

# Comparison Tables: CEC BBOB 2015 Testbed in 3-D (Expensive Setting)

The BBOBies

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## Abstract

This document provides tabular results of the special session on Black-Box Optimization Benchmarking at CEC 2015 with a focus on benchmarking black-box algorithms for small function evaluation budgets (“expensive setting”), see <http://coco.gforge.inria.fr/doku.php?id=cec-bbob-2015>. Overall, eight algorithms have been tested on 24 benchmark functions in dimensions between 2 and 20. A description of the used objective functions can be found in [6, 4]. The experimental set-up is described in [5].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [5] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed at CEC 2015.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
MATSuMoTo		Comparison of the MATSuMoTo Library for Expensive Optimization on the Noiseless Black-Box Optimization Benchmarking Testbed	[2]
R-DE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-DE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-SHADE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-SHADE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
RL-SHADE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
RL-SHADE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
SOO		Simultaneous Optimistic Optimization on the Noiseless BBOB Testbed	[3]

Table 2: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>1.6e+1:3.0</i>	<i>1.0e+1:3.6</i>	<i>1.0e-8:8.0</i>	<i>1.0e-8:8.0</i>	<i>1.0e-8:8.0</i>	15/15
MATSUMOTO	<b>1.6</b> (2)	<b>1.9</b> (1)	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
R-DE-10e2-	<b>1.6</b> (0.9)	<b>2.6</b> (3)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>2.4</b> (3)	<b>2.5</b> (3)	<b>72</b> (33)	<b>72</b> (68)	<b>72</b> (43)	15/15
RL-SHADE-1	<b>1.4</b> (1)	<b>1.5</b> (1)	279(150)	279(234)	279(385)	2/15
RL-SHADE-1	<b>1.4</b> (0.7)	<b>2.1</b> (2)	387(38)	387(29)	387(26)	15/15
R-SHADE-10	<b>1.8</b> (2)	<b>2.9</b> (3)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
R-SHADE-10	<b>2.3</b> (2)	3.0(2)	<b>74</b> (5)	<b>74</b> (11)	<b>74</b> (8)	15/15
SOO-Derbel	<b>0.69</b> (0.5)	<b>1.1</b> (1.0)	99(4)	99(7)	99(10)	15/15

Table 3: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><math>f_2</math></b>	<i>6.3e+6</i> :1.5	<i>6.3e+5</i> :4.3	<i>4.0e+4</i> :10	<i>1.0e+2</i> :32	<i>1.0e-8</i> :49	15/15
MATSUMOTO	<b>1.3</b> (1.0)	<b>0.89</b> (0.8)	<b>1.8</b> (1)	22(30)	$\infty$ 150	0/15
R-DE-10e2-	<b>1.9</b> (0.8)	<b>1.8</b> (2)	<b>2.1</b> (3)	<b>3.3</b> (1)	$\infty$ 300	0/15
R-DE-10e5-	<b>1.8</b> (6)	<b>1.6</b> (3)	<b>2.1</b> (2)	<b>3.6</b> (3)	<b>26</b> (8)	15/15
RL-SHADE-1	<b>2.1</b> (2)	<b>1.7</b> (0.7)	4.0(2)	3.9(1)	$\infty$ 300	0/15
RL-SHADE-1	<b>1.1</b> (1.0)	<b>1.3</b> (0.8)	<b>2.8</b> (3)	18(8)	91(6)	15/15
R-SHADE-10	<b>1.4</b> (1.0)	<b>1.5</b> (0.8)	4.0(3)	4.8(2)	$\infty$ 300	0/15
R-SHADE-10	<b>1.3</b> (0)	<b>1.2</b> (1)	<b>2.7</b> (1)	4.7(1)	<b>18</b> (3)	15/15
SOO-Derbel	<b>1.5</b> (1)	<b>2.5</b> (2)	3.7(3)	6.0(2)	39(5)	15/15

Table 4: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>1.0e+2:2.2</i>	<i>6.3e+1:6.1</i>	<i>4.0e+1:10</i>	<i>1.6e+1:32</i>	<i>4.0e+0:319</i>	15/15
MATSUMOTO	<b>1.9</b> <sup>(1)</sup>	<b>1.1</b> <sup>(1.0)</sup>	<b>1.4</b> <sup>(0.8)</sup>	<b>1.6</b> <sup>(0.8)</sup>	<b>0.95</b> <sup>(1)</sup>	6/15
R-DE-10e2-	<b>2.2</b> <sup>(1)</sup>	<b>2.2</b> <sup>(2)</sup>	<b>2.7</b> <sup>(1.0)</sup>	<b>2.0</b> <sup>(0.8)</sup>	<b>1.1</b> <sup>(1)</sup>	10/15
R-DE-10e5-	<b>2.0</b> <sup>(2)</sup>	<b>1.6</b> <sup>(0.9)</sup>	<b>2.3</b> <sup>(1.0)</sup>	<b>2.9</b> <sup>(0.6)</sup>	<b>1.0</b> <sup>(0.8)</sup>	15/15
RL-SHADE-1	<b>2.1</b> <sup>(2)</sup>	<b>1.8</b> <sup>(2)</sup>	<b>2.5</b> <sup>(1)</sup>	<b>2.2</b> <sup>(1)</sup>	<b>0.44</b> <sup>(0.2)</sup>	15/15
RL-SHADE-1	<b>2.2</b> <sup>(3)</sup>	<b>1.6</b> <sup>(1)</sup>	<b>2.6</b> <sup>(3)</sup>	6.5 <sup>(3)</sup>	<b>2.0</b> <sup>(0.9)</sup>	15/15
R-SHADE-10	<b>2.2</b> <sup>(0.9)</sup>	<b>2.3</b> <sup>(3)</sup>	<b>2.1</b> <sup>(0.8)</sup>	<b>2.3</b> <sup>(0.9)</sup>	<b>0.57</b> <sup>(0.1)</sup>	14/15
R-SHADE-10	<b>2.3</b> <sup>(1)</sup>	<b>1.6</b> <sup>(2)</sup>	3.1 <sup>(1)</sup>	<b>2.1</b> <sup>(2)</sup>	<b>1.7</b> <sup>(2)</sup>	15/15
SOO-Derbel	<b>0.91</b> <sup>(0)</sup>	<b>0.80</b> <sup>(0.5)</sup>	<b>2.2</b> <sup>(1)</sup>	<b>2.2</b> <sup>(1)</sup>	<b>1.4</b> <sup>(1)</sup>	15/15

