

# Comparison Tables: BBOB 2015 Function Testbed with BBOB 2009 as Reference (Expensive Setting)

The BBOBies

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## Abstract

This document provides tabular results of the workshop on Black-Box Optimization Benchmarking held at GECCO 2015 with a focus on benchmarking black-box algorithms for small function evaluation budgets (expensive setting), see <http://coco.gforge.inria.fr/doku.php?id=bbob-2015>. Overall, 18 algorithms have been tested on 24 benchmark functions in dimensions between 2 and 20. Only three of them have been tested on the optional instances in dimension 40. A description of the used objective functions can be found in [7, 5]. The experimental set-up is described in [6].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [2]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise ( $\text{ERT}_{\text{best}}$  is noted as infinite). See [6] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed at GECCO 2015.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
BSifeg		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
BSif		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
BSqi		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
BSrr		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
CMA-CSA		Benchmarking IPOP-CMA-ES-TPA and IPOP-CMA-ES-MSR on the BBOB Noiseless Testbed	[1]
CMA-MSR		Benchmarking IPOP-CMA-ES-TPA and IPOP-CMA-ES-MSR on the BBOB Noiseless Testbed	[1]
CMA-TPA		Benchmarking IPOP-CMA-ES-TPA and IPOP-CMA-ES-MSR on the BBOB Noiseless Testbed	[1]
GP1-CMAES		SBenchmarking Gaussian Processes and Random Forests Surrogate Models on the BBOB Noiseless Testbed	[3]
GP5-CMAES		Benchmarking Gaussian Processes and Random Forests Surrogate Models on the BBOB Noiseless Testbed	[3]
IPOPCMAv3p61		Benchmarking Gaussian Processes and Random Forests Surrogate Models on the BBOB Noiseless Testbed	[3]
LHD-10xDefault-MATSuMoT		The Impact of Initial Designs on the Performance of MATSuMoTo on the Noiseless BBOB-2015 Testbed: A Preliminary Study	[4]
LHD-2xDefault-MATSuMoTo		The Impact of Initial Designs on the Performance of MATSuMoTo on the Noiseless BBOB-2015 Testbed: A Preliminary Study	[4]
RAND-2xDefault-MATSuMoTo		The Impact of Initial Designs on the Performance of MATSuMoTo on the Noiseless BBOB-2015 Testbed: A Preliminary Study	[4]
RF1-CMAES		Benchmarking Gaussian Processes and Random Forests Surrogate Models on the BBOB Noiseless Testbed	[3]
RF5-CMAES		Benchmarking Gaussian Processes and Random Forests Surrogate Models on the BBOB Noiseless Testbed	[3]
Sifeg		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
Sif		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]
Srr		Dimension Selection in Axis-Parallel Brent-STEP Method for Black-Box Optimization of Separable Continuous Functions	[9]

Table 2: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>1.6e+1</i> :1.2	<i>4.0e+0</i> :2.6	<i>2.5e-2</i> :6.2	<i>1.0e-8</i> :6.2	<i>1.0e-8</i> :6.2	15/15
BSifeg	<b>1.6</b> (1)	<b>2.2</b> (2)	<b>1.7</b> (0.2)	<b>1.7</b> (0.2)	<b>1.7</b> (0.3)	15/15
BSif	<b>1.6</b> (1)	<b>2.2</b> (2)	<b>1.7</b> (0.2)	<b>1.7</b> (0.3)	<b>1.7</b> (0.2)	15/15
BSqi	<b>1.6</b> (2)	<b>2.2</b> (2)	<b>1.7</b> (0.3)	<b>1.7</b> (0.2)	<b>1.7</b> (0.3)	15/15
BSrr	<b>1.6</b> (2)	<b>2.2</b> (2)	<b>1.7</b> (0.3)	<b>1.7</b> (0.2)	<b>1.7</b> (0.3)	15/15
CMA-CSA	3.1(5)	3.0(3)	11(6)	42(5)	42(6)	15/15
CMA-MSR	<b>2.7</b> (1)	4.7(3)	16(11)	69(12)	69(9)	15/15
CMA-TPA	<b>2.8</b> (4)	4.5(4)	12(7)	44(8)	44(13)	15/15
GP1-CMAES	<b>2.4</b> (5)	<b>2.5</b> (2)	6.5(2)	24(4)	24(5)	15/15
GP5-CMAES	3.3(3)	<b>2.7</b> (2)	3.4(2)	31(14)	31(16)	15/15
IPOPCMAv3p	4.9(4)	4.6(5)	12(7)	43(9)	43(4)	15/15
LHD-10xDef	<b>2.6</b> (2)	3.8(5)	10(0)	$\infty$	$\infty$ 100	0/15
LHD-2xDefa	<b>2.4</b> (1)	<b>2.8</b> (2)	3.3(0.8)	$\infty$	$\infty$ 100	0/15
RAND-2xDef	<b>2.6</b> (2)	3.4(2)	3.5(0.9)	$\infty$	$\infty$ 100	0/15
RF1-CMAES	3.1(4)	4.2(4)	8.0(3)	86(85)	86(111)	10/15
RF5-CMAES	<b>2.8</b> (3)	4.7(4)	60(38)	$\infty$	$\infty$ 502	0/15
Sifeg	<b>1.6</b> (1)	<b>2.2</b> (2)	<b>2.3</b> (0.4)	6.3(0.5)	6.3(0.5)	15/15
Sif	<b>1.6</b> (1)	<b>2.2</b> (1)	<b>2.4</b> (0.3)	6.2(0.6)	6.2(0.6)	15/15
Srr	<b>1.6</b> (1)	<b>2.2</b> (2)	<b>2.3</b> (0.2)	5.9(0.5)	5.9(0.5)	15/15

Table 3: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>1.0e+7:1.4</i>	<i>1.6e+6:2.7</i>	<i>1.0e+5:6.1</i>	<i>6.3e-1:20</i>	<i>1.0e-8:30</i>	15/15
BSifeg	<b>1.7</b> (1)	3.1(1)	<b>1.7</b> (0.2)	<b>1.2</b> (0.3)	<b>1.2</b> (0.3)	15/15
BSif	<b>1.7</b> (1)	3.1(0.4)	<b>1.7</b> (0.2)	<b>1.1</b> (0.3)	<b>1.2</b> (0.1)	15/15
BSqi	<b>1.7</b> (1)	3.1(0.9)	<b>1.7</b> (0.2)	<b>0.93</b> (0.1)	<b>1.1</b> (0.2)	15/15
BSrr	<b>1.7</b> (1)	3.1(0)	<b>1.7</b> (0.3)	<b>1.1</b> (0.3)	<b>1.3</b> (0.2)	15/15
CMA-CSA	<b>1.3</b> (2)	<b>2.8</b> (3)	3.2(2)	15(4)	19(2)	15/15
CMA-MSR	<b>1.8</b> (0.5)	<b>2.6</b> (2)	<b>2.8</b> (2)	16(3)	24(5)	15/15
CMA-TPA	<b>1.5</b> (1)	<b>1.2</b> (0.5)	<b>1.7</b> (1)	12(5)	17(2)	15/15
GP1-CMAES	<b>2.1</b> (2)	<b>2.3</b> (2)	<b>2.2</b> (2)	13(6)	19(2)	12/15
GP5-CMAES	<b>2.2</b> (2)	<b>2.2</b> (2)	<b>1.5</b> (1)	5.1(2)	9.2(6)	14/15
IPOPCMAv3p	<b>2.3</b> (2)	<b>3.0</b> (2)	3.0(2)	17(6)	$\infty$ 506	0/15
LHD-10xDef	<b>1.3</b> (1)	<b>1.4</b> (0.8)	<b>2.6</b> (1)	$\infty$	$\infty$ 100	0/15
LHD-2xDefa	<b>1.0</b> (0.7)	<b>1.2</b> (1)	<b>1.7</b> (1)	$\infty$	$\infty$ 100	0/15
RAND-2xDef	<b>1.3</b> (2)	<b>1.0</b> (0.7)	<b>1.3</b> (1)	$\infty$	$\infty$ 100	0/15
RF1-CMAES	<b>2.5</b> (3)	<b>2.2</b> (2)	<b>2.8</b> (3)	168(242)	$\infty$ 506	0/15
RF5-CMAES	<b>1.8</b> (1)	<b>2.8</b> (2)	<b>2.8</b> (2)	167(194)	$\infty$ 502	0/15
Sifeg	<b>1.7</b> (1)	3.2(2)	<b>2.0</b> (0.3)	<b>1.5</b> (0.3)	<b>1.8</b> (0.2)	15/15
Sif	<b>1.7</b> (1)	3.2(1)	<b>2.0</b> (0.5)	<b>1.4</b> (0.3)	<b>1.7</b> (0.3)	15/15
Srr	<b>1.7</b> (1)	3.2(0.4)	<b>2.0</b> (0.5)	<b>1.4</b> (0.2)	<b>1.9</b> (0.1)	15/15

