45	86	110	130	130	140	BFGS [22]
BIPOP-CMA-ES		1	840	<i>36e+0/3e3</i>	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		1	13	5.4	7.8	2.5	3.3	4	4.6	5.1	6.1	(1+1)-CMA-ES [2]
DASA		1	6.9	3	4.2	1.4	1.8	2.2	2.6	2.9	3.5	DASA [18]
DEPSO		1	180	30	34	10	13	14	16	18	21	DEPSO [11]
EDA-PSO		1	5.8	16	27	11	16	21	26	31	41	EDA-PSO [5]
full NEWUOA		1	6.1	25	380	180	280	360	440	510	640	full NEWUOA [23]
GLOBAL		1	45	4	4.1	1	1	1	1	1	1	GLOBAL [20]
iAMaLGaM IDEA		1	3.9	13	11	3	3.3	3.7	3.9	4.1	5	iAMaLGaM IDEA [4]
MA-LS-Chain		1	5.7	8.1	13	5.1	6.9	8.3	9.9	11	14	MA-LS-Chain [19]
MCS (Neum)		1	5.5	11	19	8.3	11	13	15	16	18	MCS (Neum) [16]
NEWUOA		1	1	1	1	20	870	<i>28e-3/4e3</i>	.	.	.	NEWUOA [23]
(1+1)-ES		1	15	2.1	3	1.1	1.6	1.9	2.1	2.3	2.9	(1+1)-ES [1]
PSO		1	15	3.1	3.7	1.2	1.5	1.8	2.2	2.4	2.9	PSO [6]
PSO_Bounds		1	5.3	8.9	25	12	18	25	31	35	45	PSO_Bounds [7]
Monte Carlo		1	5.5	13	140	96	150	220	250	280	480	Monte Carlo [3]
IPOP-SEP-CMA-ES		1	3.1	2200	<i>36e-1/1e6</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT		1	11	5.1	6.5	2.2	2.8	3.3	3.9	4.3	5.1	SNOBFIT [17]
VNS (Garcia)		1	10	4.6	3.9	1	1.1	1.3	1.4	1.6	1.9	VNS (Garcia) [10]
		1	12	1.2	11	3.3	4	4.5	5.3	5.7	6.7	

Table 2: 10-D, running time excess ERT/ERT_{best} on f_{102} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS	1	0.1	3.7	69	130	52	64	78	91	100	120	ALPS [15]
AMaLGaM IDEA	1	6.8	17	17	30	11	13	15	17	17	20	AMaLGaM IDEA [4]
avg NEWUOA	1	31	2.9	3.2	3.2	1	1.1	1.2	1.3	1.4	1.7	avg NEWUOA [23]
BayEDAeG	1	5.8	51	51	73	27	37	41	52	61	63	BayEDAeG [9]
BFGS	1	640	<i>34e+0/3e3</i>	BFGS [22]
BIPOP-CMA-ES	1	8.5	4.9	7.1	7.1	2.6	2.9	3.2	3.8	4	4.5	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	11	3.1	3.1	4	1.3	1.6	1.9	2.2	2.3	2.6	(1+1)-CMA-ES [2]
DASA	1	190	31	34	34	12	13	15	17	18	22	DASA [18]
DEPSO	1	5.7	18	26	26	11	14	18	22	24	29	DEPSO [11]
EDA-PSO	1	4.8	45	390	390	200	250	310	370	400	470	EDA-PSO [5]
full NEWUOA	1	40	4.3	4.2	4.2	1.1	1	1	1	1	1	full NEWUOA [23]
GLOBAL	1	4.9	13	10	10	3.3	3.8	4.3	4.9	7.2	26	GLOBAL [20]
iAMaLGaM IDEA	1	4.4	7.2	13	13	5.1	6.1	7.3	8.3	8.9	10	iAMaLGaM IDEA [4]
MA-LS-Chain	1	5.1	11	11	21	9.2	11	12	13	13	14	MA-LS-Chain [19]
MCS (Neum)	1	1	1	1	1	460	<i>13e-2/4e3</i>	MCS (Neum) [16]
NEWUOA	1	18	3.5	7.9	7.9	9	30	48	81	150	550	NEWUOA [23]
(1+1)-ES	1	15	3	4	4	1.3	1.5	1.7	2.1	2.7	4.5	(1+1)-ES [1]
PSO	1	4.7	9.1	1800	1800	420	360	340	320	300	270	PSO [6]
PSO_Bounds	1	7.1	13	98	98	99	140	190	210	220	440	PSO_Bounds [7]
Monte Carlo	1	6.2	3100	<i>33e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	9	4.1	6.1	6.1	2.1	2.3	2.7	3	3.2	3.6	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	6.3	6.1	7.6	7.6	2	2.1	2.1	2.6	3.6	5.3	SNOBFIT [17]
VNS (Garcia)	1	12	12	11	11	3.4	3.7	4.1	4.5	4.6	5	VNS (Garcia) [10]

Table 3: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{103} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$
103 Sphere moderate Cauchy												
ALPS		1	4.9	67	110	75	96	2.5e4	<i>10e-4/5e5</i>	36.3	36.4	ALPS [15]
AMaLGaM IDEA		1	4.4	17	27	16	19	30	100	230	380	AMaLGaM IDEA [4]
avg NEWUOA		1	31	3	2.9	1.8	6.8	25	100	1500	<i>39e-6/8e3</i>	avg NEWUOA [23]
BayEDA-cG		1	5.6	44	66	62	80	49	53	58	67	BayEDA-cG [9]
BFGS		1	230	12	6.5	2.9	2.5	1	1	1	1	BFGS [22]
BIPOP-CMA-ES		1	9.3	5.5	6.1	3.6	4.2	2.2	2.6	3.1	4.2	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		1	9.7	3.4	3.6	2.5	6	23	92	710	<i>18e-6/1e4</i>	(1+1)-CMA-ES [2]
DASA		1	57	21	22	39	1100	2.4e5	<i>16e-4/6e5</i>	.	.	DASA [18]
DEPSO		1	1.4	17	21	17	72	150	<i>25e-4/2e3</i>	.	.	DEPSO [11]
EDA-PSO		1	4.6	37	350	280	1500	<i>71e-4/1e5</i>	.	.	.	EDA-PSO [5]
full NEWUOA		1	45	3.8	3.4	1.4	1.9	1.4	2.8	7.5	20	full NEWUOA [23]
GLOBAL		1	6.3	25	17	7.1	6.9	2.7	2.7	2.7	2.7	GLOBAL [20]
iAMaLGaM IDEA		1	4.4	7.5	12	7.4	9.3	7.4	39	200	1e3	iAMaLGaM IDEA [4]
MA-LS-Chain		1	7.3	10	18	12	15	8.6	11	17	30	MA-LS-Chain [19]
MCS (Neum)		1	1	1	1	1.4	14	13	25	50	170	MCS (Neum) [16]
NEWUOA		1	15	2.3	3.6	5.2	29	95	240	1100	<i>15e-5/6e3</i>	NEWUOA [23]
(1+1)-ES		1	12	3.4	3.6	1.9	7.8	46	600	7800	4.1e5	(1+1)-ES [1]
PSO		1	5.5	9.1	1500	580	2300	1.9e4	<i>56e-4/1e5</i>	.	.	PSO [6]
PSO-Bounds		1	3.4	11	110	1500	4.6e4	<i>40e-3/1e5</i>	.	.	.	PSO-Bounds [7]
Monte Carlo		1	5.3	1600	<i>36e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES		1	10	4.8	5.6	3	3.6	1.9	2.3	2.7	3.5	IPOP-SEP-CMA-ES [21]
SNBOFIT		1	3.8	3.9	2.5	1	1	1.4	2.7	5.5	7.7	SNBOFIT [17]
VNS (Garcia)		1	12	11	9.4	4.7	5.3	2.6	3.1	3.8	5	VNS (Garcia) [10]

Table 4: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{104} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	$\text{ERT}_{\text{best}}/D$	4.81	23.4	45.3	999	1660	1840	1940	2020	2080	2200	$\text{ERT}_{\text{best}}/D$
ALPS		49	26	32	14	14	16	21	33	51	110	ALPS [15]
AMaLGaM IDEA		10	4.2	5.8	1.4	1	1	1	1	1	1	AMaLGaM IDEA [4]
avg NEWUOA		1	1	1	7.1	22	<i>67e-2/8e3</i>	avg NEWUOA [23]
BayEDAacG		24	13	47	<i>97e-1/2e3</i>	BayEDAacG [9]
BFGS		<i>12e+3/1e3</i>	BFGS [22]
BIPOP-CMA-ES		3.5	3	3.6	1.8	1.3	1.3	1.3	1.2	1.2	1.2	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		2.2	2.1	2.8	5.5	19	80	<i>46e-2/1e4</i>	.	.	.	(1+1)-CMA-ES [2]
DASA		17	11	15	2.1	7.2	23	78	180	1900	<i>28e-6/9e5</i>	DASA [18]
DEPSO		11	5.8	11	30	<i>70e-1/2e3</i>	DEPSO [11]
EDA-PSO		72	74	97	18	17	22	28	34	40	<i>67e-8/1e5</i>	EDA-PSO [5]
full NEWUOA		2	1.6	1.6	1.6	2.6	2.5	6.4	6.1	11	14	full NEWUOA [23]
GLOBAL		6.9	1.9	1.8	1	1.4	2.8	<i>39e-1/300</i>	.	.	.	GLOBAL [20]
iAMaLGaM IDEA		5.7	2.6	2.9	2.5	1.6	1.5	1.5	1.5	1.5	1.4	iAMaLGaM IDEA [4]
MA-LS-Chain		7.5	3.9	5.7	34	21	20	19	18	18	17	MA-LS-Chain [19]
MCS (Neum)		3.8	36	<i>61e+0/4e3</i>	MCS (Neum) [16]
NEWUOA		1	2.1	7.2	4.6	47	<i>55e-2/5e3</i>	NEWUOA [23]
(1+1)-ES		2.5	2	1.8	5.2	9.9	32	66	390	1200	<i>21e-6/1e6</i>	(1+1)-ES [1]
PSO		7.8	5.8	9.4	400	430	<i>59e-1/1e5</i>	PSO [6]
PSO_Bounds		21	26	71	660	400	770	730	700	<i>63e-1/1e5</i>	.	PSO_Bounds [7]
Monte Carlo		6700	<i>26e+1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES		3.1	1.3	1.3	5.7	3.6	3.3	3.2	3	3	2.8	IPOP-SEP-CMA-ES [21]
SNOBFIT		6.1	5.4	18	7.3	<i>13e+0/500</i>	SNOBFIT [17]
VNS (Garcia)		7.9	3.3	22	54	51	46	45	44	42	40	VNS (Garcia) [10]