Table 5: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><math>f_4</math></b>	<i>1.0e+2:5.4</i>	<i>6.3e+1:10</i>	<i>6.3e+1:10</i>	<i>2.5e+1:36</i>	<i>4.0e+0:617</i>	15/15
MATSUMOTO	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.8</b> (1)	<b>1.4</b> (1.0)	<b>1.2</b> (2)	3/15
R-DE-10e2-	<b>2.4</b> (4)	<b>2.0</b> (2)	<b>2.0</b> (2)	<b>1.6</b> (1)	<b>0.60</b> (0.4)	10/15
R-DE-10e5-	<b>1.2</b> (1)	<b>2.0</b> (1)	<b>2.0</b> (1)	<b>1.5</b> (0.5)	<b>1.3</b> (1)	15/15
RL-SHADE-1	<b>1.0</b> (1)	<b>2.2</b> (1)	<b>2.2</b> (2)	<b>1.5</b> (1)	<b>0.58</b> (0.5)	9/15
RL-SHADE-1	<b>2.4</b> (3)	<b>2.5</b> (2)	<b>2.5</b> (5)	5.4(1)	<b>1.7</b> (0.8)	15/15
R-SHADE-10	<b>1.5</b> (2)	<b>1.8</b> (3)	<b>1.8</b> (1)	<b>1.8</b> (0.6)	<b>0.49</b> (0.4)	11/15
R-SHADE-10	<b>1.1</b> (0.9)	<b>1.2</b> (1)	<b>1.2</b> (1)	<b>2.0</b> (3)	<b>1.3</b> (1)	15/15
SOO-Derbel	<b>0.69</b> (2)	<b>0.99</b> (1.0)	<b>0.99</b> (1)	<b>2.1</b> (1)	<b>0.94</b> (0.5)	15/15

Table 6: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f5</b>	<i>4.0e+1</i> :2.2	<i>2.5e+1</i> :4.8	<i>1.0e-8</i> :6.6	<i>1.0e-8</i> :6.6	<i>1.0e-8</i> :6.6	15/15
MATSUMOTO	<b>1.5</b> (1)	<b>1.0</b> (0.8)	<b>1.9</b> (0.6) <sup>*4</sup>	<b>1.9</b> (0.5) <sup>*4</sup>	<b>1.9</b> (0.5) <sup>*4</sup>	15/15
R-DE-10e2-	<b>2.2</b> (1)	<b>3.0</b> (3)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>2.8</b> (2)	<b>3.0</b> (2)	256(292)	256(170)	256(299)	15/15
RL-SHADE-1	<b>1.8</b> (3)	<b>1.6</b> (3)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
RL-SHADE-1	3.8(2)	3.9(4)	431(21)	431(8)	431(15)	15/15
R-SHADE-10	4.7(4)	4.4(3)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
R-SHADE-10	<b>1.5</b> (0.9)	3.6(4)	<b>150</b> (17)	<b>150</b> (26)	<b>150</b> (26)	15/15
SOO-Derbel	<b>2.0</b> (0.2)	<b>1.8</b> (0.1)	531(0.1)	531(0.1)	531(0.1)	15/15

Table 7: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>6.3e+4</i> :1.8	<i>6.3e+3</i> :3.7	<i>4.0e+1</i> :13	<i>1.0e+1</i> :34	<i>6.3e-4</i> :159	15/15
MATSUMOTO	<b>1.2</b> (2)	<b>1.1</b> (1)	3.2(3)	6.3(5)	$\infty$ 150	0/15
R-DE-10e2-	<b>2.9</b> (3)	<b>2.1</b> (3)	3.2(1)	<b>1.9</b> (3)	$\infty$ 300	0/15
R-DE-10e5-	<b>2.8</b> (6)	3.4(3)	<b>2.0</b> (1)	<b>2.2</b> (0.5)	26(50)	15/15
RL-SHADE-1	<b>1.9</b> (3)	<b>2.6</b> (4)	<b>2.9</b> (1)	<b>2.7</b> (0.4)	28(31)	1/15
RL-SHADE-1	<b>1.6</b> (0.6)	4.8(4)	6.3(7)	4.9(5)	<b>16</b> (3)	15/15
R-SHADE-10	<b>2.0</b> (1)	3.9(8)	<b>3.0</b> (2)	<b>2.6</b> (1)	$\infty$ 300	0/15
R-SHADE-10	<b>1.3</b> (1)	3.7(8)	3.8(8)	<b>2.3</b> (2)	<b>3.4</b> (0.3)	15/15
SOO-Derbel	<b>1.4</b> (2)	<b>1.7</b> (1.0)	<b>2.0</b> (2)	<b>1.9</b> (2)	1.3e4(8958)	2/15