Table 4: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>1.0e+2</i> :1.4	<i>4.0e+1</i> :4.1	<i>2.5e+1</i> :6.6	<i>6.3e+0</i> :26	<i>2.5e+0</i> :112	15/15
BSifeg	<b>2.2</b> (1)	<b>1.8</b> (1)	<b>1.4</b> (0.3)	<b>0.79</b> (0.6)	<b>0.30</b> (0.2)	15/15
BSif	<b>2.2</b> (1)	<b>1.8</b> (0.7)	<b>1.4</b> (0.7)	<b>0.77</b> (0.3)	<b>0.30</b> (0.2)	15/15
BSqi	<b>2.2</b> (1)	<b>1.8</b> (1)	<b>1.4</b> (0.5)	<b>0.76</b> (0.5)	<b>0.30</b> (0.2)	15/15
BSrr	<b>2.2</b> (0.7)	<b>1.8</b> (1)	<b>1.4</b> (0.6)	<b>0.74</b> (0.6)	<b>0.28</b> (0.2)	15/15
CMA-CSA	<b>1.8</b> (1)	<b>2.4</b> (2)	<b>2.4</b> (2)	<b>2.2</b> (1)	<b>2.9</b> (4)	15/15
CMA-MSR	3.0(3)	<b>2.9</b> (1)	<b>2.6</b> (1)	3.3(2)	4.6(9)	15/15
CMA-TPA	<b>2.0</b> (3)	<b>2.9</b> (3)	<b>2.9</b> (2)	6.8(8)	5.5(4)	15/15
GP1-CMAES	<b>2.8</b> (3)	<b>1.7</b> (2)	<b>2.6</b> (2)	<b>2.2</b> (1)	<b>2.9</b> (4)	11/15
GP5-CMAES	<b>2.0</b> (1)	<b>1.9</b> (2)	4.0(1)	5.8(7)	<b>2.3</b> (2)	13/15
IPOPCMAv3p	<b>1.6</b> (0.9)	<b>1.4</b> (1.0)	<b>1.6</b> (0.8)	<b>2.6</b> (1)	3.2(2)	10/15
LHD-10xDef	<b>1.9</b> (3)	<b>1.6</b> (2)	<b>1.7</b> (1)	3.0(2)	<b>1.5</b> (0.8)	8/15
LHD-2xDefa	<b>1.6</b> (0.4)	<b>1.2</b> (1)	<b>1.4</b> (1)	<b>1.0</b> (0.7)	<b>0.67</b> (0.8)	11/15
RAND-2xDef	<b>1.8</b> (2)	<b>1.1</b> (0.7)	<b>1.9</b> (1)	<b>2.4</b> (1)	<b>1.4</b> (2)	7/15
RF1-CMAES	<b>1.7</b> (2)	11(1)	7.2(2)	9.0(6)	5.6(6)	7/15
RF5-CMAES	<b>2.2</b> (3)	<b>2.4</b> (2)	14(2)	15(15)	6.5(8)	7/15
Sifeg	<b>2.2</b> (2)	<b>1.8</b> (1)	<b>1.5</b> (0.9)	<b>1.1</b> (0.5)	<b>0.30</b> (0.2)	15/15
Sif	<b>2.2</b> (2)	<b>1.8</b> (1)	<b>1.5</b> (0.7)	<b>1.1</b> (0.5)	<b>0.34</b> (0.2)	15/15
Srr	<b>2.2</b> (1)	<b>1.8</b> (1)	<b>1.5</b> (1)	<b>1.1</b> (0.4)	<b>0.31</b> (0.1)	15/15

Table 5: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>6.3e+1:2.4</i>	<i>4.0e+1:5.2</i>	<i>2.5e+1:8.5</i>	<i>1.0e+1:22</i>	<i>2.5e+0:120</i>	5/5
BSifeg	<b>1.8</b> (1)	<b>1.1</b> (0.9)	<b>1.1</b> (0.3)	<b>0.91</b> (0.4)	<b>0.42</b> (0.3)	15/15
BSif	<b>1.8</b> (2)	<b>1.1</b> (0.8)	<b>1.1</b> (0.5)	<b>0.91</b> (0.6)	<b>0.42</b> (0.3)	15/15
BSqi	<b>1.8</b> (2)	<b>1.1</b> (0.9)	<b>1.1</b> (0.5)	<b>0.98</b> (0.4)	<b>0.45</b> (0.3)	15/15
BSrr	<b>1.8</b> (2)	<b>1.1</b> (1.0)	<b>1.1</b> (0.6)	<b>0.93</b> (0.4)	<b>0.42</b> (0.3)	15/15
CMA-CSA	<b>1.9</b> (2)	<b>2.3</b> (2)	<b>2.4</b> (1)	<b>2.3</b> (2)	4.3(7)	15/15
CMA-MSR	3.2(2)	<b>2.6</b> (2)	<b>2.3</b> (2)	6.1(20)	11(13)	15/15
CMA-TPA	3.3(4)	<b>1.9</b> (0.7)	<b>2.5</b> (2)	<b>2.9</b> (4)	6.4(9)	15/15
GP1-CMAES	<b>2.5</b> (2)	<b>1.9</b> (2)	<b>2.3</b> (2)	<b>2.2</b> (1)	4.6(3)	8/15
GP5-CMAES	3.2(3)	<b>2.1</b> (3)	10(15)	6.4(3)	3.8(3)	9/15
IPOPCMAv3p	<b>2.9</b> (3)	<b>2.2</b> (2)	<b>2.8</b> (3)	<b>2.9</b> (3)	5.0(10)	8/15
LHD-10xDef	<b>1.7</b> (4)	<b>1.7</b> (1)	<b>2.0</b> (3)	<b>2.7</b> (3)	<b>1.9</b> (2)	6/15
LHD-2xDefa	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>2.0</b> (1)	<b>1.8</b> (1)	<b>1.7</b> (1)	6/15
RAND-2xDef	<b>2.2</b> (1)	<b>1.6</b> (0.8)	<b>1.2</b> (0.8)	<b>1.7</b> (2)	<b>2.1</b> (1.0)	5/15
RF1-CMAES	<b>2.1</b> (2)	<b>2.3</b> (3)	<b>2.1</b> (2)	3.3(3)	28(27)	2/15
RF5-CMAES	17(2)	8.6(1)	12(16)	16(22)	28(26)	2/15
Sifeg	<b>1.8</b> (1)	<b>1.2</b> (1.0)	<b>1.3</b> (0.2)	<b>0.96</b> (0.3)	<b>0.50</b> (0.3)	15/15
Sif	<b>1.8</b> (2)	<b>1.2</b> (1)	<b>1.3</b> (0.9)	<b>0.95</b> (0.1)	<b>0.52</b> (0.3)	15/15
Srr	<b>1.8</b> (2)	<b>1.2</b> (1)	<b>1.2</b> (0.3)	<b>0.96</b> (0.6)	<b>0.51</b> (0.1)	15/15