Table 5: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{105} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

105 Rosenbrock moderate unif												
	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	$\text{ERT}_{\text{best}}/D$											$\text{ERT}_{\text{best}}/D$
ALPS		74	17	16	10	5.3	6.9	12	14	19	42	ALPS [15]
AMaLGaM IDEA		13	2.6	2.3	3.9	1.2	1.2	1.2	1.2	1.2	1.2	AMaLGaM IDEA [4]
avg NEWUOA		1.9	1.7	2.5	5.1	3.7	16	<i>88e-2/8e3</i>				avg NEWUOA [23]
BayEDAeG		42	8.8	18	<i>83e-1/2e3</i>							BayEDAeG [9]
BFGS		<i>20e+3/1e3</i>										BFGS [22]
BIPOP-CMA-ES		4.8	1.1	1	2.9	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		3.7	2.4	1.8	4.5	4.4	20	<i>55e-2/1e4</i>				(1+1)-CMA-ES [2]
DASA		33	11	18	3.1	2.6	17	54	250	1400	<i>24e-5/8e5</i>	DASA [18]
DEPSO		18	3.5	3.4	<i>76e-1/2e3</i>							DEPSO [11]
EDA-PSO		120	54	45	<i>52e-1/1e5</i>							EDA-PSO [5]
full NEWUOA		2.9	1.3	1.2	4.4	6.4	<i>32e-2/1e4</i>					full NEWUOA [23]
GLOBAL		11	1.5	1.6	1	<i>70e-1/300</i>						GLOBAL [20]
iAMaLGaM IDEA		9	1.8	1.2	9.5	3	2.9	2.9	2.8	2.8	2.8	iAMaLGaM IDEA [4]
MA-LS-Chain		12	3	5.2	160	<i>52e-1/5e4</i>						MA-LS-Chain [19]
MCS (Neum)		7	25	<i>70e+0/4e3</i>								MCS (Neum) [16]
NEWUOA		1	1.2	11	10	<i>52e-1/5e3</i>						NEWUOA [23]
(1+1)-ES		3.6	1	1.7	8.7	10	45	170	300	1800	<i>71e-5/1e6</i>	(1+1)-ES [1]
PSO		15	220	80	300	<i>65e-1/1e5</i>						PSO [6]
PSO_Bounds		27	16	98	320	200	<i>75e-1/1e5</i>					PSO_Bounds [7]
Monte Carlo		7500	<i>32e+1/1e6</i>									Monte Carlo [3]
IPOP-SEP-CMA-ES		5.4	1.4	1	32	20	<i>72e-1/1e4</i>					IPOP-SEP-CMA-ES [21]
SNOBFIT		14	4.6	11	<i>16e+0/500</i>							SNOBFIT [17]
VNS (Garcia)		11	29	18	310	300	650	730	800	1200	4900	VNS (Garcia) [10]

Table 6: 10-D, running time excess ERT/ERT_{best} on f_{106} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

106 Rosenbrock moderate Cauchy											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT _{best} /D	3.44	12.8	28.8	342	771	819	850	874	897	937	ERT _{best} /D
ALPS	72	47	47	140	140	1500	<i>12e-3/5e5</i>				ALPS [15]
AMaLGaM IDEA	13	7.6	8.6	35	45	86	210	340	430	620	AMaLGaM IDEA [4]
avg NEWUOA	1.5	1	1.3	5.4	19	160	<i>13e-2/9e3</i>				avg NEWUOA [23]
BayEDAeG	36	25	100	<i>11e+0/2e3</i>							BayEDAeG [9]
BFGS	71	210	<i>44e+0/4e3</i>								BFGS [22]
BIPOP-CMA-ES	5.3	3.8	2.9	1.7	1	1.1	1.2	1.2	1.2	1.2	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	3.5	3.1	3.5	24	40	170	<i>51e-2/1e4</i>				(1+1)-CMA-ES [2]
DASA	21	13	11	6.6	29	4e3	<i>16e-3/1e6</i>				DASA [18]
DEPSO	16	10	17	85	<i>67e-1/2e3</i>						DEPSO [11]
EDA-PSO	140	140	160	<i>43e-1/1e5</i>							EDA-PSO [5]
full NEWUOA	2.6	1.5	1	1	8.1	89	<i>48e-3/1e4</i>				full NEWUOA [23]
GLOBAL	9.8	3.3	2.6	5.4	<i>42e-1/300</i>						GLOBAL [20]
iAMaLGaM IDEA	7.1	4.5	4.4	21	17	46	90	210	340	810	iAMaLGaM IDEA [4]
MA-LS-Chain	11	7.3	8.3	5.7	4.9	6.5	8.2	11	14	32	MA-LS-Chain [19]
MCS (Neum)	5.3	24	<i>61e+0/4e3</i>								MCS (Neum) [16]
NEWUOA	1	1.3	1.6	7.5	14	26	<i>11e-2/7e3</i>				NEWUOA [23]
(1+1)-ES	2.7	2.3	2.4	18	61	370	1.7e4	<i>57e-4/1e6</i>			(1+1)-ES [1]
PSO	9.8	11	13	1900	1800	<i>62e-1/1e5</i>					PSO [6]
PSO_Bounds	27	37	320	<i>65e-1/1e5</i>							PSO_Bounds [7]
Monte Carlo	1e4	<i>32e+1/1e6</i>									Monte Carlo [3]
IPOP-SEP-CMA-ES	4.8	2.3	2.1	2	1	1	1	1	1	1	IPOP-SEP-CMA-ES [21]
SNOBFFT	8.8	9.3	14	<i>70e-1/500</i>							SNOBFFT [17]
VNS (Garcia)	11	5.3	4.6	11	4.8	4.6	4.5	4.4	4.3	4.2	VNS (Garcia) [10]

Table 7: 10-D, running time excess ERT/ERT_{best} on f_{107} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS	1	0.1	5.1	3.2	6	8	11	14	19	26	86	ALPS [15]
AMaLGaM IDEA	1	3.5	5.8	230	13	15	14	12	10	9.7	9.4	AMaLGaM IDEA [4]
avg NEWUOA	1	32	230	<i>15e+0/7e3</i>								avg NEWUOA [23]
BayEDAeG	1	4.2	3	3	4	4.5	29	<i>32e-3/2e3</i>				BayEDAeG [9]
BFGS	1	600	<i>33e+0/1e3</i>									BFGS [22]
BIPOP-CMA-ES	1	17	1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	180	230	<i>11e+0/1e4</i>								(1+1)-CMA-ES [2]
DASA	1	3e3	1.1e4									DASA [18]
DEPSO	1	4.1	2.7	<i>11e+0/4e5</i>		<i>97e-2/2e3</i>						DEPSO [11]
EDA-PSO	1	3.5	9.2	44	44	30	37	40	32	28	24	EDA-PSO [5]
full NEWUOA	1	130	230	<i>13e+0/1e4</i>								full NEWUOA [23]
GLOBAL	1	5.1	77	<i>17e+0/500</i>								GLOBAL [20]
iAMaLGaM IDEA	1	7	3.9	26	26	42	53	45	35	30	27	iAMaLGaM IDEA [4]
MA-LS-Chain	1	6.1	2.2	6.1	6.1	6.9	7.8	7.7	6.9	6.3	5.8	MA-LS-Chain [19]
MCS (Neum)	1	1	28	<i>87e-1/4e3</i>								MCS (Neum) [16]
NEWUOA	1	15	130	<i>23e+0/4e3</i>								NEWUOA [23]
(1+1)-ES	1	200	240	6.3e4		<i>19e-1/1e6</i>						(1+1)-ES [1]
PSO	1	4.9	460	260	260	270	240	260	210	310	1e3	PSO [6]
PSO_Bounds	1	4.4	84	240	240	560	1300	<i>59e-2/1e5</i>				PSO_Bounds [7]
Monte Carlo	1	4.2	38	<i>30e-1/1e6</i>								Monte Carlo [3]
IPOP-SEP-CMA-ES	1	17	12	16	16	16	14	12	9.5	8.2	13	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	7.9	11	<i>13e+0/500</i>								SNOBFIT [17]
VNS (Garcia)	1	12	28	27	27	36	42	65	110	200	960	VNS (Garcia) [10]

Table 8: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{108} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

108 Sphere unif											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
$\text{ERT}_{\text{best}}/D$	0.1	0.1	1e3	3140	4760	7750	10900	13600	17900	30800	$\text{ERT}_{\text{best}}/D$
ALPS [15]	1	2.6	1.2	460	<i>12e-1/5e5</i>	77	85	320	28e-4/1e6	1	ALPS [15]
AMaLGaM IDEA [4]	1	5.2	19	33	77	85	320	28e-4/1e6	1	1	AMaLGaM IDEA [4]
avg NEWUOA [23]	1	1400	<i>27e+0/7e3</i>	33	77	85	320	28e-4/1e6	1	1	avg NEWUOA [23]
BayEDAeG [9]	1	5.7	<i>21e+0/2e3</i>	33	77	85	320	28e-4/1e6	1	1	BayEDAeG [9]
BFGS [22]	1	240	<i>40e+0/800</i>	33	77	85	320	28e-4/1e6	1	1	BFGS [22]
BIPOP-CMA-ES [14]	1	180	30	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES [2]	1	380	30	<i>13e+0/1e4</i>	1	1	1	1	1	1	(1+1)-CMA-ES [2]
DASA [18]	1	4600	640	<i>10e+0/4e5</i>	1	1	1	1	1	1	DASA [18]
DEPSO [11]	1	28	29	<i>18e+0/2e3</i>	1	1	1	1	1	1	DEPSO [11]
EDA-PSO [5]	1	4.4	94	450	<i>99e-1/1e5</i>	1	1	1	1	1	EDA-PSO [5]
full NEWUOA [23]	1	3300	140	<i>29e+0/1e4</i>	1	1	1	1	1	1	full NEWUOA [23]
GLOBAL [20]	1	3.9	<i>19e+0/500</i>	1	1	1	1	1	1	1	GLOBAL [20]
iAMaLGaM IDEA [4]	1	5.9	18	61	97	160	1300	1100	62e-4/1e6	1	iAMaLGaM IDEA [4]
MA-LS-Chain [19]	1	5.5	1.1	240	<i>24e-1/5e4</i>	1	1	1	1	1	MA-LS-Chain [19]
MCS (Neum) [16]	1	1	27	<i>18e+0/4e3</i>	1	1	1	1	1	1	MCS (Neum) [16]
NEWUOA [23]	1	590	<i>28e+0/4e3</i>	1	1	1	1	1	1	1	NEWUOA [23]
(1+1)-ES [1]	1	270	95	<i>54e-1/1e6</i>	1	1	1	1	1	1	(1+1)-ES [1]
PSO [6]	1	2.7	190	<i>17e+0/1e5</i>	1	1	1	1	1	1	PSO [6]
PSO_Bounds [7]	1	4.7	120	<i>11e+0/1e5</i>	1	1	1	1	1	1	PSO_Bounds [7]
Monte Carlo [3]	1	6	4.1	<i>34e-1/1e6</i>	1	1	1	1	1	1	Monte Carlo [3]
IPOP-SEP-CMA-ES [21]	1	47	45	<i>15e+0/1e4</i>	1	1	1	1	1	1	IPOP-SEP-CMA-ES [21]
SNOBFIT [17]	1	5.1	<i>21e+0/500</i>	1	1	1	1	1	1	1	SNOBFIT [17]
VNS (Garcia) [10]	1	12	48	4300	<i>13e-1/5e6</i>	1	1	1	1	1	VNS (Garcia) [10]