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Table 8: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><math>f_7</math></b>	<i>2.5e+2</i> :1.5	<i>6.3e+1</i> :4.2	<i>1.0e+1</i> :11	<i>2.5e+0</i> :38	<i>4.0e-1</i> :174	15/15
MATSUMOTO	<b>1.3</b> (0.8)	<b>1.4</b> (1)	<b>2.3</b> (2)	<b>1.6</b> (0.7)	<b>1.7</b> (1.0)	7/15
R-DE-10e2-	<b>1.0</b> (1.0)	<b>1.4</b> (2)	<b>2.2</b> (1)	<b>1.4</b> (1)	<b>1.0</b> (1)	13/15
R-DE-10e5-	<b>1.2</b> (1)	<b>0.94</b> (1.0)	<b>1.7</b> (2)	<b>1.4</b> (2)	<b>2.4</b> (1)	15/15
RL-SHADE-1	<b>1.7</b> (2)	<b>2.1</b> (3)	3.5(4)	<b>2.3</b> (1)	<b>1.2</b> (0.6)	13/15
RL-SHADE-1	<b>2.0</b> (0.7)	3.8(2)	6.6(7)	5.0(3)	<b>2.5</b> (0.4)	15/15
R-SHADE-10	<b>1.3</b> (1.0)	<b>1.3</b> (2)	3.4(3)	<b>2.2</b> (0.7)	<b>2.5</b> (3)	8/15
R-SHADE-10	<b>2.2</b> (2)	3.6(2)	3.7(6)	<b>2.2</b> (2)	<b>1.4</b> (0.7)	15/15
SOO-Derbel	<b>1.1</b> (0.7)	<b>1.1</b> (2)	<b>2.3</b> (0.7)	<b>1.5</b> (0.7)	<b>2.6</b> (8)	15/15

Table 9: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>1.0e+4</i> :1.8	<i>1.6e+3</i> :4.0	<i>1.0e+2</i> :15	<i>6.3e+0</i> :31	<i>1.0e-1</i> :152	15/15
MATSUMOTO	<b>1.6</b> (2)	<b>1.1</b> (0.5)	<b>1.5</b> (0.8)	4.1(5)	15(15)	1/15
R-DE-10e2-	<b>1.7</b> (1)	3.5(5)	3.2(2)	3.7(1)	5.6(6)	5/15
R-DE-10e5-	<b>1.3</b> (1.0)	<b>1.6</b> (2)	<b>2.2</b> (2)	3.5(1)	14(19)	15/15
RL-SHADE-1	<b>1.4</b> (0.8)	3.8(2)	3.2(1)	<b>3.3</b> (1)	14(10)	2/15
RL-SHADE-1	<b>1.1</b> (0.6)	<b>2.6</b> (1)	5.7(3)	11(4)	14(4)	15/15
R-SHADE-10	<b>1.5</b> (1)	<b>2.1</b> (2)	3.1(2)	5.3(3)	$\infty$ 300	0/15
R-SHADE-10	<b>2.0</b> (2)	<b>2.0</b> (2)	<b>2.2</b> (2)	3.4(1)	<b>4.6</b> (2)	15/15
SOO-Derbel	<b>1.4</b> (2)	<b>1.1</b> (0.9)	<b>1.1</b> (0.8)	<b>1.8</b> (0.7)	<b>4.6</b> (2)	15/15

Table 10: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>1.0e+1:21</i>	<i>6.3e+0:25</i>	<i>4.0e+0:32</i>	<i>2.5e+0:48</i>	<i>6.3e-3:152</i>	15/15
MATSUMOTO-	<b>2.5</b> (2)	<b>2.5</b> (1)	<b>2.7</b> (3)	<b>2.4</b> (3)	$\infty$ 150	0/15
R-DE-10e2-	4.5(2)	4.4(2)	4.2(2)	4.4(1)	$\infty$ 300	0/15
R-DE-10e5-	8.1(17)	8.4(24)	15(30)	26(34)	36(23)	15/15
RL-SHADE-1	5.1(4)	5.2(10)	5.0(2)	5.4(5)	$\infty$ 300	0/15
RL-SHADE-1	14(12)	15(13)	15(8)	13(6)	19(4)	15/15
R-SHADE-10	6.2(3)	8.3(7)	12(12)	9.3(9)	$\infty$ 300	0/15
R-SHADE-10	3.7(1)	3.6(2)	3.6(2)	3.1(2)	<b>4.4</b> (4)	15/15
SOO-Derbel	<b>2.2</b> (1)	<b>2.1</b> (0.5)	<b>2.0</b> (1.0)	<b>1.7</b> (0.8)	<b>12</b> (5)	15/15