Table 6: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><math>f_5</math></b>	<i>4.0e+1</i> :1.4	<i>1.6e+1</i> :3.5	<i>1.0e-8</i> :4.4	<i>1.0e-8</i> :4.4	<i>1.0e-8</i> :4.4	15/15
BSifeg	<b>2.9</b> (1)	<b>1.8</b> (0.1)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
BSif	<b>2.9</b> (2)	<b>1.8</b> (0.1)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
BSqi	<b>2.9</b> (2)	<b>1.8</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.1)	15/15
BSrr	<b>2.9</b> (2)	<b>1.8</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
CMA-CSA	4.2(4)	<b>3.0</b> (3)	4.8(3)	4.8(4)	4.8(3)	15/15
CMA-MSR	4.0(5)	<b>2.9</b> (2)	6.2(3)	6.2(2)	6.2(2)	15/15
CMA-TPA	3.3(4)	<b>2.0</b> (2)	4.0(1)	4.0(1)	4.0(2)	15/15
GP1-CMAES	3.5(4)	<b>2.2</b> (1)	9.3(9)	9.3(14)	9.3(12)	15/15
GP5-CMAES	<b>2.6</b> (4)	<b>1.9</b> (0.9)	4.4(2)	4.4(3)	4.4(2)	15/15
IPOPCMAv3p	5.0(3)	4.1(4)	13(8)	13(9)	13(16)	15/15
LHD-10xDef	<b>2.6</b> (2)	<b>2.2</b> (2)	14(0.6)	14(0.3)	14(0.6)	15/15
LHD-2xDefa	<b>1.4</b> (0.7)	<b>2.0</b> (1)	3.3(0.6)	3.3(0.6)	3.3(0.6)	15/15
RAND-2xDef	<b>1.4</b> (0.7)	<b>1.9</b> (2)	3.6(0.6)	3.6(0.6)	3.6(0.9)	15/15
RF1-CMAES	<b>2.4</b> (3)	<b>1.9</b> (2)	22(26)	22(32)	22(26)	15/15
RF5-CMAES	3.7(5)	3.2(3)	61(75)	61(34)	61(76)	12/15
Sifeg	<b>2.9</b> (2)	<b>1.8</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
Sif	<b>2.9</b> (2)	<b>1.8</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
Srr	<b>2.9</b> (2)	<b>1.8</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15

Table 7: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>6.3e+4</i> :1.4	<i>1.0e+2</i> :2.8	<i>1.6e+1</i> :10	<i>1.0e+0</i> :23	<i>2.5e-6</i> :103	15/15
BSifeg	<b>1.3</b> (1)	<b>2.0</b> (3)	245(513)	416(421)	2668(4813)	1/15
BSif	<b>1.3</b> (1)	<b>2.1</b> (3)	307(617)	442(1192)	$\infty$ 2e4	0/15
BSqi	<b>1.3</b> (1)	<b>2.0</b> (1)	355(776)	344(686)	2671(5134)	1/15
BSrr	<b>1.3</b> (1)	<b>2.0</b> (1)	341(56)	403(547)	1293(1193)	2/15
CMA-CSA	<b>1.6</b> (2)	3.6(5)	3.1(2)	<b>4.3</b> (4)	<b>4.2</b> (0.8)	15/15
CMA-MSR	<b>1.8</b> (2)	<b>2.3</b> (3)	<b>2.4</b> (1)	5.3(3)	5.2(0.8)	15/15
CMA-TPA	<b>1.3</b> (0.4)	<b>1.2</b> (1)	<b>1.2</b> (2)	<b>3.6</b> (3)	<b>3.8</b> (0.7)	15/15
GP1-CMAES	<b>2.4</b> (3)	3.1(5)	<b>2.8</b> (2)	4.9(0.7)	$\infty$ 506	0/15
GP5-CMAES	<b>1.1</b> (0.4)	<b>2.3</b> (7)	<b>2.3</b> (2)	9.2(15)	$\infty$ 506	0/15
IPOPCMAv3p	<b>1.5</b> (2)	<b>2.7</b> (2)	<b>2.6</b> (5)	<b>4.6</b> (2)	<b>4.8</b> (4)	13/15
LHD-10xDef	<b>1.3</b> (1)	<b>1.5</b> (2)	<b>1.3</b> (1)	9.0(12)	$\infty$ 100	0/15
LHD-2xDefa	<b>1.1</b> (0)	<b>1.9</b> (2)	<b>1.5</b> (0.9)	12(16)	$\infty$ 100	0/15
RAND-2xDef	<b>1.4</b> (0.7)	<b>1.9</b> (2)	<b>1.2</b> (0.7)	6.3(8)	$\infty$ 100	0/15
RF1-CMAES	<b>1.8</b> (0.7)	<b>2.3</b> (2)	5.5(14)	67(146)	$\infty$ 506	0/15
RF5-CMAES	<b>1.5</b> (0.9)	3.2(5)	4.8(6)	40(35)	$\infty$ 508	0/15
Sifeg	<b>1.3</b> (1)	<b>2.3</b> (4)	333(47)	271(534)	2624(3800)	1/15
Sif	<b>1.3</b> (1)	<b>2.3</b> (4)	355(1172)	318(750)	2659(2915)	1/15
Srr	<b>1.3</b> (1)	<b>2.1</b> (3)	319(1229)	242(376)	1251(1158)	2/15