Table 9: 10-D, running time excess ERT/ERT_{best} on f_{109} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

109 Sphere Cauchy											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT _{best} /D	0.1	0.1	2.79	28.6	49.9	82.4	116	146	179	242	ERT _{best} /D
ALPS	1	2.3	68	57	1.4e5	<i>20e-2/5e5</i>	ALPS [15]
AMaLGA M IDEA	1	4.9	16	4.1	12	43	53	58	91	160	AMaLGA M IDEA [4]
avg NEWUOA	1	20	11	38	670	<i>31e-2/7e3</i>	avg NEWUOA [23]
BayEDA cG	1	2.9	43	11	11	17	21	19	17	<i>35e-7/2e3</i>	BayEDA cG [9]
BFGS	1	440	270	49	28	17	12	9.7	9.9	7.3	BFGS [22]
BIPOP-CMA-ES	1	13	4.7	1.1	1.1	1.1	1.1	1.1	1.2	1.2	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	13	8.9	53	1400	<i>30e-2/1e4</i>	(1+1)-CMA-ES [2]
DASA	1	150	1600	<i>26e-1/5e5</i>	DASA [18]
DEPSO	1	6.1	17	7.5	46	<i>87e-3/2e3</i>	DEPSO [11]
EDA-PSO	1	4.1	39	1.1e4	<i>13e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	1	33	27	24	2900	<i>34e-2/1e4</i>	full NEWUOA [23]
GLOBAL	1	7.3	13	6.3	<i>35e-2/300</i>	GLOBAL [20]
iAMaLGA M IDEA	1	5.1	8.3	2.1	10	54	130	190	270	450	iAMaLGA M IDEA [4]
MA-LS-Chaim	1	5.3	10	4.5	9.5	180	3200	<i>28e-4/5e4</i>	MA-LS-Chaim [19]
MCS (Neum)	1	1	1	19	73	200	230	180	320	240	MCS (Neum) [16]
NEWUOA	1	16	12	77	<i>57e-2/4e3</i>	NEWUOA [23]
(1+1)-ES	1	12	5.9	7.7	1900	<i>42e-3/1e6</i>	(1+1)-ES [1]
PSO	1	5.1	160	4100	<i>10e-1/1e5</i>	PSO [6]
PSO_Bounds	1	5	2600	<i>31e-1/1e5</i>	PSO_Bounds [7]
Monte Carlo	1	5.9	2400	<i>29e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	9	4.8	1	1	1	1	1	1	1	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	4.8	6.5	18	140	<i>85e-2/500</i>	SNOBFIT [17]
VNS (Garcia)	1	12	11	1.6	1.5	1.4	1.3	1.3	1.3	1.3	VNS (Garcia) [10]

Table 10: 10-D, running time excess ERT/ERT_{best} on f_{110} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

110 Rosenbrock Gauss											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT_{best}/D	35.2	141	1120	3.32e6	7.03e6	1.64e7	nan	nan	nan	nan	ERT_{best}/D
ALPS	8.2	6.1	15	1	1	<i>27e-1/5e5</i>	ALPS [15]
AMaLGaM IDEA	1.6	1.1	6.5	<i>70e-1/1e6</i>	AMaLGaM IDEA [4]
avg NEWUOA	620	<i>16e+2/7e3</i>	avg NEWUOA [23]
BayEDAeG	4.8	3.9	4.3	<i>11e+0/2e3</i>	BayEDAeG [9]
BFGS	<i>19e+3/700</i>	BFGS [22]
BIPOP-CMA-ES	1.3	1	1	4.9	2.3	1	<i>56e-1/1e6</i>	.	.	.	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	220	<i>69e+1/1e4</i>	(1+1)-CMA-ES [2]
DASA	1.3e4	<i>79e+1/4e5</i>	DASA [18]
DEPSO	2.8	5.7	<i>28e+0/2e3</i>	DEPSO [11]
EDA-PSO	15	12	83	<i>87e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	1300	<i>27e+2/1e4</i>	full NEWUOA [23]
GLOBAL	1	GLOBAL [20]
iAMaLGaM IDEA	1	4.3	20	<i>61e-1/1e6</i>	iAMaLGaM IDEA [4]
MA-LS-Chain	3.2	3	7.4	<i>75e-1/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	29	<i>45e+1/4e3</i>	MCS (Neum) [16]
NEWUOA	100	<i>83e+1/4e3</i>	NEWUOA [23]
(1+1)-ES	570	<i>14e+1/1e6</i>	(1+1)-ES [1]
PSO	3	17	610	<i>14e+0/1e5</i>	PSO [6]
PSO_Bounds	210	370	370	<i>27e+0/1e5</i>	PSO_Bounds [7]
Monte Carlo	1600	<i>26e+1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1.1	7.6	13	<i>95e-1/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	12	<i>43e+1/500</i>	SNOBFIT [17]
VNS (Garcia)	1.9	26	39	3.6	16e-1/6e6	VNS (Garcia) [10]

Table 11: 10-D, running time excess ERT/ERT_{best} on f_{111} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS	1.8	384	1950	8290	nan	nan	nan	nan	nan	nan	nan	ALPS [15]
AMaLGaM IDEA	6	3.8	3.7	16	<i>80e-1/1e6</i>	AMaLGaM IDEA [4]
avg NEWUOA	260	<i>10e+3/7e3</i>	<i>39e+1/2e3</i>	avg NEWUOA [23]
BayEDA-cG	1.5	15	15	<i>39e+1/2e3</i>	BayEDA-cG [9]
BFGS	<i>14e+3/500</i>	BFGS [22]
BIPOP-CMA-ES	1.1	1.1	1	1	<i>70e-1/1e6</i>	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	<i>25e+2/1e4</i>	(1+1)-CMA-ES [2]
DASA	<i>19e+2/4e5</i>	DASA [18]
DEPSO	24	<i>21e+2/2e3</i>	<i>17e+1/1e5</i>	DEPSO [11]
EDA-PSO	45	120	<i>17e+1/1e5</i>	EDA-PSO [5]
full NEWUOA	<i>94e+2/1e4</i>	full NEWUOA [23]
GLOBAL	<i>56e+2/400</i>	GLOBAL [20]
iAMaLGaM IDEA	4.6	11	11	35	<i>86e-1/1e6</i>	iAMaLGaM IDEA [4]
MA-LS-Chain	1	5.6	<i>42e+0/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	33	<i>20e+2/4e3</i>	<i>76e+1/1e5</i>	MCS (Neum) [16]
NEWUOA	<i>74e+2/4e3</i>	NEWUOA [23]
(1+1)-ES	340	<i>54e+1/1e6</i>	<i>76e+1/1e5</i>	(1+1)-ES [1]
PSO	250	730	<i>76e+1/1e5</i>	PSO [6]
PSO_Bounds	180	<i>85e+1/1e5</i>	<i>30e+1/1e6</i>	PSO_Bounds [7]
Monte Carlo	59	<i>30e+1/1e6</i>	<i>11e+1/1e4</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	13	9.2	<i>11e+1/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	<i>28e+2/500</i>	SNOBFIT [17]
VNS (Garcia)	34	130	<i>23e+0/6e6</i>	VNS (Garcia) [10]

Table 12: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{112} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

112 Rosenbrock Cauchy											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
$\text{ERT}_{\text{best}}/D$	3.71	14.9	88.4	1160	1610	1740	1820	1890	1950	2040	$\text{ERT}_{\text{best}}/D$
ALPS	56	37	30	1500	<i>17e-1/5e5</i>	ALPS [15]
AMaLGaM IDEA	11	5.9	6.6	300	250	240	230	230	220	210	AMaLGaM IDEA [4]
avg NEWUOA	1.5	2.2	10	98	71	<i>42e-1/8e3</i>	avg NEWUOA [23]
BayEDAacG	31	20	23	<i>85e-1/2e3</i>	BayEDAacG [9]
BFGS	2900	<i>24e+2/2e3</i>	BFGS [22]
BIPOP-CMA-ES	4.6	5	1.2	1	1	1.1	1.1	1.1	1.1	1.1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	3.6	4.5	8.1	<i>48e-1/1e4</i>	(1+1)-CMA-ES [2]
DASA	23	61	320	<i>31e-1/6e5</i>	DASA [18]
DEPSO	15	8.4	15	<i>88e-1/2e3</i>	DEPSO [11]
EDA-PSO	120	120	300	<i>93e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	2.7	3	4.6	<i>32e-1/1e4</i>	full NEWUOA [23]
GLOBAL	8.9	3.7	2.5	<i>78e-1/300</i>	GLOBAL [20]
iAMaLGaM IDEA	6.4	4.1	2.2	390	340	320	310	330	320	310	iAMaLGaM IDEA [4]
MA-LS-Chain	9.7	6.1	2.9	280	<i>56e-1/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	4.3	37	<i>66e+0/4e3</i>	MCS (Neum) [16]
NEWUOA	1	1	27	<i>81e-1/5e3</i>	NEWUOA [23]
(1+1)-ES	3.7	2.7	7.4	760	<i>70e-2/1e6</i>	(1+1)-ES [1]
PSO	11	530	1400	<i>10e+0/1e5</i>	PSO [6]
PSO_Bounds	31	51	1.6e4	<i>16e+0/1e5</i>	PSO_Bounds [7]
Monte Carlo	8100	<i>33e+1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	4.4	2.6	1	1.2	1	1	1	1	1	1	IPOP-SEP-CMA-ES [21]
SNOBFIT	7.8	8.9	40	<i>21e+0/500</i>	SNOBFIT [17]
VNS (Garcia)	10	4.3	1.2	4.9	3.7	3.6	3.4	3.3	3.3	3.2	VNS (Garcia) [10]