Table 11: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>6.3e+6:1.7</i>	<i>1.6e+5:4.4</i>	<i>4.0e+4:12</i>	<i>4.0e+2:37</i>	<i>1.0e+0:152</i>	15/15
MATSUMOTO	<b>1.2</b> (1)	<b>2.2</b> (1)	<b>1.1</b> (0.5)	10(18)	$\infty$ 150	0/15
R-DE-10e2-	<b>0.88</b> (0.4)	<b>2.1</b> (3)	<b>1.6</b> (1)	5.5(5)	29(33)	1/15
R-DE-10e5-	<b>1.3</b> (4)	<b>2.3</b> (2)	<b>1.6</b> (1)	14(7)	52(40)	15/15
RL-SHADE-1	<b>1.0</b> (0.8)	3.0(3)	<b>2.0</b> (2)	8.9(9)	$\infty$ 300	0/15
RL-SHADE-1	<b>1.3</b> (0.6)	3.7(3)	4.5(4)	11(11)	<b>14</b> (4)	15/15
R-SHADE-10	<b>2.0</b> (0.9)	<b>2.8</b> (2)	<b>2.3</b> (1)	20(17)	$\infty$ 300	0/15
R-SHADE-10	<b>1.2</b> (0.6)	<b>2.6</b> (3)	<b>1.8</b> (2)	<b>3.0</b> (1)	<b>2.2</b> (0.4)	15/15
SOO-Derbel	<b>1.0</b> (1)	<b>1.8</b> (2)	<b>1.2</b> (0.9)	<b>3.7</b> (2)	92(178)	15/15

Table 12: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>2.5e+6</i> :1.9	<i>4.0e+5</i> :4.5	<i>6.3e+4</i> :9.4	<i>2.5e+1</i> :36	<i>2.5e-1</i> :174	15/15
MATSUMOTO	<b>1.6</b> (2)	<b>1.3</b> (1)	<b>1.4</b> (0.8)	7.8(12)	$\infty$ <i>150</i>	0/15
R-DE-10e2-	<b>1.2</b> (1)	<b>1.3</b> (1)	<b>1.4</b> (1)	13(16)	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>2.0</b> (2)	<b>1.4</b> (1)	<b>1.7</b> (2)	23(39)	100(176)	15/15
RL-SHADE-1	<b>2.8</b> (3)	<b>2.3</b> (2)	<b>2.6</b> (2)	17(9)	$\infty$ <i>300</i>	0/15
RL-SHADE-1	<b>1.6</b> (0.8)	<b>1.3</b> (1)	<b>1.3</b> (0.5)	15(16)	<b>12</b> (2)	15/15
R-SHADE-10	<b>1.2</b> (1)	<b>0.99</b> (0.5)	<b>1.1</b> (2)	9.2(13)	$\infty$ <i>300</i>	0/15
R-SHADE-10	<b>1.4</b> (0.8)	<b>2.3</b> (2)	<b>1.6</b> (1)	<b>4.6</b> (2)	<b>3.3</b> (4)	15/15
SOO-Derbel	<b>1.8</b> (2)	<b>1.6</b> (2)	<b>1.8</b> (0.8)	<b>4.6</b> (3)	183(927)	14/15

Table 13: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>1.0e+8</i> :1.5	<i>1.0e+7</i> :3.6	<i>6.3e+5</i> :13	<i>6.3e+2</i> :31	<i>1.0e+0</i> :168	15/15
MATSUMOTO	<b>0.83</b> <sup>(0)</sup>	<b>1.1</b> <sup>(2)</sup>	<b>1.4</b> <sup>(0.5)</sup>	<b>3.4</b> <sup>(1)</sup>	14 <sup>(19)</sup>	1/15
R-DE-10e2-	<b>0.91</b> <sup>(0.7)</sup>	<b>1.6</b> <sup>(1)</sup>	<b>2.4</b> <sup>(2)</sup>	6.7 <sup>(0.9)</sup>	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>1.1</b> <sup>(1.0)</sup>	<b>2.5</b> <sup>(4)</sup>	<b>2.5</b> <sup>(1)</sup>	10 <sup>(8)</sup>	76 <sup>(126)</sup>	15/15
RL-SHADE-1	<b>1.2</b> <sup>(1.0)</sup>	<b>1.9</b> <sup>(2)</sup>	<b>2.4</b> <sup>(1)</sup>	5.4 <sup>(2)</sup>	$\infty$ <i>300</i>	0/15
RL-SHADE-1	<b>1.0</b> <sup>(0.3)</sup>	<b>2.3</b> <sup>(3)</sup>	4.2 <sup>(2)</sup>	25 <sup>(16)</sup>	20 <sup>(7)</sup>	15/15
R-SHADE-10	<b>1.3</b> <sup>(0.7)</sup>	<b>2.0</b> <sup>(2)</sup>	<b>2.3</b> <sup>(2)</sup>	11 <sup>(12)</sup>	$\infty$ <i>300</i>	0/15
R-SHADE-10	<b>0.87</b> <sup>(0.3)</sup>	<b>1.3</b> <sup>(1)</sup>	<b>2.7</b> <sup>(2)</sup>	5.5 <sup>(2)</sup>	<b>8.2</b> <sup>(20)</sup>	15/15
SOO-Derbel	<b>0.87</b> <sup>(0)</sup>	<b>0.89</b> <sup>(0.6)</sup>	<b>1.3</b> <sup>(1)</sup>	<b>4.8</b> <sup>(0.8)</sup>	<b>4.3</b> <sup>(0.8)</sup>	15/15