Table 8: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f7</i></b>	<i>4.0e+2</i> :1.6	<i>1.0e+1</i> :3.2	<i>2.5e+0</i> :14	<i>1.6e+0</i> :21	<i>1.6e-2</i> :188	15/15
BSifeg	<b>1.3</b> <sub>(0.5)</sub>	<b>1.7</b> <sub>(1)</sub>	135 <sub>(216)</sub>	376 <sub>(318)</sub>	698 <sub>(696)</sub>	2/15
BSif	<b>1.3</b> <sub>(0.6)</sub>	<b>1.7</b> <sub>(1)</sub>	173 <sub>(395)</sub>	376 <sub>(1149)</sub>	252 <sub>(216)</sub>	5/15
BSqi	<b>1.3</b> <sub>(1)</sub>	<b>1.7</b> <sub>(1)</sub>	206 <sub>(466)</sub>	256 <sub>(513)</sub>	355 <sub>(565)</sub>	4/15
BSrr	<b>1.3</b> <sub>(1)</sub>	<b>1.7</b> <sub>(1)</sub>	268 <sub>(467)</sub>	543 <sub>(2200)</sub>	331 <sub>(424)</sub>	4/15
CMA-CSA	<b>1.3</b> <sub>(0.6)</sub>	4.0 <sub>(3)</sub>	3.6 <sub>(2)</sub>	3.5 <sub>(10)</sub>	<b>1.1</b> <sub>(1)</sub>	15/15
CMA-MSR	<b>1.7</b> <sub>(2)</sub>	4.4 <sub>(5)</sub>	<b>2.0</b> <sub>(3)</sub>	<b>1.6</b> <sub>(2)</sub>	<b>1.0</b> <sub>(0.3)</sub>	15/15
CMA-TPA	<b>1.1</b> <sub>(0.3)</sub>	3.7 <sub>(3)</sub>	<b>2.5</b> <sub>(2)</sub>	<b>1.9</b> <sub>(2)</sub>	<b>0.80</b> <sub>(0.8)</sub>	15/15
GP1-CMAES	<b>1.4</b> <sub>(1)</sub>	4.2 <sub>(1)</sub>	<b>2.1</b> <sub>(0.9)</sub>	<b>1.9</b> <sub>(2)</sub>	<b>1.0</b> <sub>(0.4)</sub>	14/15
GP5-CMAES	<b>0.67</b> <sub>(0.2)</sub>	3.3 <sub>(3)</sub>	<b>2.0</b> <sub>(3)</sub>	<b>2.0</b> <sub>(3)</sub>	<b>0.98</b> <sub>(0.3)</sub>	14/15
IPOPCMAv3p	<b>1.9</b> <sub>(0.9)</sub>	3.9 <sub>(8)</sub>	<b>2.5</b> <sub>(3)</sub>	3.6 <sub>(4)</sub>	<b>1.7</b> <sub>(1)</sub>	13/15
LHD-10xDef	<b>1.2</b> <sub>(1)</sub>	7.6 <sub>(5)</sub>	<b>3.0</b> <sub>(2)</sub>	<b>2.6</b> <sub>(2)</sub>	$\infty$ 100	0/15
LHD-2xDefa	<b>1</b> <sub>(0.3)</sub>	3.0 <sub>(2)</sub>	<b>1.2</b> <sub>(0.9)</sub>	<b>1.0</b> <sub>(0.8)</sub>	<b>1.3</b> <sub>(1)</sub>	5/15
RAND-2xDef	<b>1.7</b> <sub>(1)</sub>	3.8 <sub>(1)</sub>	<b>1.2</b> <sub>(0.4)</sub>	<b>1.2</b> <sub>(1)</sub>	<b>1.1</b> <sub>(2)</sub>	6/15
RF1-CMAES	<b>1.5</b> <sub>(1)</sub>	4.1 <sub>(1)</sub>	<b>2.0</b> <sub>(2)</sub>	<b>2.7</b> <sub>(2)</sub>	<b>2.2</b> <sub>(2)</sub>	11/15
RF5-CMAES	<b>1.6</b> <sub>(2)</sub>	3.8 <sub>(4)</sub>	<b>2.5</b> <sub>(2)</sub>	3.5 <sub>(2)</sub>	13 <sub>(15)</sub>	3/15
Sifeg	<b>1.3</b> <sub>(0.3)</sub>	<b>1.8</b> <sub>(2)</sub>	68 <sub>(180)</sub>	256 <sub>(954)</sub>	444 <sub>(405)</sub>	3/15
Sif	<b>1.3</b> <sub>(0.9)</sub>	<b>1.8</b> <sub>(2)</sub>	78 <sub>(36)</sub>	204 <sub>(440)</sub>	485 <sub>(501)</sub>	3/15
Srr	<b>1.3</b> <sub>(0.6)</sub>	<b>1.8</b> <sub>(1)</sub>	135 <sub>(144)</sub>	287 <sub>(367)</sub>	473 <sub>(349)</sub>	3/15

Table 9: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>2.5e+3</i> :1.2	<i>1.0e+2</i> :3.2	<i>6.3e+0</i> :7.0	<i>1.6e-1</i> :27	<i>1.6e-6</i> :100	15/15
BSifeg	<b>1.9</b> (3)	<b>1.9</b> (1)	4.0(3)	2208(3277)	$\infty$ 2e4	0/15
BSif	<b>1.9</b> (0.4)	<b>1.9</b> (1)	4.2(8)	2303(3150)	$\infty$ 2e4	0/15
BSqi	<b>1.9</b> (2)	<b>1.9</b> (1)	4.1(8)	1323(2706)	$\infty$ 2e4	0/15
BSrr	<b>1.9</b> (2)	<b>1.9</b> (1)	4.9(5)	2159(3507)	$\infty$ 2e4	0/15
CMA-CSA	3.5(2)	3.8(3)	8.4(6)	12(11)	<b>5.9</b> (3)	15/15
CMA-MSR	<b>2.1</b> (0.6)	<b>1.7</b> (0.9)	7.3(3)	10(8)	<b>5.8</b> (2)	15/15
CMA-TPA	5.2(2)	4.6(3)	4.8(4)	<b>6.9</b> (4)	<b>4.0</b> (0.9)	15/15
GP1-CMAES	<b>2.2</b> (2)	<b>2.6</b> (5)	5.0(2)	9.1(6)	10(6)	7/15
GP5-CMAES	<b>2.6</b> (2)	<b>2.6</b> (2)	<b>3.8</b> (6)	11(20)	6.6(6)	9/15
IPOPCMAv3p	3.6(3)	4.0(5)	5.1(4)	<b>7.8</b> (12)	8.7(12)	8/15
LHD-10xDef	<b>2.4</b> (2)	3.9(8)	6.0(5)	13(12)	$\infty$ 100	0/15
LHD-2xDefa	<b>1.6</b> (2)	<b>2.4</b> (2)	<b>3.0</b> (2)	<b>5.1</b> (2)	$\infty$ 100	0/15
RAND-2xDef	<b>2.4</b> (2)	3.5(1)	<b>3.2</b> (1)	10(6)	$\infty$ 100	0/15
RF1-CMAES	3.2(3)	3.1(2)	9.1(19)	17(10)	$\infty$ 506	0/15
RF5-CMAES	3.1(3)	22(82)	39(55)	78(92)	$\infty$ 506	0/15
Sifeg	<b>1.9</b> (2)	<b>2.0</b> (2)	4.1(6)	933(701)	$\infty$ 2e4	0/15
Sif	<b>1.9</b> (3)	<b>2.0</b> (0.6)	4.3(5)	975(1446)	$\infty$ 2e4	0/15
Srr	<b>1.9</b> (2)	<b>2.0</b> (1)	3.8(0.4)	1348(1373)	$\infty$ 2e4	0/15

Table 10: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>6.3e+0:13</i>	<i>4.0e+0:15</i>	<i>2.5e+0:15</i>	<i>2.5e-1:21</i>	<i>1.0e-8:94</i>	15/15
BSifeg	15(24)	14(12)	14(17)	210(120)	$\infty$ 2e4	0/15
BSif	13(10)	12(19)	12(13)	193(218)	$\infty$ 2e4	0/15
BSqi	13(14)	12(19)	12(13)	207(294)	$\infty$ 2e4	0/15
BSrr	12(17)	12(20)	14(20)	241(104)	$\infty$ 2e4	0/15
CMA-CSA	<b>2.7</b> (1)	3.5(1)	4.1(5)	8.7(9)	<b>6.0</b> (3)	15/15
CMA-MSR	<b>2.4</b> (2)	<b>2.4</b> (2)	4.6(2)	10(14)	7.0(3)	15/15
CMA-TPA	<b>2.5</b> (2)	3.3(4)	4.6(7)	9.3(7)	<b>6.0</b> (2)	15/15
GP1-CMAES	<b>2.8</b> (2)	4.1(5)	6.8(17)	15(22)	26(44)	3/15
GP5-CMAES	<b>1.7</b> (1)	<b>1.5</b> (0.2)	<b>2.0</b> (2)	<b>6.0</b> (3)	<b>5.8</b> (6)	10/15
IPOPCMAv3p	<b>2.3</b> (2)	<b>2.2</b> (2)	<b>2.5</b> (2)	6.1(5)	11(10)	7/15
LHD-10xDefa	<b>2.8</b> (2)	3.4(2)	3.8(3)	16(15)	$\infty$ 100	0/15
LHD-2xDefa	<b>1.3</b> (0.7)	<b>1.2</b> (0.8)	<b>1.9</b> (1)	<b>4.6</b> (3)	$\infty$ 100	0/15
RAND-2xDef	<b>1.6</b> (1)	<b>1.6</b> (1)	<b>2.0</b> (0.9)	<b>6.0</b> (5)	$\infty$ 100	0/15
RF1-CMAES	4.8(3)	6.6(35)	11(10)	26(40)	$\infty$ 506	0/15
RF5-CMAES	21(28)	20(19)	21(31)	57(61)	$\infty$ 504	0/15
Sifeg	<b>2.6</b> (3)	<b>2.8</b> (2)	4.0(5)	182(348)	$\infty$ 2e4	0/15
Sif	<b>2.5</b> (3)	5.0(3)	5.8(4)	259(407)	$\infty$ 2e4	0/15
Srr	<b>2.5</b> (3)	<b>2.8</b> (2)	3.6(3)	232(223)	$\infty$ 2e4	0/15