Table 13: 10-D, running time excess ERT/ERT_{best} on f_{113} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D											ERT_{best}/D
ALPS	2.6	3.3	2.4	2760	7.3	43	72	72	72	72	83	ALPS [15]
AMaLGaM IDEA	1.7	1	1.8	2.9	1.2	1.4	1.6	1.6	1.6	1.6	1.6	AMaLGaM IDEA [4]
avg NEWUOA	4.9	59	<i>40e+0/7e3</i>									avg NEWUOA [23]
BayEDAeG	1.9	3	2.3	<i>40e-1/2e3</i>								BayEDAeG [9]
BFGS	110	360	<i>14e+1/1e3</i>									BFGS [22]
BIPOP-CMA-ES	4	1	1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	5.8	55	320	<i>32e+0/1e4</i>								(1+1)-CMA-ES [2]
DASA	760	560	1.4e4	<i>25e+0/4e5</i>								DASA [18]
DEPSO	1.7	3.1	6.3	<i>10e+0/2e3</i>								DEPSO [11]
EDA-PSO	2.6	24	58	73	<i>21e-1/1e5</i>							EDA-PSO [5]
full NEWUOA	9.8	100	<i>50e+0/1e4</i>									full NEWUOA [23]
GLOBAL	1.9	3.5	<i>34e+0/600</i>									GLOBAL [20]
iAMaLGaM IDEA	1.8	1.1	3.1	4.7	3.4	4.1	4.1	4.1	4.1	4.1	3.9	iAMaLGaM IDEA [4]
MA-LS-Chain	1	12	130	7	16	67	67	67	67	67	65	MA-LS-Chain [19]
MCS (Neum)	1.9	2	2.2	<i>23e+0/4e3</i>								MCS (Neum) [16]
NEWUOA	32	47	<i>39e+0/4e3</i>									NEWUOA [23]
(1+1)-ES	22	37	1200	<i>87e-1/1e6</i>								(1+1)-ES [1]
PSO	1.8	2.8	150	510	<i>70e-1/1e5</i>							PSO [6]
PSO_Bounds	1.8	2.1	1500	<i>23e+0/1e5</i>								PSO_Bounds [7]
Monte Carlo	2.5	3.4	4200	<i>10e+0/1e6</i>								Monte Carlo [3]
IPOP-SEP-CMA-ES	3.2	16	7.4	17	<i>23e-1/1e4</i>							IPOP-SEP-CMA-ES [21]
SNOBFIT	2.2	4.2	<i>29e+0/500</i>									SNOBFIT [17]
VNS (Garcia)	1.4	2.3	1.4	64	360	7100	7100	7100	7100	7100	6900	VNS (Garcia) [10]

Table 14: 10-D, running time excess ERT/ERT_{best} on f_{114} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$1e+03$	$1e+02$	$1e+01$	$1e+00$	$1e-01$	$1e-02$	$1e-03$	$1e-04$	$1e-05$	$1e-07$	Δf_{target} ERT_{best}/D
ALPS [15]	2.7	2.3	9.7	<i>47e-1/5e5</i>	30	120	120	120	120	180	ALPS [15]
AMaLGaM IDEA [4]	2.6	2.2	5.7	11	30	120	120	120	120	180	AMaLGaM IDEA [4]
avg NEWUOA [23]	100	240	<i>82e+0/7e3</i>	avg NEWUOA [23]
BayEDAacG [9]	1.7	18	<i>66e+0/2e3</i>	BayEDAacG [9]
BFGS [22]	49	83	<i>15e+1/800</i>	BFGS [22]
BIPOP-CMA-ES [14]	4.1	6.1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES [2]	110	68	<i>40e+0/1e4</i>	(1+1)-CMA-ES [2]
DASA [18]	96	370	1800	<i>28e+0/4e5</i>	DASA [18]
DEPSO [11]	2.3	38	<i>79e+0/2e3</i>	DEPSO [11]
EDA-PSO [5]	2	820	180	<i>55e+0/1e5</i>	EDA-PSO [5]
full NEWUOA [23]	180	140	<i>77e+0/1e4</i>	full NEWUOA [23]
GLOBAL [20]	2.3	2.3	<i>68e+0/400</i>	GLOBAL [20]
iAMaLGaM IDEA [4]	1.8	31	12	20	29	180	180	180	180	170	iAMaLGaM IDEA [4]
MA-LS-Chain [19]	2.7	1.4	10	<i>67e-1/5e4</i>	MA-LS-Chain [19]
MCS (Neum) [16]	1	20	<i>39e+0/4e3</i>	MCS (Neum) [16]
NEWUOA [23]	32	110	<i>88e+0/4e3</i>	NEWUOA [23]
(1+1)-ES [1]	110	61	2e3	<i>16e+0/1e6</i>	(1+1)-ES [1]
PSO [6]	1.7	510	<i>70e+0/1e5</i>	PSO [6]
PSO_Bounds [7]	2.1	500	<i>49e+0/1e5</i>	PSO_Bounds [7]
Monte Carlo [3]	2.5	1	520	<i>11e+0/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES [21]	2.1	120	<i>39e+0/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT [17]	2.4	2.8	<i>51e+0/500</i>	SNOBFIT [17]
VNS (Garcia) [10]	1.4	170	190	<i>42e-1/5e6</i>	VNS (Garcia) [10]

Table 15: 10-D, running time excess ERT/ERT_{best} on f_{115} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT_{best}/D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT_{best}/D
ALPS		0.1	3.81	39.8	290	859	1230	1260	1260	1260	1280	ALPS [15]
AMaLGaM IDEA	2	2.1	14	11	490	<i>61e-2/5e5</i>	4.3	4.3	4.3	4.3	4.2	AMaLGaM IDEA [4]
avg NEWUOA	7	2.6	4.3	1.8	3.9	3.6	4.3	4.3	4.3	4.3	4.2	avg NEWUOA [23]
BayEDAeG	1.9	150	9.6	11	<i>40e-1/2e3</i>	<i>24e-1/7e3</i>	BayEDAeG [9]
BFGS	150	1400	1400	<i>11e+1/2e3</i>	BFGS [22]
BIPOP-CMA-ES	4.5	2	2	1	4.5	6.9	5.5	5.4	5.4	5.4	5.6	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	4	7.7	12	12	<i>21e-1/1e4</i>	(1+1)-CMA-ES [2]
DASA	35	140	8300	8300	<i>77e-1/5e5</i>	DASA [18]
DEPSO	1.9	6.5	7	7	16	<i>12e-1/2e3</i>	DEPSO [11]
EDA-PSO	2	5.2	27	27	4800	<i>19e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	16	2	6.1	3.7	140	<i>13e-1/1e4</i>	full NEWUOA [23]
GLOBAL	2.4	1.9	4.1	4.1	<i>56e-1/500</i>	GLOBAL [20]
iAMaLGaM IDEA	1.9	2.8	2.8	1.4	1.5	4.4	13	14	14	14	14	iAMaLGaM IDEA [4]
MA-LS-Chain	1.9	3.8	3.7	3.7	42	260	<i>59e-2/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	1	1	1	300	<i>12e+0/4e3</i>	MCS (Neum) [16]
NEWUOA	11	2.4	2.4	19	<i>41e-1/4e3</i>	NEWUOA [23]
(1+1)-ES	7.3	1.6	1.6	17	2900	<i>88e-2/1e6</i>	(1+1)-ES [1]
PSO	1.7	2.6	2.6	640	<i>32e-1/1e5</i>	PSO [6]
PSO_Bounds	1.9	3	1400	1400	<i>64e-1/1e5</i>	PSO_Bounds [7]
Monte Carlo	1.9	13	6.6e4	6.6e4	<i>11e+0/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	3.2	2	2	1	1	1	1	1	1	1	1	IPOP-SEP-CMA-ES [21]
SNOBFIT	2.3	4.8	89	89	<i>16e+0/500</i>	SNOBFIT [17]
VNS (Garcia)	1.4	6.5	1.9	1.9	13	38	56	64	64	64	65	VNS (Garcia) [10]

Table 16: 10-D, running time excess ERT/ERT_{best} on f_{116} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δ ftarget
ERT _{best} /D	105	1650	7140	10600	10900	11300	11600	11900	12300	16700	ERT _{best} /D
ALPS	4.8	5	15	160	<i>15e-1/5e5</i>	ALPS [15]
AMaLGaM IDEA	1	1	1	1	1	1	1	1	1	1	AMaLGaM IDEA [4]
avg NEWUOA	970	<i>35e+2/7e3</i>	avg NEWUOA [23]
BayEDAeG	16	18	<i>68e+1/2e3</i>	BayEDAeG [9]
BFGS	<i>10e+3/800</i>	BFGS [22]
BIPOP-CMA-ES	5.1	2.2	1.3	1.3	1.6	1.7	1.7	1.7	1.7	1.3	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	130	<i>86e+1/1e4</i>	(1+1)-CMA-ES [2]
DASA	6200	<i>10e+2/4e5</i>	DASA [18]
DEPSO	13	18	<i>63e+1/2e3</i>	DEPSO [11]
EDA-PSO	150	390	200	<i>46e+1/1e5</i>	EDA-PSO [5]
full NEWUOA	1400	<i>25e+2/1e4</i>	full NEWUOA [23]
GLOBAL	<i>31e+2/500</i>	GLOBAL [20]
iAMaLGaM IDEA	1.7	2.5	2.8	2.7	3	3.4	3.5	3.5	3.7	2.8	iAMaLGaM IDEA [4]
MA-LS-Chain	5.2	15	33	<i>30e+0/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	45	<i>99e+1/4e3</i>	MCS (Neum) [16]
NEWUOA	<i>28e+2/4e3</i>	NEWUOA [23]
(1+1)-ES	330	<i>28e+1/1e6</i>	(1+1)-ES [1]
PSO	530	890	<i>59e+1/1e5</i>	PSO [6]
PSO_Bounds	240	850	<i>46e+1/1e5</i>	PSO_Bounds [7]
Monte Carlo	530	<i>40e+1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	46	16	<i>17e+1/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFFT	9.3	<i>18e+2/500</i>	SNOBFFT [17]
VNS (Garcia)	87	54	1400	<i>12e+0/5e6</i>	VNS (Garcia) [10]