Table 14: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>1.0e+3</i> :1.6	<i>4.0e+2</i> :6.8	<i>2.5e+2</i> :11	<i>4.0e+1</i> :30	<i>2.5e-3</i> :182	15/15
MATSUMOTO	<b>1.5</b> (1)	<b>1.0</b> (0.9)	<b>0.86</b> (0.5)	<b>1.6</b> (0.4)	$\infty$ 150	0/15
R-DE-10e2-	<b>1.0</b> (0.9)	<b>1.2</b> (1)	<b>1.1</b> (0.6)	<b>2.6</b> (0.8)	$\infty$ 300	0/15
R-DE-10e5-	<b>1.6</b> (2)	<b>1.9</b> (2)	<b>1.7</b> (2)	3.9(4)	44(24)	15/15
RL-SHADE-1	<b>1.2</b> (1)	<b>1.6</b> (2)	<b>1.7</b> (2)	3.8(9)	$\infty$ 300	0/15
RL-SHADE-1	<b>1.4</b> (0.3)	<b>2.4</b> (2)	3.3(4)	12(3)	21(1)	15/15
R-SHADE-10	<b>2.0</b> (1)	<b>1.5</b> (2)	<b>1.8</b> (2)	3.9(2)	$\infty$ 300	0/15
R-SHADE-10	<b>1.3</b> (0.8)	<b>2.1</b> (3)	<b>2.4</b> (1)	3.7(1)	<b>3.8</b> (1)	15/15
SOO-Derbel	<b>0.83</b> (1)	<b>0.74</b> (0.7)	<b>0.87</b> (0.6)	<b>2.4</b> (2)	<b>20</b> (17)	15/15

Table 15: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>1.0e+1:2.2</i>	<i>6.3e+0:4.2</i>	<i>2.5e+0:10</i>	<i>6.3e-2:31</i>	<i>2.5e-6:160</i>	15/15
MATSUMOTO	<b>1.5</b> (1)	<b>1.5</b> (2)	<b>1.6</b> (1)	<b>2.8</b> (4)	$\infty$ <i>150</i>	0/15
R-DE-10e2-	<b>1.8</b> (1)	<b>1.7</b> (1)	<b>2.2</b> (1)	3.7(1)	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>2.8</b> (7)	<b>2.0</b> (2)	<b>2.2</b> (2)	4.9(5)	107(113)	15/15
RL-SHADE-1	<b>1.7</b> (2)	<b>2.0</b> (2)	<b>2.5</b> (2)	3.7(2)	$\infty$ <i>300</i>	0/15
RL-SHADE-1	<b>1.3</b> (1)	<b>0.90</b> (0.8)	<b>2.7</b> (5)	19(5)	<b>22</b> (2)	15/15
R-SHADE-10	3.5(6)	<b>2.5</b> (4)	<b>2.4</b> (2)	4.9(2)	$\infty$ <i>300</i>	0/15
R-SHADE-10	<b>2.7</b> (3)	<b>2.0</b> (2)	<b>2.5</b> (4)	4.5(1)	<b>3.8</b> (0.4)	15/15
SOO-Derbel	<b>1.3</b> (1)	<b>0.92</b> (0.8)	<b>0.93</b> (0.5)	<b>3.4</b> (1)	225(75)	14/15



Table 16: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>1.6e+2</i> :1.6	<i>6.3e+1</i> :5.6	<i>4.0e+1</i> :12	<i>1.6e+1</i> :68	<i>6.3e+0</i> :221	15/15
MATSUMOTO	<b>1.3</b> <sup>(0.9)</sup>	<b>0.96</b> <sup>(0.6)</sup>	<b>1.3</b> <sup>(1)</sup>	<b>0.66</b> <sup>(0.6)</sup>	<b>0.82</b> <sup>(0.6)</sup>	9/15
R-DE-10e2-	<b>2.2</b> <sup>(4)</sup>	<b>1.9</b> <sup>(2)</sup>	<b>2.0</b> <sup>(2)</sup>	<b>0.92</b> <sup>(0.7)</sup>	<b>1.3</b> <sup>(1)</sup>	11/15
R-DE-10e5-	<b>2.1</b> <sup>(4)</sup>	<b>1.9</b> <sup>(2)</sup>	<b>1.5</b> <sup>(1)</sup>	<b>0.97</b> <sup>(0.4)</sup>	3.3 <sup>(3)</sup>	15/15
RL-SHADE-1	<b>1.8</b> <sup>(2)</sup>	<b>2.2</b> <sup>(2)</sup>	<b>2.1</b> <sup>(1.0)</sup>	<b>1.3</b> <sup>(0.4)</sup>	<b>0.91</b> <sup>(0.6)</sup>	13/15
RL-SHADE-1	<b>2.0</b> <sup>(2)</sup>	<b>2.0</b> <sup>(3)</sup>	<b>2.6</b> <sup>(2)</sup>	<b>2.9</b> <sup>(1)</sup>	<b>2.8</b> <sup>(2)</sup>	15/15
R-SHADE-10	<b>0.96</b> <sup>(0.3)</sup>	<b>1.4</b> <sup>(4)</sup>	<b>1.9</b> <sup>(2)</sup>	<b>1.6</b> <sup>(0.9)</sup>	<b>2.1</b> <sup>(2)</sup>	8/15
R-SHADE-10	<b>3.0</b> <sup>(2)</sup>	<b>3.0</b> <sup>(2)</sup>	3.1 <sup>(4)</sup>	<b>1.4</b> <sup>(0.6)</sup>	<b>1.3</b> <sup>(0.6)</sup>	15/15
SOO-Derbel	<b>1.3</b> <sup>(1)</sup>	<b>1.0</b> <sup>(1)</sup>	<b>1</b> <sup>(1)</sup>	<b>1.1</b> <sup>(0.5)</sup>	<b>0.76</b> <sup>(0.3)</sup>	15/15