Table 11: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>1.6e+6</i> :2.0	<i>4.0e+5</i> :3.2	<i>6.3e+2</i> :8.8	<i>1.0e+1</i> :30	<i>2.5e-8</i> :101	15/15
BSifeg	<b>2.7</b> (2)	<b>2.5</b> (0.2)	<b>1.5</b> (0.5)	38(59)	$\infty$ <i>5883</i>	0/15
BSif	<b>2.7</b> (2)	<b>2.5</b> (0.7)	<b>1.5</b> (0.5)	71(116)	$\infty$ <i>8444</i>	0/15
BSqi	<b>2.7</b> (2)	<b>2.5</b> (2)	<b>1.5</b> (0.5)	135(10)	$\infty$ <i>1e4</i>	0/15
BSrr	<b>2.7</b> (2)	<b>2.5</b> (0.2)	<b>1.5</b> (0.5)	46(108)	$\infty$ <i>6681</i>	0/15
CMA-CSA	3.7(4)	3.3(4)	7.2(3)	7.5(4)	<b>5.3</b> (0.9)	15/15
CMA-MSR	<b>2.1</b> (2)	<b>2.3</b> (2)	7.0(5)	7.4(4)	6.8(0.6)	15/15
CMA-TPA	3.4(4)	<b>2.8</b> (3)	5.9(5)	<b>6.3</b> (3)	5.3(1)	15/15
GP1-CMAES	<b>1.5</b> (2)	<b>1.5</b> (0.5)	4.4(3)	<b>4.6</b> (3)	<b>5.2</b> (2)	12/15
GP5-CMAES	<b>2.2</b> (2)	<b>2.2</b> (2)	<b>2.2</b> (0.9)	<b>1.6</b> (0.6)	<b>2.5</b> (0.9)	14/15
IPOPCMAv3p	<b>2.6</b> (3)	<b>2.7</b> (2)	6.8(3)	8.3(7)	$\infty$ <i>506</i>	0/15
LHD-10xDef	<b>1.7</b> (1)	<b>1.6</b> (2)	7.9(1)	16(9)	$\infty$ <i>100</i>	0/15
LHD-2xDefa	<b>1.7</b> (2)	<b>2.2</b> (1)	3.8(2)	6.9(7)	$\infty$ <i>100</i>	0/15
RAND-2xDef	<b>2.7</b> (3)	<b>2.7</b> (2)	3.9(1)	10(9)	$\infty$ <i>100</i>	0/15
RF1-CMAES	<b>2.3</b> (3)	<b>2.2</b> (2)	4.2(1)	19(25)	$\infty$ <i>506</i>	0/15
RF5-CMAES	3.4(2)	<b>2.9</b> (2)	8.7(6)	14(18)	$\infty$ <i>502</i>	0/15
Sifeg	<b>2.7</b> (2)	<b>2.8</b> (1)	<b>1.9</b> (0.3)	8.6(12)	$\infty$ <i>2159</i>	0/15
Sif	<b>2.7</b> (2)	<b>2.8</b> (2)	<b>1.9</b> (0.4)	12(17)	$\infty$ <i>2178</i>	0/15
Srr	<b>2.7</b> (2)	<b>2.8</b> (1)	<b>1.9</b> (0.3)	7.9(0.1)	$\infty$ <i>2193</i>	0/15

Table 12: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>1.0e+7:1.1</i>	<i>1.6e+6:3.2</i>	<i>1.0e+4:6.6</i>	<i>4.0e+1:23</i>	<i>4.0e-8:100</i>	15/15
BSifeg	<b>1.2</b> (0)	<b>1.6</b> (1)	<b>1.4</b> (0.3)	47(49)	$\infty$ <i>6926</i>	0/15
BSif	<b>1.2</b> (0.5)	<b>1.6</b> (1)	<b>1.4</b> (0.3)	39(23)	$\infty$ <i>5430</i>	0/15
BSqi	<b>1.2</b> (0)	<b>1.6</b> (1)	<b>1.4</b> (0.3)	71(92)	$\infty$ <i>5998</i>	0/15
BSrr	<b>1.2</b> (0.5)	<b>1.6</b> (1)	<b>1.4</b> (0.6)	40(109)	$\infty$ <i>6000</i>	0/15
CMA-CSA	<b>1.6</b> (0.2)	<b>1.3</b> (1)	3.5(3)	4.7(5)	<b>5.2</b> (0.8)	15/15
CMA-MSR	<b>1.1</b> (0.9)	<b>0.96</b> (1)	3.8(5)	5.3(0.8)	6.6(0.6)	15/15
CMA-TPA	<b>1.9</b> (2)	<b>1.5</b> (1)	4.2(3)	6.0(3)	5.3(0.4)	15/15
GP1-CMAES	<b>2.2</b> (4)	<b>1.6</b> (2)	3.4(3)	<b>3.6</b> (3)	<b>4.7</b> (0.8)	14/15
GP5-CMAES	3.6(4)	<b>1.8</b> (2)	<b>2.2</b> (0.9)	<b>1.3</b> (0.4)	<b>2.4</b> (0.7)	15/15
IPOPCMAv3p	3.1(2)	<b>1.9</b> (1)	3.7(1)	4.3(2)	$\infty$ <i>506</i>	0/15
LHD-10xDef	<b>1.5</b> (0.7)	<b>1.3</b> (0.8)	4.9(5)	11(7)	$\infty$ <i>100</i>	0/15
LHD-2xDefa	<b>1.7</b> (1)	<b>1.3</b> (0.9)	<b>2.5</b> (1)	5.6(8)	$\infty$ <i>100</i>	0/15
RAND-2xDef	<b>1.8</b> (1)	<b>1.2</b> (1)	<b>2.7</b> (2)	<b>3.0</b> (0.5)	$\infty$ <i>100</i>	0/15
RF1-CMAES	<b>2.7</b> (4)	<b>2.9</b> (5)	4.9(4)	5.5(7)	$\infty$ <i>506</i>	0/15
RF5-CMAES	<b>1.7</b> (0.9)	<b>2.2</b> (3)	3.8(3)	6.4(12)	$\infty$ <i>508</i>	0/15
Sifeg	<b>1.2</b> (1)	<b>1.7</b> (1)	<b>1.7</b> (1.0)	10(6)	$\infty$ <i>2391</i>	0/15
Sif	<b>1.2</b> (1)	<b>1.7</b> (1)	<b>1.7</b> (0.6)	10(29)	$\infty$ <i>2405</i>	0/15
Srr	<b>1.2</b> (0.5)	<b>1.7</b> (1)	<b>1.7</b> (0.8)	11(11)	$\infty$ <i>2357</i>	0/15