Table 17: 10-D, running time excess ERT/ERT_{best} on f_{117} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT_{best}/D	2240	10100	22800	39900	48900	62600	65400	68700	71700	79400	ERT_{best}/D
ALPS	1.2	160	<i>12e+1/5e5</i>	6.5	13	30	100	<i>31e-3/1e6</i>	.	.	ALPS [15]
AMaLGaM IDEA	2.3	4.2	7	AMaLGaM IDEA [4]
avg NEWUOA	<i>46e+2/7e3</i>	avg NEWUOA [23]
BayEDA-cG	<i>28e+2/2e3</i>	BayEDA-cG [9]
BFGS	<i>14e+3/500</i>	BFGS [22]
BIPOP-CMA-ES	1	1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	65	<i>25e+2/1e4</i>	(1+1)-CMA-ES [2]
DASA	1400	<i>15e+2/4e5</i>	DASA [18]
DEPSO	<i>39e+2/2e3</i>	DEPSO [11]
EDA-PSO	53	<i>97e+1/1e5</i>	EDA-PSO [5]
full NEWUOA	64	<i>62e+2/1e4</i>	full NEWUOA [23]
GLOBAL	<i>38e+2/400</i>	GLOBAL [20]
iAMaLGaM IDEA	4	11	9.5	14	24	51	110	<i>33e-3/1e6</i>	.	.	iAMaLGaM IDEA [4]
MA-LS-Chain	1.1	<i>36e+1/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	5.5	<i>20e+2/4e3</i>	MCS (Neum) [16]
NEWUOA	27	<i>51e+2/4e3</i>	NEWUOA [23]
(1+1)-ES	96	<i>61e+1/1e6</i>	(1+1)-ES [1]
PSO	130	<i>18e+2/1e5</i>	PSO [6]
PSO_Bounds	180	<i>19e+2/1e5</i>	PSO_Bounds [7]
Monte Carlo	13	<i>35e+1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	21	<i>15e+2/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	<i>33e+2/500</i>	SNOBFIT [17]
VNS (Garcia)	28	1600	<i>16e+1/5e6</i>	VNS (Garcia) [10]

Table 18: 10-D, running time excess ERT/ERT_{best} on f_{118} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D											ERT_{best}/D
ALPS		34	40	260	2.2e4	30e-1/5e5						ALPS [15]
AMaLGaM IDEA		4.8	3.6	1.3	2.9	4.4	9.6	12	12	20	34	AMaLGaM IDEA [4]
avg NEWUOA		1	3.2	17	37e-1/9e3							avg NEWUOA [23]
BayEDAeG		98	59e+1/2e3									BayEDAeG [9]
BFGS		71e+2/2e3										BFGS [22]
BIPOP-CMA-ES		6.2	5.6	3.2	2.2	2.2	2.1	2	2	1.9	1.8	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		2.7	18	350	13e+0/1e4							(1+1)-CMA-ES [2]
DASA		110	4900	58e+0/7e5								DASA [18]
DEPSO		14	61	72e+0/2e3								DEPSO [11]
EDA-PSO		52	72	29e+0/1e5								EDA-PSO [5]
full NEWUOA		1	1	14	430	48e-1/1e4						full NEWUOA [23]
GLOBAL		3.8	5.3	50	16e+0/1e3							GLOBAL [20]
iAMaLGaM IDEA		3.7	2.8	1	2.2	5.1	18	30	54	59	140	iAMaLGaM IDEA [4]
MA-LS-Chain		6.7	12	16	130	780	64e-2/5e4					MA-LS-Chain [19]
MCS (Neum)		140	65e+1/4e3									MCS (Neum) [16]
NEWUOA		1.2	3.9	57	99e-1/5e3							NEWUOA [23]
(1+1)-ES		4.9	150	5e4	16e+0/1e6							(1+1)-ES [1]
PSO		6.7	2300	1e4	54e+0/1e5							PSO [6]
PSO_Bounds		18	1700	63e+0/1e5								PSO_Bounds [7]
Monte Carlo		2200	34e+1/1e6									Monte Carlo [3]
IPOP-SEP-CMA-ES		5.6	7.8	3.4	2.1	1.8	1.7	1.5	1.5	1.5	1.4	IPOP-SEP-CMA-ES [21]
SNOBFIT		16	40e+1/500									SNOBFIT [17]
VNS (Garcia)		7.1	4.3	1.7	1	1	1	1	1	1	1	VNS (Garcia) [10]

Table 19: 10-D, running time excess ERT/ERT_{best} on f_{119} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.1	0.1	12.8	312	497	1120	3650	17900	30100	4e4	ERT_{best}/D
ALPS	ALPS [15]	1	2.9	3.4	4.1	8	11	44	<i>43e-5/5e5</i>	.	.	ALPS [15]
AMaLGaM IDEA	AMaLGaM IDEA [4]	1	2.7	2.1	8.5	14	8.3	3.9	1.3	1.2	1.1	AMaLGaM IDEA [4]
avg NEWUOA	avg NEWUOA [23]	1	25	200	<i>65e-1/7e3</i>	avg NEWUOA [23]
BayEDAacG	BayEDAacG [9]	1	2.5	6.6	2.6	4.1	<i>67e-3/2e3</i>	BayEDAacG [9]
BFGS	BFGS [22]	1.7	270	<i>13e+0/2e3</i>	BFGS [22]
BIPOP-CMA-ES	BIPOP-CMA-ES [14]	1	7.5	87	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	(1+1)-CMA-ES [2]	1	66	87	<i>31e-1/1e4</i>	(1+1)-CMA-ES [2]
DASA	DASA [18]	1	750	1100	<i>33e-1/4e5</i>	DASA [18]
DEPSO	DEPSO [11]	1.1	2.5	5.9	6.6	<i>80e-2/2e3</i>	DEPSO [11]
EDA-PSO	EDA-PSO [5]	1	2.7	4.6	83	110	83	180	<i>64e-4/1e5</i>	.	.	EDA-PSO [5]
full NEWUOA	full NEWUOA [23]	1	120	160	<i>55e-1/1e4</i>	full NEWUOA [23]
GLOBAL	GLOBAL [20]	1	3.4	8.7	<i>54e-1/600</i>	GLOBAL [20]
iAMaLGaM IDEA	iAMaLGaM IDEA [4]	1	3.1	1.4	10	38	24	13	3.5	2.4	2.2	iAMaLGaM IDEA [4]
MA-LS-Chain	MA-LS-Chain [19]	1	4	1.7	3.2	8.8	9.3	9.1	<i>49e-5/5e4</i>	.	.	MA-LS-Chain [19]
MCS (Neum)	MCS (Neum) [16]	1	1	18	<i>56e-1/4e3</i>	MCS (Neum) [16]
NEWUOA	NEWUOA [23]	1	11	120	<i>60e-1/4e3</i>	NEWUOA [23]
(1+1)-ES	(1+1)-ES [1]	1.5	170	44	<i>13e-1/1e6</i>	(1+1)-ES [1]
PSO	PSO [6]	1	3.3	1.4	4.6e4	330	380	<i>38e-2/1e5</i>	.	.	.	PSO [6]
PSO_Bounds	PSO_Bounds [7]	1.1	3.1	560	890	2800	<i>28e-1/1e5</i>	PSO_Bounds [7]
Monte Carlo	Monte Carlo [3]	1	3.1	7.5	4.7e4	<i>14e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	IPOP-SEP-CMA-ES [21]	1	7.1	34	11	13	7.1	20	<i>54e-4/1e4</i>	.	.	IPOP-SEP-CMA-ES [21]
SNOBFIT	SNOBFIT [17]	1	4.3	7.6	<i>52e-1/500</i>	SNOBFIT [17]
VNS (Garcia)	VNS (Garcia) [10]	1	3	2.6	18	41	180	2900	<i>10e-4/7e6</i>	.	.	VNS (Garcia) [10]

Table 20: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{120} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
	$\text{ERT}_{\text{best}}/D$	0.1	0.1	47.1	3990	7460	15700	43900	93000	1.27e5	2.5e5	$\text{ERT}_{\text{best}}/D$
ALPS	1	2.8	1.7	48	<i>62e-2/5e5</i>	ALPS [15]
AMaLGaM IDEA	1	1.9	6.4	16	39	<i>32e-3/1e6</i>	AMaLGaM IDEA [4]
avg NEWUOA	1	440	160	<i>97e-1/7e3</i>	avg NEWUOA [23]
BayEDA cG	1	2.8	1.3	<i>77e-1/2e3</i>	BayEDA cG [9]
BFGS	1	110	260	<i>15e+0/800</i>	BFGS [22]
BIPOP-CMA-ES	1	17	4.1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	220	64	<i>63e-1/1e4</i>	(1+1)-CMA-ES [2]
DASA	1	43	460	<i>46e-1/4e5</i>	DASA [18]
DEPSO	1	2.5	21	<i>63e-1/2e3</i>	DEPSO [11]
EDA-PSO	1	2.8	330	160	<i>47e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	1	440	310	<i>99e-1/1e4</i>	full NEWUOA [23]
GLOBAL	1	2.3	2.3	<i>79e-1/500</i>	GLOBAL [20]
iAMaLGaM IDEA	1	2.8	15	29	98	<i>47e-3/1e6</i>	iAMaLGaM IDEA [4]
MA-LS-Cham	1	5.1	1	18	<i>10e-1/5e4</i>	MA-LS-Cham [19]
MCS (Neum)	1	1	59	<i>81e-1/4e3</i>	MCS (Neum) [16]
NEWUOA	1	180	46	<i>11e+0/4e3</i>	NEWUOA [23]
(1+1)-ES	1	220	330	3700	<i>23e-1/1e6</i>	(1+1)-ES [1]
PSO	1	3.2	330	350	<i>48e-1/1e5</i>	PSO [6]
PSO_Bounds	1	2.6	770	<i>61e-1/1e5</i>	PSO_Bounds [7]
Monte Carlo	1	2.7	2	<i>15e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	2100	98	<i>52e-1/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	3.1	4.1	<i>69e-1/500</i>	SNOBFIT [17]
VNS (Garcia)	1	3	97	380	<i>63e-2/6e6</i>	VNS (Garcia) [10]