Table 17: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>6.3e+1:1.5</i>	<i>2.5e+1:8.2</i>	<i>1.6e+1:10</i>	<i>1.0e+1:41</i>	<i>2.5e+0:208</i>	15/15
MATSUMOTO	<b>1.5</b> <sup>(1)</sup>	<b>1.8</b> <sup>(3)</sup>	<b>2.7</b> <sup>(4)</sup>	<b>1.3</b> <sup>(1.0)</sup>	<b>0.82</b> <sup>(0.7)</sup>	10/15
R-DE-10e2-	<b>2.1</b> <sup>(2)</sup>	<b>1.6</b> <sup>(1)</sup>	3.2 <sup>(4)</sup>	<b>1.8</b> <sup>(0.8)</sup>	<b>1.6</b> <sup>(2)</sup>	10/15
R-DE-10e5-	<b>2.1</b> <sup>(4)</sup>	<b>1.1</b> <sup>(0.5)</sup>	<b>1.3</b> <sup>(0.8)</sup>	<b>1.7</b> <sup>(2)</sup>	<b>2.7</b> <sup>(5)</sup>	15/15
RL-SHADE-1	<b>2.0</b> <sup>(0.8)</sup>	<b>1.9</b> <sup>(2)</sup>	3.1 <sup>(3)</sup>	<b>1.3</b> <sup>(2)</sup>	<b>1.0</b> <sup>(0.8)</sup>	12/15
RL-SHADE-1	<b>1.5</b> <sup>(0.7)</sup>	<b>1.3</b> <sup>(2)</sup>	<b>2.7</b> <sup>(3)</sup>	<b>1.9</b> <sup>(1)</sup>	<b>2.9</b> <sup>(3)</sup>	15/15
R-SHADE-10	<b>1.8</b> <sup>(2)</sup>	<b>1.4</b> <sup>(0.7)</sup>	<b>2.7</b> <sup>(4)</sup>	<b>0.98</b> <sup>(0.7)</sup>	<b>2.3</b> <sup>(2)</sup>	7/15
R-SHADE-10	<b>1.3</b> <sup>(0.7)</sup>	<b>1.3</b> <sup>(2)</sup>	<b>2.2</b> <sup>(3)</sup>	<b>1.0</b> <sup>(0.9)</sup>	<b>1.6</b> <sup>(3)</sup>	15/15
SOO-Derbel	<b>2.0</b> <sup>(2)</sup>	<b>1.2</b> <sup>(1)</sup>	<b>1.6</b> <sup>(0.8)</sup>	<b>0.91</b> <sup>(0.6)</sup>	<b>0.45</b> <sup>(0.3)</sup>	15/15

Table 18: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.6e+1</i> :1.8	<i>1.0e+1</i> :3.6	<i>6.3e+0</i> :14	<i>2.5e+0</i> :34	<i>2.5e-1</i> :189	5/5
MATSUMOTO	<b>2.4</b> (2)	<b>2.6</b> (4)	<b>1.1</b> (1)	<b>1.3</b> (0.4)	<b>2.8</b> (4)	4/15
R-DE-10e2-	<b>2.7</b> (3)	<b>2.2</b> (2)	<b>1.5</b> (2)	<b>1.6</b> (1)	<b>1.4</b> (2)	13/15
R-DE-10e5-	<b>1.6</b> (1)	<b>2.1</b> (1)	<b>1.1</b> (1)	<b>1.6</b> (1)	<b>1.4</b> (0.7)	15/15
RL-SHADE-1	<b>2.1</b> (2)	<b>2.5</b> (2)	<b>1.6</b> (2)	<b>1.6</b> (2)	3.5(5)	6/15
RL-SHADE-1	<b>2.6</b> (0.8)	<b>2.1</b> (2)	<b>0.90</b> (1)	3.6(3)	5.1(2)	15/15
R-SHADE-10	<b>2.4</b> (2)	<b>2.6</b> (2)	<b>1.6</b> (2)	<b>2.1</b> (0.8)	4.7(3)	5/15
R-SHADE-10	<b>1.9</b> (2)	<b>1.8</b> (1)	<b>0.98</b> (0.4)	<b>1.2</b> (0.8)	<b>1.1</b> (0.6)	15/15
SOO-Derbel	<b>0.67</b> (0)	<b>1.2</b> (1)	<b>0.72</b> (0.3)	<b>0.96</b> (0.7)	<b>0.98</b> (0.1)	15/15

Table 19: 03-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>6.3e+1:1.8</i>	<i>4.0e+1:4.8</i>	<i>2.5e+1:13</i>	<i>1.0e+1:40</i>	<i>6.3e-1:184</i>	15/15
MATSUMOTO	<b>3.0</b> (2)	<b>1.6</b> (0.9)	<b>1.2</b> (1)	<b>1.1</b> (0.4)	$\infty$ <i>150</i>	0/15
R-DE-10e2-	<b>1.3</b> (0.4)	<b>1.7</b> (1)	<b>1.2</b> (2)	<b>1.3</b> (1)	<b>2.4</b> (3)	9/15
R-DE-10e5-	<b>2.1</b> (3)	<b>2.1</b> (0.8)	<b>1.5</b> (1)	<b>1.3</b> (0.9)	21(0.5)	15/15
RL-SHADE-1	4.0(6)	<b>2.9</b> (3)	3.2(3)	<b>2.2</b> (1)	24(20)	1/15
RL-SHADE-1	3.1(3)	<b>2.4</b> (2)	<b>2.2</b> (3)	<b>2.9</b> (2)	6.7(0.8)	15/15
R-SHADE-10	3.9(6)	<b>1.9</b> (3)	<b>2.3</b> (2)	<b>2.4</b> (2)	24(12)	1/15
R-SHADE-10	3.1(3)	<b>1.9</b> (2)	<b>1.1</b> (0.9)	<b>1.2</b> (1)	<b>1.8</b> (0.4)	15/15
SOO-Derbel	<b>0.96</b> (1)	<b>1.2</b> (1)	<b>0.90</b> (0.5)	<b>0.97</b> (0.7)	<b>1.5</b> (0.8)	15/15