Table 13: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>2.5e+8</i> :1.3	<i>6.3e+6</i> :2.7	<i>6.3e+5</i> :6.3	<i>4.0e+1</i> :21	<i>1.6e-3</i> :101	15/15
BSifeg	<b>0.85</b> (0.4)	<b>1.2</b> (1)	<b>1.3</b> (0.8)	12(28)	295(517)	5/15
BSif	<b>0.85</b> (0.4)	<b>1.2</b> (1)	<b>1.3</b> (1.0)	29(3)	368(224)	4/15
BSqi	<b>0.85</b> (0.2)	<b>1.2</b> (1)	<b>1.3</b> (0.5)	23(5)	320(351)	4/15
BSrr	<b>0.85</b> (0.2)	<b>1.2</b> (1)	<b>1.3</b> (0.9)	19(0.4)	326(335)	4/15
CMA-CSA	<b>1.4</b> (2)	<b>1.9</b> (3)	<b>1.4</b> (2)	6.5(5)	<b>8.5</b> (17)	15/15
CMA-MSR	<b>1.3</b> (0.8)	<b>1.3</b> (0.7)	<b>0.87</b> (0.8)	9.1(7)	9.3(5)	15/15
CMA-TPA	<b>1.4</b> (2)	<b>1.8</b> (2)	<b>1.8</b> (2)	7.0(7)	<b>6.8</b> (9)	15/15
GP1-CMAES	<b>2.0</b> (6)	<b>1.5</b> (2)	<b>1.2</b> (1)	3.6(1.0)	10(9)	7/15
GP5-CMAES	<b>1.2</b> (2)	<b>1.6</b> (1)	<b>1.3</b> (2)	<b>3.5</b> (6)	<b>7.8</b> (5)	7/15
IPOPCMAv3p	<b>1.7</b> (3)	<b>1.8</b> (1)	<b>1.7</b> (2)	4.0(1)	14(26)	5/15
LHD-10xDef	<b>0.90</b> (0.4)	<b>1.2</b> (0.7)	<b>0.97</b> (1)	24(19)	$\infty$ 100	0/15
LHD-2xDefa	1(0.2)	<b>0.78</b> (0.6)	<b>0.97</b> (0.9)	5.0(4)	$\infty$ 100	0/15
RAND-2xDef	<b>1.1</b> (0.4)	<b>0.95</b> (0.7)	<b>1.1</b> (0.8)	6.3(11)	$\infty$ 100	0/15
RF1-CMAES	<b>1.6</b> (4)	<b>1.5</b> (2)	<b>1.4</b> (0.8)	4.8(3)	$\infty$ 506	0/15
RF5-CMAES	<b>1.2</b> (0.2)	<b>1.9</b> (3)	<b>1.9</b> (2)	11(6)	$\infty$ 504	0/15
Sifeg	<b>0.85</b> (0)	<b>1.2</b> (1)	<b>1.3</b> (1)	<b>2.8</b> (6)	76(138)	5/15
Sif	<b>0.85</b> (0)	<b>1.2</b> (1)	<b>1.4</b> (0.6)	4.9(14)	83(92)	5/15
Srr	<b>0.85</b> (0.4)	<b>1.2</b> (1)	<b>1.4</b> (1)	<b>3.4</b> (1)	124(113)	4/15

Table 14: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>4.0e+2</i> :1.6	<i>2.5e+2</i> :3.1	<i>6.3e+1</i> :8.7	<i>1.0e+1</i> :23	<i>4.0e-6</i> :100	15/15
BSifeg	<b>2.3</b> (2)	<b>1.6</b> (1)	184(1215)	541(602)	$\infty$ <i>2e4</i>	0/15
BSif	<b>2.3</b> (2)	<b>1.6</b> (1)	224(780)	789(712)	$\infty$ <i>2e4</i>	0/15
BSqi	<b>2.3</b> (2)	<b>1.6</b> (1)	252(879)	430(542)	$\infty$ <i>2e4</i>	0/15
BSrr	<b>2.3</b> (2)	<b>1.6</b> (1)	184(0.7)	491(498)	$\infty$ <i>2e4</i>	0/15
CMA-CSA	<b>2.5</b> (2)	<b>2.1</b> (1)	<b>2.8</b> (3)	<b>2.9</b> (3)	<b>5.0</b> (0.5)	15/15
CMA-MSR	<b>2.8</b> (5)	<b>2.1</b> (2)	4.1(4)	3.7(1)	<b>6.2</b> (1)	15/15
CMA-TPA	<b>2.8</b> (3)	<b>2.5</b> (2)	3.5(5)	4.5(3)	<b>5.3</b> (0.6)	15/15
GP1-CMAES	<b>1.6</b> (2)	1.4(1)	<b>1.9</b> (2)	<b>2.7</b> (2)	24(20)	3/15
GP5-CMAES	<b>2.4</b> (3)	<b>1.9</b> (3)	5.5(1)	3.8(2)	11(4)	6/15
IPOPCMAv3p	<b>2.2</b> (3)	<b>1.8</b> (2)	<b>2.6</b> (2)	3.9(2)	$\infty$ <i>506</i>	0/15
LHD-10xDefa	<b>2.0</b> (1)	<b>2.2</b> (2)	<b>2.8</b> (2)	<b>2.9</b> (1)	$\infty$ <i>100</i>	0/15
LHD-2xDefa	<b>1.7</b> (2)	<b>1.5</b> (0.6)	<b>1.4</b> (0.7)	<b>1.4</b> (0.8)	$\infty$ <i>100</i>	0/15
RAND-2xDef	<b>1.6</b> (1)	<b>1.8</b> (2)	<b>1.7</b> (0.8)	<b>1.4</b> (0.8)	$\infty$ <i>100</i>	0/15
RF1-CMAES	<b>2.1</b> (0.9)	<b>1.8</b> (3)	<b>2.2</b> (2)	7.9(7)	$\infty$ <i>506</i>	0/15
RF5-CMAES	<b>2.6</b> (2)	<b>2.1</b> (1)	<b>1.9</b> (3)	11(33)	$\infty$ <i>508</i>	0/15
Sifeg	<b>2.3</b> (2)	<b>1.6</b> (1)	178(899)	563(826)	$\infty$ <i>2e4</i>	0/15
Sif	<b>2.3</b> (2)	<b>1.6</b> (1)	258(1006)	410(561)	$\infty$ <i>2e4</i>	0/15
Srr	<b>2.3</b> (2)	<b>1.6</b> (1.0)	278(884)	428(499)	$\infty$ <i>2e4</i>	0/15

Table 15: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>1.6e+1:1.4</i>	<i>2.5e+0:4.2</i>	<i>1.0e+0:7.4</i>	<i>2.5e-2:21</i>	<i>1.0e-8:101</i>	15/15
BSifeg	<b>2.0</b> (3)	12(11)	8.5(20)	7.3(22)	$\infty$ <i>2e4</i>	0/15
BSif	<b>2.0</b> (3)	12(20)	8.7(11)	6.8(12)	$\infty$ <i>2e4</i>	0/15
BSqi	<b>2.0</b> (3)	7.4(15)	5.7(7)	4.2(4)	$\infty$ <i>2e4</i>	0/15
BSrr	<b>2.0</b> (2)	11(24)	8.4(13)	6.2(6)	$\infty$ <i>2e4</i>	0/15
CMA-CSA	<b>1.3</b> (0.7)	<b>1.7</b> (1)	<b>1.9</b> (2)	4.1(2)	<b>5.5</b> (0.9)	15/15
CMA-MSR	<b>2.1</b> (2)	<b>2.4</b> (1.0)	<b>2.8</b> (2)	6.0(2)	<b>6.5</b> (0.7)	15/15
CMA-TPA	<b>2.4</b> (1)	3.5(4)	3.5(2)	5.8(2)	<b>5.8</b> (0.8)	15/15
GP1-CMAES	<b>0.95</b> (1)	<b>2.2</b> (0.6)	<b>1.9</b> (2)	<b>2.5</b> (0.7)	$\infty$ <i>506</i>	0/15
GP5-CMAES	<b>1.9</b> (3)	<b>2.9</b> (2)	<b>2.3</b> (1)	<b>1.7</b> (0.8)	$\infty$ <i>506</i>	0/15
IPOPCMAv3p	<b>1.2</b> (0.7)	3.3(2)	3.1(2)	3.8(1)	$\infty$ <i>506</i>	0/15
LHD-10xDef	<b>1.4</b> (0.7)	<b>1.2</b> (1)	3.1(3)	8.2(9)	$\infty$ <i>100</i>	0/15
LHD-2xDefa	<b>1.4</b> (0.9)	<b>1.6</b> (2)	<b>1.4</b> (1)	<b>2.0</b> (1)	$\infty$ <i>100</i>	0/15
RAND-2xDef	<b>1.1</b> (1)	<b>2.2</b> (1)	<b>1.9</b> (1)	<b>2.1</b> (0.9)	$\infty$ <i>100</i>	0/15
RF1-CMAES	<b>1.4</b> (2)	5.9(6)	6.3(9)	8.8(9)	$\infty$ <i>506</i>	0/15
RF5-CMAES	<b>1.2</b> (0.9)	44(46)	48(59)	79(74)	$\infty$ <i>506</i>	0/15
Sifeg	<b>2.0</b> (1)	<b>2.8</b> (1)	<b>2.3</b> (1)	3.2(5)	$\infty$ <i>2e4</i>	0/15
Sif	<b>2.0</b> (2)	<b>2.8</b> (3)	<b>2.4</b> (0.7)	4.1(4)	$\infty$ <i>2e4</i>	0/15
Srr	<b>2.0</b> (1)	<b>2.6</b> (2)	<b>2.1</b> (0.7)	<b>2.1</b> (3)	$\infty$ <i>2e4</i>	0/15