Table 21: 10-D, running time excess ERT/ERT_{best} on f_{121} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.1	0.1	7.24	31.7	63.1	1.48	368	694	999	1820	ERT_{best}/D
ALPS		1.1	3.3	9.6	81	<i>25e-2/5e5</i>						ALPS [15]
AMaLGaM IDEA		1	2.1	3.2	11	30	44	32	39	46	43	AMaLGaM IDEA [4]
avg NEWUOA		1	15	2.1	150	1700	<i>76e-2/7e3</i>					avg NEWUOA [23]
BayEDAeG		1	1.7	8.6	22	30	64	<i>41e-3/2e3</i>				BayEDAeG [9]
BFGS		1	400	570	<i>10e+0/2e3</i>							BFGS [22]
BIPOP-CMA-ES		1	5.4	1.1	1	1.1	1.1	1.1	1.4	1.9	2.1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		1	4.7	4	41	<i>49e-2/1e4</i>						(1+1)-CMA-ES [2]
DASA		1	45	580	<i>26e-1/5e5</i>							DASA [18]
DEPSO		1	2.2	4.6	8.8	140	<i>17e-2/2e3</i>					DEPSO [11]
EDA-PSO		1	2.9	2.3	9400	<i>14e-1/1e5</i>						EDA-PSO [5]
full NEWUOA		1	32	10	140	<i>55e-2/1e4</i>						full NEWUOA [23]
GLOBAL		1	1.9	3.8	18	<i>11e-1/300</i>						GLOBAL [20]
iAMaLGaM IDEA		1	2.9	1.6	3.4	21	72	94	87	130	120	iAMaLGaM IDEA [4]
MA-LS-Chain		1	2.7	2.5	4.8	43	<i>28e-3/5e4</i>					MA-LS-Chain [19]
MCS (Neum)		1	1	7.1	<i>22e-1/4e3</i>							MCS (Neum) [16]
NEWUOA		1	7.9	3.4	220	<i>11e-1/4e3</i>						NEWUOA [23]
(1+1)-ES		1	11	3.3	54	2.8e4	<i>10e-2/1e6</i>					(1+1)-ES [1]
PSO		1	2.9	1.7	7400	<i>13e-1/1e5</i>						PSO [6]
PSO_Bounds		1	2.9	4.9	<i>20e-1/1e5</i>							PSO_Bounds [7]
Monte Carlo		1	3	9.6	<i>15e-1/1e6</i>							Monte Carlo [3]
IPOP-SEP-CMA-ES		1	4.1	1	1	1	1	1.2	1.1	1.1	1	IPOP-SEP-CMA-ES [21]
SNOBFIT		1	3.5	4.4	<i>26e-1/500</i>							SNOBFIT [17]
VNS (Garcia)		1	3	3.5	1.6	1.4	1.1	1	1	1	1	VNS (Garcia) [10]

Table 22: 10-D, running time excess ERT/ERT_{best} on f_{122} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.1	0.1	5.53	1160	3320	9790	14100	17600	43900	81700	ERT_{best}/D
ALPS	1	1.3	1.9	1.7	4.2	10	<i>6.2</i>	5	4.2	2.3	5.4	ALPS [15]
AMaLGaM IDEA	1	1.3	1.7	28	<i>42e-1/7e3</i>							AMaLGaM IDEA [4]
avg NEWUOA	1	3.7	2.4	1.4	<i>85e-2/2e3</i>							avg NEWUOA [23]
BayEDA-cG	1	1.2	1.4	1.4	<i>82e-1/2e3</i>							BayEDA-cG [9]
BFGS	1	11	1.7	1.7	1	1	1	1	1	1	1	BFGS [22]
BIPOP-CMA-ES	1	1	1.5	24	<i>40e-1/1e4</i>							BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	1	1	1	1	1	1	1	1	1	1	(1+1)-CMA-ES [2]
DASA	1	1	1	350	<i>38e-1/4e5</i>							DASA [18]
DEPSO	1	1.1	1.1	3.8	<i>27e-1/2e3</i>							DEPSO [11]
EDA-PSO	1	1.1	1.1	3.4	200	<i>16e-1/1e5</i>						EDA-PSO [5]
full NEWUOA	1	10	65	49e-1/1e4								full NEWUOA [23]
GLOBAL	1	1.1	1.1	2.4	<i>50e-1/600</i>							GLOBAL [20]
iAMaLGaM IDEA	1	1.1	1.1	1	11	27	11	8.6	7.7	3.4	7	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1.3	1.2	17	<i>56e-2/5e4</i>							MA-LS-Chain [19]
MCS (Neum)	1	1	3.3	<i>37e-1/4e3</i>								MCS (Neum) [16]
NEWUOA	1	2.5	45	<i>47e-1/4e3</i>								NEWUOA [23]
(1+1)-ES	1	1	20	<i>19e-1/1e6</i>								(1+1)-ES [1]
PSO	1	1.1	1.7	610	<i>25e-1/1e5</i>							PSO [6]
PSO-Bounds	1	1	4.1	580	<i>24e-1/1e5</i>							PSO-Bounds [7]
Monte Carlo	1	1.2	2.8	<i>20e-1/1e6</i>								Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1.1	39	18	<i>14e-1/1e4</i>							IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1	4.2	<i>49e-1/500</i>								SNOBFIT [17]
VNS (Garcia)	1	1	3.7	150	2.9e4	<i>24e-2/7e6</i>						VNS (Garcia) [10]

Table 23: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{123} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$\Delta\text{ftarget}$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$
	$\text{ERT}_{\text{best}}/D$	0.1	0.1	3.99	9440	38900	66500	1.29e5	1.99e5	3.33e5	1.03e6	$\text{ERT}_{\text{best}}/D$
ALPS	1	1.1	2.4	<i>15e-1/5e5</i>	ALPS [15]
AMaLGaM IDEA	1	1.9	3	34	<i>68e-2/1e6</i>	AMaLGaM IDEA [4]
avg NEWUOA	1	1.3	180	<i>68e-1/7e3</i>	avg NEWUOA [23]
BayEDA-cG	1	1.1	9.3	<i>57e-1/2e3</i>	BayEDA-cG [9]
BFGS	1	11	150	<i>87e-1/900</i>	BFGS [22]
BIPOP-CMA-ES	1	2.2	18	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	1.2	140	<i>48e-1/1e4</i>	(1+1)-CMA-ES [2]
DASA	1	2.7	290	<i>37e-1/4e5</i>	DASA [18]
DEPSO	1	1.2	64	<i>50e-1/2e3</i>	DEPSO [11]
EDA-PSO	1	1.3	3.7	<i>48e-1/1e5</i>	EDA-PSO [5]
full NEWUOA	1	91	350	<i>60e-1/1e4</i>	full NEWUOA [23]
GLOBAL	1	1	5	<i>53e-1/400</i>	GLOBAL [20]
iAMaLGaM IDEA	1	1.3	5.9	79	<i>85e-2/1e6</i>	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1.3	1	<i>19e-1/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	1	1	37	<i>47e-1/4e3</i>	MCS (Neum) [16]
NEWUOA	1	31	190	<i>64e-1/4e3</i>	NEWUOA [23]
(1+1)-ES	1	17	76	<i>25e-1/1e6</i>	(1+1)-ES [1]
PSO	1	1.3	2.8	<i>43e-1/1e5</i>	PSO [6]
PSO-Bounds	1	1.1	6.1	<i>56e-1/1e5</i>	PSO-Bounds [7]
Monte Carlo	1	1.1	3.1	<i>20e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1.6	160	<i>44e-1/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1.1	5.4	<i>53e-1/500</i>	SNOBFIT [17]
VNS (Garcia)	1	1	350	<i>15e-1/6e6</i>	VNS (Garcia) [10]

Table 24: 10-D, running time excess ERT/ERT_{best} on f_{124} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

124 Schaffer F7 Cauchy											
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
ERT_{best}/D	0.1	0.1	3.73	61.4	1050	3430	5290	7380	13700	33100	ERT_{best}/D
ALPS	1	1.2	2.8	7200	<i>99e-2/5e5</i>						ALPS [15]
AMaLGaM IDEA	1	1.3	2.5	6.7	4.9	4.6	7.6	10	7.9	7.4	AMaLGaM IDEA [4]
avg NEWUOA	1	3.5	12	<i>24e-1/7e3</i>							avg NEWUOA [23]
BayEDAeG	1	1.3	2.8	10	2.7	8.7	<i>74e-3/2e3</i>				BayEDAeG [9]
BFGS	1	6.9	460	<i>89e-1/2e3</i>							BFGS [22]
BIPOP-CMA-ES	1	2.1	1.8	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	3.3	9	2400	<i>19e-1/1e4</i>						(1+1)-CMA-ES [2]
DASA	1	1	210	<i>31e-1/5e5</i>							DASA [18]
DEPSO	1	1.4	3.6	50	<i>97e-2/2e3</i>						DEPSO [11]
EDA-PSO	1.1	1.2	2.3	<i>31e-1/1e5</i>							EDA-PSO [5]
full NEWUOA	1	1	9.2	<i>23e-1/1e4</i>							full NEWUOA [23]
GLOBAL	1	1.3	3.2	<i>33e-1/500</i>							GLOBAL [20]
iAMaLGaM IDEA	1	1.1	1.5	12	16	17	26	27	17	8.6	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1.3	1.7	130	<i>62e-2/5e4</i>						MA-LS-Chain [19]
MCS (Neum)	1	1	1	<i>25e-1/4e3</i>							MCS (Neum) [16]
NEWUOA	1	5	11	<i>34e-1/4e3</i>							NEWUOA [23]
(1+1)-ES	1	9.8	6.8	1.2e4	<i>93e-2/1e6</i>						(1+1)-ES [1]
PSO	1	1.4	1.3	<i>27e-1/1e5</i>							PSO [6]
PSO_Bounds	1	1	2.4	<i>34e-1/1e5</i>							PSO_Bounds [7]
Monte Carlo	1	1.3	2.5	<i>22e-1/1e6</i>							Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1.3	1.8	5.5	2.3	1.5	1.5	2.2	5.3	<i>86e-6/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1.5	2	<i>28e-1/500</i>							SNOBFIT [17]
VNS (Garcia)	1	1	4.1	1.5	8.6	46	520	<i>64e-5/6e6</i>			VNS (Garcia) [10]