Table 20: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:81</i>	<i>1.0e-1:109</i>	<i>6.3e-2:109</i>	<i>4.0e-2:119</i>	<i>1.6e-2:1230</i>	15/15
MATSUMOTO	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
R-DE-10e2-	25(26)	39(75)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
R-DE-10e5-	<b>20</b> (25)	31(19)	54(67)	103(190)	20(14)	15/15
RL-SHADE-1	27(20)	41(49)	$\infty$	$\infty$	$\infty$ <i>300</i>	0/15
RL-SHADE-1	25(11)	25(20)	34(29)	64(61)	11(4)	15/15
R-SHADE-10	52(73)	38(55)	38(64)	<b>35</b> (31)	$\infty$ <i>300</i>	0/15
R-SHADE-10	24(30)	<b>24</b> (41)	<b>30</b> (19)	50(60)	<b>10</b> (28)	15/15
SOO-Derbel	<b>2.8</b> (2)	<b>2.8</b> (2)	<b>3.1</b> (4)	<b>4.4</b> (6)	<b>0.92</b> (0.7)	15/15

Table 21: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f20</b>	<i>4.0e+3:3.5</i>	<i>2.5e+3:4.3</i>	<i>4.0e+0:13</i>	<i>1.6e+0:41</i>	<i>1.0e+0:385</i>	5/5
MATSUMOTO	<b>1.1</b> <sub>(0.6)</sub>	<b>0.86</b> <sub>(0.6)</sub>	<b>1.5</b> <sub>(0.8)</sub>	17 <sub>(30)</sub>	<b>2.9</b> <sub>(3)</sub>	2/15
R-DE-10e2-	<b>1.8</b> <sub>(0.7)</sub>	<b>1.6</b> <sub>(2)</sub>	<b>2.9</b> <sub>(2)</sub>	3.4 <sub>(1)</sub>	<b>0.89</b> <sub>(1.0)</sub>	10/15
R-DE-10e5-	<b>1.3</b> <sub>(0.7)</sub>	<b>1.3</b> <sub>(0.8)</sub>	18 <sub>(2)</sub>	8.7 <sub>(40)</sub>	<b>2.7</b> <sub>(3)</sub>	15/15
RL-SHADE-1	<b>1.6</b> <sub>(1)</sub>	<b>1.5</b> <sub>(0.5)</sub>	<b>2.5</b> <sub>(2)</sub>	<b>3.2</b> <sub>(2)</sub>	<b>0.62</b> <sub>(0.5)</sub>	12/15
RL-SHADE-1	<b>1.2</b> <sub>(0.4)</sub>	<b>1.2</b> <sub>(0.8)</sub>	4.9 <sub>(3)</sub>	13 <sub>(7)</sub>	<b>2.7</b> <sub>(1)</sub>	15/15
R-SHADE-10	<b>1.6</b> <sub>(1)</sub>	<b>1.8</b> <sub>(2)</sub>	3.3 <sub>(2)</sub>	3.8 <sub>(1.0)</sub>	<b>1.3</b> <sub>(1)</sub>	8/15
R-SHADE-10	<b>1.6</b> <sub>(2)</sub>	<b>1.6</b> <sub>(2)</sub>	<b>2.8</b> <sub>(2)</sub>	6.0 <sub>(5)</sub>	<b>1.8</b> <sub>(2)</sub>	15/15
SOO-Derbel	<b>0.75</b> <sub>(0.1)</sub>	<b>0.61</b> <sub>(0.1)</sub>	3.8 <sub>(0.0)</sub>	<b>1.8</b> <sub>(6e-3)</sub>	<b>0.19</b> <sub>(1e-3)*2</sub>	15/15

Table 22: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><math>f_{21}</math></b>	<i>1.6e+1:2.5</i>	<i>1.0e+1:5.9</i>	<i>6.3e+0:14</i>	<i>2.5e+0:41</i>	<i>1.6e+0:167</i>	15/15
MATSUMOTO	<b>2.1</b> (2)	<b>1.6</b> (1)	<b>1.3</b> (0.8)	<b>0.70</b> (0.8)	<b>0.63</b> (0.4)	11/15
R-DE-10e2-	<b>1.4</b> (2)	<b>1.3</b> (0.9)	<b>1.3</b> (2)	<b>1.1</b> (1)	<b>1.1</b> (1)	12/15
R-DE-10e5-	<b>2.7</b> (4)	<b>1.8</b> (3)	<b>1.9</b> (2)	4.2(9)	4.1(8)	15/15
RL-SHADE-1	<b>2.3</b> (2)	<b>1.2</b> (2)	<b>1.1</b> (1)	<b>0.96</b> (1)	<b>1.3</b> (1)	12/15
RL-SHADE-1	<b>2.3</b> (2)	<b>1.3</b> (1)	<b>1.7</b> (3)	<b>1.8</b> (1)	<b>2.0</b> (2)	15/15
R-SHADE-10	<b>2.4</b> (1)	<b>2.6</b> (1)	<b>2.7</b> (2)	<b>2.3</b> (2)	<b>2.3</b> (3)	8/15
R-SHADE-10	<b>2.5</b> (3)	<b>1.4</b> (1)	<b>1.5</b> (1)	<b>1.5</b> (2)	<b>1.4</b> (3)	15/15
SOO-Derbel	<b>1.3</b> (2)	<b>1.3</b> (1)	<b>1.2</b> (0.4)	<b>0.90</b> (0.5)	<b>0.43</b> (0.7)	15/15