Table 16: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>1.6e+2</i> :1.2	<i>4.0e+1</i> :4.7	<i>2.5e+1</i> :10	<i>1.0e+1</i> :37	<i>2.5e+0</i> :118	5/5
BSifeg	<b>1.4</b> (0.4)	<b>1.8</b> (1.0)	<b>2.2</b> (0.8)	27(5)	111(252)	10/15
BSif	<b>1.4</b> (1)	151(561)	70(257)	22(140)	118(120)	10/15
BSqi	<b>1.4</b> (2)	3.3(0.9)	4.0(9)	3.3(4)	62(119)	13/15
BSrr	<b>1.4</b> (0.4)	6.5(39)	6.4(0.1)	4.2(11)	59(91)	13/15
CMA-CSA	<b>1.3</b> (0)	<b>1.0</b> (1)	<b>1.1</b> (1)	<b>1.1</b> (0.5)	<b>1.6</b> (3)	15/15
CMA-MSR	<b>2.1</b> (0.8)	<b>1.3</b> (2)	<b>1.3</b> (2)	<b>0.86</b> (0.5)	<b>2.2</b> (0.6)	15/15
CMA-TPA	<b>1.8</b> (2)	<b>2.2</b> (5)	<b>1.5</b> (0.7)	<b>1.5</b> (1)	3.6(5)	15/15
GP1-CMAES	<b>2.3</b> (5)	<b>1.6</b> (1)	<b>1.3</b> (1.0)	<b>1.3</b> (1)	3.1(3)	10/15
GP5-CMAES	<b>2.4</b> (2)	<b>2.1</b> (2)	<b>1.3</b> (0.4)	<b>0.75</b> (0.3)	<b>1.6</b> (3)	14/15
IPOPCMAv3p	<b>1.4</b> (0.4)	<b>2.0</b> (2)	<b>1.4</b> (0.5)	<b>1.3</b> (1)	4.8(5)	8/15
LHD-10xDef	<b>2.5</b> (2)	<b>1.8</b> (2)	<b>1.6</b> (2)	<b>2.2</b> (1)	<b>3.0</b> (2)	4/15
LHD-2xDefa	<b>1.4</b> (1)	<b>0.81</b> (1)	<b>0.94</b> (0.7)	<b>0.90</b> (0.8)	<b>1.4</b> (2)	7/15
RAND-2xDef	<b>2.1</b> (0.8)	<b>1.6</b> (2)	<b>1.1</b> (0.8)	<b>1.4</b> (1.0)	<b>1.4</b> (2)	7/15
RF1-CMAES	3.2(6)	<b>1.8</b> (0.8)	<b>1.5</b> (1)	<b>1.9</b> (0.7)	<b>1.8</b> (2)	12/15
RF5-CMAES	<b>2.0</b> (1)	<b>1.8</b> (1)	<b>1.9</b> (3)	6.1(1)	8.0(6)	6/15
Sifeg	<b>1.4</b> (2)	<b>1.5</b> (2)	<b>1.8</b> (0.7)	<b>1.7</b> (3)	50(103)	12/15
Sif	<b>1.4</b> (1)	<b>1.5</b> (2)	<b>1.9</b> (3)	<b>1.7</b> (0.4)	33(42)	13/15
Srr	<b>1.4</b> (1)	<b>1.5</b> (1)	<b>1.5</b> (0.5)	<b>1.6</b> (3)	35(46)	15/15

Table 17: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>1.0e+2</i> :1.1	<i>2.5e+1</i> :3.9	<i>1.6e+1</i> :6.5	<i>4.0e+0</i> :31	<i>2.5e-1</i> :127	5/5
BSifeg	<b>1.8</b> (1)	<b>2.9</b> (5)	<b>2.7</b> (3)	<b>1.0</b> (0.8)	12(29)	15/15
BSif	<b>1.8</b> (0.9)	<b>2.9</b> (2)	<b>2.9</b> (2)	<b>1.1</b> (1)	7.0(12)	15/15
BSqi	<b>1.8</b> (3)	3.9(1)	<b>2.9</b> (5)	<b>1.1</b> (0.9)	17(14)	15/15
BSrr	<b>1.8</b> (3)	3.4(1)	3.8(4)	<b>1.2</b> (1)	20(54)	15/15
CMA-CSA	<b>1.8</b> (2)	3.3(3)	4.1(3)	6.1(9)	3.6(4)	15/15
CMA-MSR	<b>1.5</b> (0.9)	<b>1.9</b> (3)	<b>2.3</b> (2)	6.7(0.9)	8.1(7)	15/15
CMA-TPA	<b>1.8</b> (2)	<b>1.6</b> (2)	<b>2.1</b> (2)	3.7(7)	<b>3.0</b> (4)	15/15
GP1-CMAES	<b>1.5</b> (0.7)	<b>1.8</b> (0.6)	<b>1.5</b> (1)	<b>2.3</b> (1)	4.6(7)	8/15
GP5-CMAES	<b>1.6</b> (2)	<b>2.3</b> (2)	<b>2.4</b> (2)	11(15)	6.6(10)	7/15
IPOPCMAv3p	<b>1.2</b> (0.4)	<b>1.6</b> (1)	<b>1.7</b> (2)	<b>1.2</b> (0.9)	<b>2.5</b> (4)	11/15
LHD-10xDef	<b>1.5</b> (0.9)	<b>1.8</b> (0.8)	<b>1.5</b> (1)	<b>1.5</b> (1)	5.8(6)	2/15
LHD-2xDefa	<b>1.5</b> (0.9)	<b>1.7</b> (3)	<b>2.0</b> (2)	<b>1.4</b> (1)	<b>2.6</b> (3)	4/15
RAND-2xDef	<b>1.2</b> (0.4)	<b>1.7</b> (2)	<b>1.5</b> (2)	<b>1.0</b> (1)	<b>1.1</b> (1.0)	8/15
RF1-CMAES	<b>1.8</b> (2)	<b>1.7</b> (1)	<b>1.7</b> (3)	3.6(5)	5.3(4)	7/15
RF5-CMAES	<b>1.1</b> (0)	<b>1.3</b> (1.0)	<b>1.7</b> (2)	6.1(8)	6.4(9)	6/15
Sifeg	<b>1.8</b> (3)	<b>2.4</b> (2)	<b>2.1</b> (0.7)	<b>0.94</b> (0.6)	7.4(0.8)	15/15
Sif	<b>1.8</b> (3)	<b>2.4</b> (2)	<b>2.0</b> (1)	<b>0.89</b> (0.2)	14(42)	15/15
Srr	<b>1.8</b> (3)	<b>2.3</b> (2)	<b>2.0</b> (1)	<b>0.91</b> (0.4)	12(29)	15/15