Table 25: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{125} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$
ALPS	1	1	1	1.1	490	3.4e7	<i>12e-2/5e5</i>	2.97e5	6.38e5	6.44e5	6.44e5	ALPS [15]
AMaLGaM IDEA	1	1	1	1.1	160	1.1e6	<i>42e-3/1e6</i>	•	•	•	•	AMaLGaM IDEA [4]
avg NEWUOA	1	1	1	5.9	39	<i>19e-2/7e3</i>	•	•	•	•	•	avg NEWUOA [23]
BayEDA _{cG}	1	1	1	1.1	220	<i>24e-2/2e3</i>	•	•	•	•	•	BayEDA _{cG} [9]
BFGS	1	1	1	1.7	4.1e4	<i>97e-2/3e3</i>	•	•	•	•	•	BFGS [22]
BIPOP-CMA-ES	1	1	1	1	110	5e5	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	1	1	1	3e3	<i>40e-2/1e4</i>	•	•	•	•	•	(1+1)-CMA-ES [2]
DASA	1	1	1	2.9	8.9e4	<i>40e-2/4e5</i>	•	•	•	•	•	DASA [18]
DEPSO	1	1	1	1.1	290	<i>41e-2/2e3</i>	•	•	•	•	•	DEPSO [11]
EDA-PSO	1	1	1	1	310	7e6	<i>12e-2/1e5</i>	•	•	•	•	EDA-PSO [5]
full NEWUOA	1	1	1	9.8	240	<i>20e-2/1e4</i>	•	•	•	•	•	full NEWUOA [23]
GLOBAL	1	1	1	1.3	1200	<i>69e-2/500</i>	•	•	•	•	•	GLOBAL [20]
iAMaLGaM IDEA	1	1	1	1.2	110	1.9e6	130	<i>37e-3/1e6</i>	•	•	•	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1	1	1.1	170	8.5e5	<i>10e-2/5e4</i>	•	•	•	•	MA-LS-Chain [19]
MCS (Neum)	1	1	1	1	1	1	<i>25e-3/4e3</i>	•	•	•	•	MCS (Neum) [16]
NEWUOA	1	1	1	3.8	84	<i>22e-2/4e3</i>	•	•	•	•	•	NEWUOA [23]
(1+1)-ES	1	1	1	1	3e3	<i>25e-2/1e6</i>	•	•	•	•	•	(1+1)-ES [1]
PSO	1	1	1	1.1	250	<i>21e-2/1e5</i>	•	•	•	•	•	PSO [6]
PSO_Bounds	1	1	1	1.2	320	1.5e7	<i>17e-2/1e5</i>	•	•	•	•	PSO_Bounds [7]
Monte Carlo	1	1	1	1	1400	<i>28e-2/1e6</i>	•	•	•	•	•	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1	1	1	89	7.3e5	<i>22e-2/1e4</i>	•	•	•	•	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1	1	1.1	380	<i>58e-2/500</i>	•	•	•	•	•	SNOBFIT [17]
VNS (Garcia)	1	1	1	1.4	300	2.2e7	<i>76e-3/8e6</i>	•	•	•	•	VNS (Garcia) [10]

Table 26: 10-D, running time excess $\text{ERT}/\text{ERT}_{\text{best}}$ on f_{126} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

126 Griewank-Rosenbrock unif

	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$	1e+03 0.1	1e+02 0.1	1e+01 0.1	1e+00 0.1	1e-01 0.1	1e-02 nan	1e-03 nan	1e-04 nan	1e-05 nan	1e-07 nan	$\Delta\text{ftarget}$ $\text{ERT}_{\text{best}}/D$
ALPS	1	1	1	1	510	<i>21e-2/5e5</i>	ALPS [15]
AMaLGaM IDEA	1	1	1	1.3	220	4.9e7	<i>11e-2/1e6</i>	AMaLGaM IDEA [4]
avg NEWUOA	1	1	1	9.4	4.9e4	<i>89e-2/7e3</i>	avg NEWUOA [23]
BayEDA-cG	1	1	1	1.1	310	<i>59e-2/2e3</i>	BayEDA-cG [9]
BFGS	1	1	1	6.1	1.6e4	<i>11e-1/1e3</i>	BFGS [22]
BIPOP-CMA-ES	1	1	1	1	870	3.9e6	<i>84e-3/7e5</i>	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	1	1	1	4500	<i>53e-2/1e4</i>	(1+1)-CMA-ES [2]
DASA	1	1	1	1.2	1.1e5	<i>47e-2/4e5</i>	DASA [18]
DEPSO	1	1	1	1.1	1e3	<i>77e-2/2e3</i>	DEPSO [11]
EDA-PSO	1	1	1	1	2600	1.5e7	<i>41e-2/1e5</i>	EDA-PSO [5]
full NEWUOA	1	1	1	28	7.1e4	<i>75e-2/1e4</i>	full NEWUOA [23]
GLOBAL	1	1	1	1.1	1500	<i>78e-2/500</i>	GLOBAL [20]
iAMaLGaM IDEA	1	1	1	1.3	200	3.3e7	<i>13e-2/1e6</i>	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1	1	1.1	190	<i>22e-2/5e4</i>	MA-LS-Chain [19]
MCS (Neum)	1	1	1	1	1	1	<i>25e-3/4e3</i>	MCS (Neum) [16]
NEWUOA	1	1	1	29	1.2e4	<i>66e-2/4e3</i>	NEWUOA [23]
(1+1)-ES	1	1	1	1	6800	<i>30e-2/1e6</i>	(1+1)-ES [1]
PSO	1	1	1	1.3	950	<i>34e-2/1e5</i>	PSO [6]
PSO-Bounds	1	1	1	1	1.5e5	<i>61e-2/1e5</i>	PSO-Bounds [7]
Monte Carlo	1	1	1	1.1	980	<i>31e-2/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1	1	1.1	1.3e4	<i>41e-2/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1	1	1.2	670	<i>73e-2/500</i>	SNOBFIT [17]
VNS (Garcia)	1	1	1	1.4	1.8e4	<i>16e-2/7e6</i>	VNS (Garcia) [10]

Table 27: 10-D, running time excess ERT/ERT_{best} on f_{127} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target} ERT _{best} /D	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target} ERT _{best} /D
ALPS		1	1	1	370	<i>17e-2/5e5</i>	79900	1.35e5	2.06e5	2.08e5	2.11e5	ALPS [15]
AMaLGaM IDEA		1	1	1	150	1.3e5	5.5	25	34	34	34	AMaLGaM IDEA [4]
avg NEWUOA		1	1	1	40	<i>20e-2/7e3</i>	avg NEWUOA [23]
BayEDAeG		1	1	1.2	240	<i>21e-2/2e3</i>	BayEDAeG [9]
BFGS		1	1	60	5.8e4	<i>11e-1/2e3</i>	BFGS [22]
BIPOP-CMA-ES		1	1	1	54	8.5e4	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		1	1	1	790	<i>39e-2/1e4</i>	(1+1)-CMA-ES [2]
DASA		1	1	10	5.8e4	<i>46e-2/4e5</i>	DASA [18]
DEPSO		1	1	1.1	280	<i>33e-2/2e3</i>	DEPSO [11]
EDA-PSO		1	1	1.1	92	<i>29e-2/1e5</i>	EDA-PSO [5]
full NEWUOA		1	1	1	69	<i>23e-2/1e4</i>	full NEWUOA [23]
GLOBAL		1	1	1.1	880	<i>68e-2/500</i>	GLOBAL [20]
iAMaLGaM IDEA		1	1	1	90	4e5	15	23	22	21	21	iAMaLGaM IDEA [4]
MA-LS-Chain		1	1	1.1	130	<i>19e-2/5e4</i>	MA-LS-Chain [19]
MCS (Neum)		1	1	1	1	<i>25e-3/4e3</i>	MCS (Neum) [16]
NEWUOA		1	1	2.4	79	<i>25e-2/4e3</i>	NEWUOA [23]
(1+1)-ES		1	1	2.5	850	<i>19e-2/1e6</i>	(1+1)-ES [1]
PSO		1	1	1.1	570	<i>32e-2/1e5</i>	PSO [6]
PSO.Bounds		1	1	1	530	<i>40e-2/1e5</i>	PSO.Bounds [7]
Monte Carlo		1	1	1.1	1200	<i>33e-2/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES		1	1	1	47	3.7e4	1.8	<i>34e-3/1e4</i>	.	.	.	IPOP-SEP-CMA-ES [21]
SNOBFIT		1	1	1	250	<i>65e-2/500</i>	93	SNOBFIT [17]
VNS (Garcia)		1	1	1.4	220	3.8e5	93	<i>96e-4/7e6</i>	.	.	.	VNS (Garcia) [10]

Table 28: 10-D, running time excess ERT_{best} on f_{128} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}
	ERT_{best}/D	0.1	0.1	915	13800	14000	14400	29200	29300	38300	52900	ERT_{best}/D
ALPS	1	1	1	3.8	1.7	1.9	2	1.1	1.2	1	1	ALPS [15]
AMaLGaM IDEA	1	1	1	5	5.1	5.4	5.4	2.8	2.8	2.1	1.6	AMaLGaM IDEA [4]
avg NEWUOA	1	1	1	32	<i>21e+0/7e3</i>							avg NEWUOA [23]
BayEDAeG	1	1	1	2.6	2.2	<i>93e-1/2e3</i>						BayEDAeG [9]
BFGS	1	1	1	<i>57e+0/2e3</i>								BFGS [22]
BIPOP-CMA-ES	1	1	1	1	6.4	6.6	6.4	3.2	3.2	2.4	1.8	BIPOP-CMA-ES [14]
(1+1)-CMA-ES	1	1	1	25	<i>15e+0/1e4</i>							(1+1)-CMA-ES [2]
DASA	1	1	1	400	<i>91e-1/4e5</i>							DASA [18]
DEPSO	1	1	1	5.2	1	1	1	1	1	<i>15e+0/2e3</i>		DEPSO [11]
EDA-PSO	1	1	1	310	100	100	97	48	48	37	27	EDA-PSO [5]
full NEWUOA	1	1	1	77	<i>23e+0/1e4</i>							full NEWUOA [23]
GLOBAL	1	1	1	8.6	<i>22e+0/500</i>							GLOBAL [20]
iAMaLGaM IDEA	1	1	1	14	6	11	11	5.7	5.8	4.4	3.3	iAMaLGaM IDEA [4]
MA-LS-Chain	1	1	1	4.1	2.9	3	3.1	1.6	1.6	1.2	1	MA-LS-Chain [19]
MCS (Neum)	1	1	1	14	4.1	<i>13e+0/4e3</i>						MCS (Neum) [16]
NEWUOA	1	1	1	<i>24e+0/4e3</i>								NEWUOA [23]
(1+1)-ES	1	1	1	36	120							(1+1)-ES [1]
PSO	1	1	1	230	<i>16e+0/1e5</i>							PSO [6]
PSO_Bounds	1	1	1	220	<i>19e+0/1e5</i>							PSO_Bounds [7]
Monte Carlo	1	1	1	11	1100							Monte Carlo [3]
IPOP-SEP-CMA-ES	1	1	1	11	3.2	<i>20e-1/1e6</i>						IPOP-SEP-CMA-ES [21]
SNOBFIT	1	1	1	4	<i>22e+0/500</i>							SNOBFIT [17]
VNS (Garcia)	1	1	1	31	9	9.1	11	7	10	13	14	VNS (Garcia) [10]