Table 23: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f22</b>	<i>4.0e+1:2.9</i>	<i>2.5e+1:5.2</i>	<i>1.0e+1:18</i>	<i>6.3e+0:33</i>	<i>1.0e+0:170</i>	5/5
MATSUMOTO	<b>2.1</b> (3)	<b>2.2</b> (2)	<b>1.4</b> (0.8)	<b>1.4</b> (2)	<b>1.5</b> (2)	7/15
R-DE-10e2-	<b>1.8</b> (0.9)	<b>1.7</b> (2)	<b>1.7</b> (3)	<b>1.9</b> (1)	<b>1.5</b> (0.9)	11/15
R-DE-10e5-	<b>2.1</b> (6)	<b>1.9</b> (1)	8.2(28)	5.6(30)	5.7(7)	15/15
RL-SHADE-1	<b>1.2</b> (0.5)	<b>1.4</b> (1)	<b>2.9</b> (4)	<b>2.3</b> (0.7)	<b>1.5</b> (1)	11/15
RL-SHADE-1	<b>1.3</b> (2)	<b>0.78</b> (0.4)	<b>2.0</b> (3)	<b>2.0</b> (2)	<b>2.4</b> (2)	15/15
R-SHADE-10	<b>1.8</b> (2)	<b>2.4</b> (3)	<b>2.2</b> (3)	<b>2.9</b> (4)	<b>1.6</b> (1)	10/15
R-SHADE-10	<b>1.3</b> (0.9)	<b>1.5</b> (0.7)	<b>0.87</b> (0.5)	<b>1.2</b> (1)	<b>1.9</b> (3)	15/15
SOO-Derbel	<b>1.0</b> (1)	<b>0.74</b> (0.6)	<b>0.71</b> (0.7)	<b>0.78</b> (0.8)	<b>0.47</b> (0.2)	15/15



Table 24: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>1.0e+1:2.6</i>	<i>6.3e+0:16</i>	<i>4.0e+0:44</i>	<i>2.5e+0:79</i>	<i>1.6e+0:198</i>	15/15
MATSUMOTO	4.3(2)	<b>1.5</b> (2)	<b>2.1</b> (2)	5.0(6)	$\infty$ 150	0/15
R-DE-10e2-	<b>3.1</b> (2)	<b>2.1</b> (3)	<b>1.8</b> (2)	3.4(3)	7.0(4)	3/15
R-DE-10e5-	4.6(3)	<b>2.5</b> (2)	<b>1.9</b> (2)	<b>2.8</b> (1)	6.8(6)	15/15
RL-SHADE-1	3.4(4)	<b>0.90</b> (0.6)	<b>1.3</b> (4)	3.6(3)	7.2(8)	3/15
RL-SHADE-1	3.3(2)	<b>1.5</b> (2)	<b>2.0</b> (2)	<b>2.9</b> (2)	7.9(6)	15/15
R-SHADE-10	4.1(4)	3.6(5)	<b>2.8</b> (2)	5.3(6)	6.9(9)	3/15
R-SHADE-10	<b>2.8</b> (3)	<b>1.7</b> (0.8)	<b>1.5</b> (2)	3.3(2)	<b>3.0</b> (3)	15/15
SOO-Derbel	4.4(6)	<b>1.8</b> (3)	<b>2.2</b> (2)	<b>2.8</b> (2)	<b>1.8</b> (1.0)	15/15

Table 25: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f</i>24</b>	<i>4.0e+1:4.6</i>	<i>2.5e+1:13</i>	<i>1.6e+1:47</i>	<i>1.6e+1:47</i>	<i>6.9e+0:382</i>	15/15
MATSUMOTO	<b>1.6</b> (1)	<b>1.9</b> (2)	<b>1.7</b> (1)	<b>1.7</b> (4)	5.8(5)	1/15
R-DE-10e2-	<b>1.9</b> (0.7)	<b>2.2</b> (2)	<b>1.8</b> (1)	<b>1.8</b> (0.7)	<b>2.4</b> (2)	4/15
R-DE-10e5-	<b>1.1</b> (1)	<b>1.6</b> (0.9)	<b>2.7</b> (4)	<b>2.7</b> (4)	4.4(7)	15/15
RL-SHADE-1	<b>1.6</b> (2)	<b>2.2</b> (1)	<b>1.3</b> (0.4)	<b>1.3</b> (0.5)	<b>2.6</b> (3)	4/15
RL-SHADE-1	<b>1.2</b> (0.5)	<b>1.8</b> (2)	<b>2.0</b> (1)	<b>2.0</b> (1.0)	3.1(3)	15/15
R-SHADE-10	<b>1.0</b> (0.6)	<b>1.5</b> (2)	<b>1.5</b> (2)	<b>1.5</b> (2)	5.4(4)	2/15
R-SHADE-10	<b>1.7</b> (1)	<b>1.9</b> (2)	<b>1.5</b> (0.9)	<b>1.5</b> (0.9)	<b>1.1</b> (0.9)	15/15
SOO-Derbel	<b>1.4</b> (2)	<b>1.4</b> (1)	<b>2.1</b> (0.7)	<b>2.1</b> (3)	<b>1.4</b> (1)	15/15

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