Table 29: 10-D, running time excess ERT/ERT_{best} on f_{129} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

	Δt_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δt_{target}
	ERT_{best}/D	0.1	0.1	5400	1.36e5	1.41e5	1.42e5	1.43e5	1.44e5	1.45e5	1.47e5	ERT_{best}/D
ALPS		1	1	2	26	<i>23e-1/5e5</i>	23	23	23	31	100	ALPS [15]
AMaLGaM IDEA		1	1	12	6.1	14	23	23	23	31	100	AMaLGaM IDEA [4]
avg NEWUOA		1	1	<i>39e+0/7e3</i>	avg NEWUOA [23]
BayEDAacG		1	1	<i>30e+0/2e3</i>	BayEDAacG [9]
BFGS		1	1	<i>46e+0/900</i>	BFGS [22]
BIPOP-CMA-ES		1	1	1	1	1	1	1	1	1	1	BIPOP-CMA-ES [14]
(1+1)-CMA-ES		1	1	<i>18e+0/1e4</i>	(1+1)-CMA-ES [2]
DASA		1	1	360	<i>13e+0/4e5</i>	DASA [18]
DEPSO		1	1	5.5	<i>24e+0/2e3</i>	DEPSO [11]
EDA-PSO		1	1	260	<i>20e+0/1e5</i>	EDA-PSO [5]
full NEWUOA		1	1	<i>41e+0/1e4</i>	full NEWUOA [23]
GLOBAL		1	1	<i>28e+0/400</i>	GLOBAL [20]
iAMaLGaM IDEA		1	1	12	18	47	100	99	99	98	97	iAMaLGaM IDEA [4]
MA-LS-Chain		1	1	1.7	5.3	<i>48e-1/5e4</i>	MA-LS-Chain [19]
MCS (Neum)		1	1	<i>21e+0/4e3</i>	MCS (Neum) [16]
NEWUOA		1	1	<i>39e+0/4e3</i>	NEWUOA [23]
(1+1)-ES		1	1	21	110	<i>56e-1/1e6</i>	(1+1)-ES [1]
PSO		1	1	260	<i>18e+0/1e5</i>	PSO [6]
PSO_Bounds		1	1	260	<i>26e+0/1e5</i>	PSO_Bounds [7]
Monte Carlo		1	1	1.3	32	<i>20e-1/1e6</i>	Monte Carlo [3]
IPOP-SEP-CMA-ES		1	1	13	<i>22e+0/1e4</i>	IPOP-SEP-CMA-ES [21]
SNOBFIT		1	1	<i>27e+0/500</i>	SNOBFIT [17]
VNS (Garcia)		1	1	42	69	<i>72e-2/7e6</i>	VNS (Garcia) [10]

129 Gallagher unif

Table 30: 10-D, running time excess ERT/ERT_{best} on f_{130} , in italics is given the median final function value and the median number of function evaluations to reach this value divided by dimension

130 Gallagher Cauchy												
Δf_{target}	1e+03	1e+02	1e+01	1e+00	1e-01	1e-02	1e-03	1e-04	1e-05	1e-07	Δf_{target}	
ERT_{best}/D	0.1	0.1	48.1	588	3750	7050	7090	7150	7220	7330	ERT_{best}/D	
ALPS	1	1	6.7	9	67	<i>62e-3/5e5</i>					ALPS [15]	
AMaLGaM IDEA	1	1	8	170	35	19	19	20	20	20	AMaLGaM IDEA [4]	
avg NEWUOA	1	1	1.9	6	8.6	<i>41e-2/7e3</i>					avg NEWUOA [23]	
BayEDAeG	1	1	17	23	<i>20e-1/2e3</i>						BayEDAeG [9]	
BFGS	1	1	100	<i>10e+0/2e3</i>							BFGS [22]	
BIPOP-CMA-ES	1	1	4.9	34	18	9.7	9.6	9.6	9.5	9.4	BIPOP-CMA-ES [14]	
(1+1)-CMA-ES	1	1	2.5	6.5	11	<i>51e-2/1e4</i>					(1+1)-CMA-ES [2]	
DASA	1	1	590	<i>30e-1/5e5</i>							DASA [18]	
DEPSO	1	1	8.3	10	1.8	<i>19e-1/2e3</i>					DEPSO [11]	
EDA-PSO	1	1	380	680	<i>53e-1/1e5</i>						EDA-PSO [5]	
full NEWUOA	1	1	6.7	8.3	5.1	<i>12e-2/1e4</i>					full NEWUOA [23]	
GLOBAL	1	1	1	1	1	<i>50e-2/600</i>					GLOBAL [20]	
iAMaLGaM IDEA	1	1	1	4.4	1.5	1.8	8.4	11	12	21	iAMaLGaM IDEA [4]	
MA-LS-Chain	1	1	4.7	19	7.1	3.9	5.2	15	<i>15e-5/5e4</i>		MA-LS-Chain [19]	
MCS (Neum)	1	1	32	<i>30e-1/4e3</i>							MCS (Neum) [16]	
NEWUOA	1	1	2.6	11	8	8.8	8.7	<i>14e-1/4e3</i>			NEWUOA [23]	
(1+1)-ES	1	1	1.7	4.6	24	460	<i>18e-3/1e6</i>				(1+1)-ES [1]	
PSO	1	1	180	680	190	<i>25e-1/1e5</i>					PSO [6]	
PSO_Bounds	1	1	770	<i>69e-1/1e5</i>							PSO_Bounds [7]	
Monte Carlo	1	1	160	2.4e4							Monte Carlo [3]	
IPOP-SEP-CMA-ES	1	1	2.3	11	1.9	1	1	1	1	1	IPOP-SEP-CMA-ES [21]	
SNOBFIT	1	1	2.2	12	<i>28e-1/500</i>						SNOBFIT [17]	
VNS (Garcia)	1	1	97	210	38	20	20	20	20	19	VNS (Garcia) [10]	

References

- [1] Anne Auger. Benchmarking the (1+1)-ES with one-fifth success rule on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2453–2458.
- [2] Anne Auger and Nikolaus Hansen. Benchmarking the (1+1)-CMA-ES on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2467–2472.
- [3] Anne Auger and Raymond Ros. Benchmarking the pure random search on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2485–2490.
- [4] Peter A. N. Bosman, Jörn Grahl, and Dirk Thierens. AMaLGaM IDEAs in noisy black-box optimization benchmarking. In Rothlauf [24], pages 2351–2358.
- [5] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using an EDA and PSO hybrid. In Rothlauf [24], pages 2263–2268.
- [6] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using particle swarm optimization. In Rothlauf [24], pages 2269–2274.
- [7] Mohammed El-Abd and Mohamed S. Kamel. Black-box optimization benchmarking for noiseless function testbed using PSO_Bounds. In Rothlauf [24], pages 2275–2280.
- [8] S. Finck, N. Hansen, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Presentation of the noisy functions. Technical Report 2009/21, Research Center PPE, 2009.
- [9] Marcus R. Gallagher. Black-box optimization benchmarking: results for the BayEDAcG algorithm on the noisy function testbed. In Rothlauf [24], pages 2383–2388.
- [10] Carlos García-Martínez and Manuel Lozano. A continuous variable neighbourhood search based on specialised EAs: application to the noisy BBO-benchmark 2009 testbed. In Rothlauf [24], pages 2367–2374.
- [11] José García-Nieto, Enrique Alba, and Javier Apolloni. Particle swarm hybridized with differential evolution: black box optimization benchmarking for noisy functions. In Rothlauf [24], pages 2343–2350.
- [12] N. Hansen, A. Auger, S. Finck, and R. Ros. Real-parameter black-box optimization benchmarking 2009: Experimental setup. Technical Report RR-6828, INRIA, 2009.
- [13] N. Hansen, S. Finck, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Noisy functions definitions. Technical Report RR-6869, INRIA, 2009.
- [14] Nikolaus Hansen. Benchmarking a bi-population CMA-ES on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2397–2402.

- [15] Gregory S. Hornby. The Age-Layered Population Structure (ALPS) evolutionary algorithm, July 2009. Noisy testbed.
- [16] Waltraud Huyer and Arnold Neumaier. Benchmarking of MCS on the noisy function testbed. <http://www.mat.univie.ac.at/~neum/papers.html>, 2009. P. 988.
- [17] Waltraud Huyer and Arnold Neumaier. Benchmarking of SNOBFIT on the noisy function testbed. <http://www.mat.univie.ac.at/~neum/papers.html>, 2009. P. 987.
- [18] Peter Korosec and Jurij Silc. A stigmergy-based algorithm for black-box optimization: noisy function testbed. In Rothlauf [24], pages 2375–2382.
- [19] Daniel Molina, Manuel Lozano, and Francisco Herrera. A memetic algorithm using local search chaining for black-box optimization benchmarking 2009 for noisy functions. In Rothlauf [24], pages 2359–2366.
- [20] László Pál, Tibor Csendes, Mihály Csaba Markót, and Arnold Neumaier. BBO-benchmarking of the GLOBAL method for the noisy function testbed. <http://www.mat.univie.ac.at/~neum/papers.html>, 2009. P. 985.
- [21] Raymond Ros. Benchmarking sep-CMA-ES on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2441–2446.
- [22] Raymond Ros. Benchmarking the BFGS algorithm on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2415–2420.
- [23] Raymond Ros. Benchmarking the NEWUOA on the BBOB-2009 noisy testbed. In Rothlauf [24], pages 2429–2434.
- [24] Franz Rothlauf, editor. *Genetic and Evolutionary Computation Conference, GECCO 2009, Proceedings, Montreal, Québec, Canada, July 8-12, 2009, Companion Material*. ACM, 2009.