Table 18: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>4.0e+1</i> :1.2	<i>1.0e+1</i> :2.7	<i>4.0e+0</i> :10	<i>2.5e+0</i> :28	<i>1.6e-1</i> :119	5/5
BSifeg	<b>1.2</b> (1)	<b>2.2</b> (2)	<b>1.9</b> (2)	6.6(22)	41(41)	14/15
BSif	<b>1.2</b> (1)	<b>2.2</b> (2)	<b>2.1</b> (3)	11(21)	40(48)	15/15
BSqi	<b>1.2</b> (0.8)	<b>2.2</b> (2)	<b>1.9</b> (2)	32(0.8)	21(28)	15/15
BSrr	<b>1.2</b> (0.6)	<b>2.2</b> (2)	<b>1.9</b> (2)	21(0.7)	40(57)	15/15
CMA-CSA	<b>1.3</b> (0.6)	3.1(10)	9.3(14)	3.5(11)	<b>2.1</b> (2)	15/15
CMA-MSR	<b>1.7</b> (1)	20(59)	12(20)	5.8(1)	3.5(3)	15/15
CMA-TPA	<b>1.4</b> (0.8)	3.6(6)	3.3(6)	<b>1.4</b> (1)	<b>2.2</b> (0.3)	15/15
GP1-CMAES	<b>2.2</b> (3)	3.8(9)	6.6(26)	4.1(10)	4.7(8)	8/15
GP5-CMAES	<b>1.4</b> (0.6)	7.6(7)	17(29)	8.8(12)	5.7(4)	7/15
IPOPCMAv3p	<b>1.2</b> (0.4)	<b>2.5</b> (2)	<b>1.8</b> (2)	<b>2.2</b> (0.4)	<b>2.3</b> (3)	12/15
LHD-10xDefa	<b>1.4</b> (0.6)	<b>1.8</b> (2)	<b>1.8</b> (2)	<b>1.6</b> (1.0)	4.1(5)	3/15
LHD-2xDefa	<b>1.2</b> (0.8)	<b>1.5</b> (2)	<b>1.5</b> (1)	<b>0.77</b> (0.6)	3.9(6)	3/15
RAND-2xDef	<b>1.5</b> (0.6)	<b>1.9</b> (2)	<b>1.8</b> (1)	<b>0.79</b> (0.3)	<b>2.6</b> (4)	4/15
RF1-CMAES	<b>1.3</b> (1)	<b>2.6</b> (4)	5.6(1)	<b>2.3</b> (0.7)	7.2(10)	6/15
RF5-CMAES	<b>1.4</b> (0)	50(50)	29(35)	16(15)	61(86)	1/15
Sifeg	<b>1.2</b> (0.6)	<b>2.2</b> (2)	<b>1.5</b> (2)	<b>1.4</b> (2)	6.8(5)	15/15
Sif	<b>1.2</b> (0)	<b>2.2</b> (1)	<b>1.6</b> (2)	6.4(1)	8.5(11)	15/15
Srr	<b>1.2</b> (0.2)	<b>2.2</b> (2)	<b>1.4</b> (2)	<b>1.9</b> (4)	3.6(5)	15/15

Table 19: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>4.0e+2:1.2</i>	<i>1.0e+2:3.2</i>	<i>4.0e+1:7.2</i>	<i>6.3e+0:32</i>	<i>1.6e+0:104</i>	5/5
BSifeg	<b>1.2</b> (0)	<b>1.2</b> (1)	<b>1.0</b> (0.6)	10(2)	133(112)	10/15
BSif	<b>1.2</b> (1)	<b>1.2</b> (1)	<b>1.0</b> (0.7)	12(45)	126(193)	10/15
BSqi	<b>1.2</b> (0.6)	<b>1.2</b> (0.9)	<b>1.0</b> (0.6)	16(37)	119(162)	10/15
BSrr	<b>1.2</b> (0.6)	<b>1.2</b> (1)	<b>1.0</b> (0.5)	13(0.4)	98(172)	12/15
CMA-CSA	1(0.4)	<b>2.0</b> (4)	<b>1.8</b> (2)	<b>2.7</b> (6)	3.5(3)	15/15
CMA-MSR	<b>1.3</b> (1)	<b>1.8</b> (1)	<b>1.6</b> (2)	6.1(6)	6.2(6)	15/15
CMA-TPA	<b>0.94</b> (0)	<b>1.5</b> (0.5)	<b>1.2</b> (0.3)	<b>1.2</b> (1)	<b>3.0</b> (3)	15/15
GP1-CMAES	<b>2.7</b> (3)	<b>2.2</b> (2)	4.2(9)	<b>2.0</b> (5)	4.3(4)	9/15
GP5-CMAES	14(0.6)	26(1)	17(53)	9.5(16)	6.5(10)	8/15
IPOPCMAv3p	<b>2.4</b> (8)	<b>1.9</b> (0.6)	<b>1.7</b> (0.8)	<b>1.1</b> (0.9)	<b>2.7</b> (10)	11/15
LHD-10xDef	<b>1.2</b> (1)	<b>1.1</b> (1)	<b>1.2</b> (0.8)	<b>1.8</b> (1)	<b>2.3</b> (2)	6/15
LHD-2xDefa	<b>1.3</b> (1)	<b>1.3</b> (0.7)	<b>0.80</b> (0.5)	<b>1.0</b> (0.9)	<b>1.1</b> (0.9)	9/15
RAND-2xDef	<b>1.2</b> (0.8)	<b>1.1</b> (1)	<b>0.79</b> (0.8)	<b>0.96</b> (0.6)	<b>1.7</b> (2)	7/15
RF1-CMAES	<b>1.2</b> (0.8)	<b>1.9</b> (2)	<b>1.1</b> (1)	<b>1.3</b> (0.6)	8.0(2)	6/15
RF5-CMAES	<b>1.6</b> (2)	3.9(8)	6.4(2)	5.0(12)	9.0(15)	6/15
Sifeg	<b>1.2</b> (0.6)	<b>1.1</b> (0.8)	<b>1.0</b> (0.7)	24(2)	52(98)	14/15
Sif	<b>1.2</b> (1)	<b>1.1</b> (1)	<b>1.0</b> (0.8)	19(1)	119(97)	11/15
Srr	<b>1.2</b> (1)	<b>1.1</b> (0.8)	<b>1.0</b> (0.7)	40(255)	129(97)	10/15

Table 20: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:23</i>	<i>1.0e-1:26</i>	<i>6.3e-2:38</i>	<i>4.0e-2:40</i>	<i>1.0e-2:216</i>	15/15
BSifeg	<b>4.0</b> (3)	<b>4.0</b> (3)	<b>2.8</b> (2)	<b>3.7</b> (4)	15(10)	15/15
BSif	4.2(3)	4.2(4)	<b>3.0</b> (3)	<b>3.7</b> (3)	33(77)	12/15
BSqi	<b>3.6</b> (2)	<b>3.7</b> (2)	<b>2.6</b> (2)	4.2(5)	35(31)	14/15
BSrr	<b>3.5</b> (2)	<b>3.6</b> (2)	<b>2.6</b> (3)	<b>3.7</b> (4)	28(58)	13/15
CMA-CSA	13(4)	21(45)	18(20)	26(22)	13(8)	15/15
CMA-MSR	8.0(11)	12(10)	16(23)	26(43)	13(14)	15/15
CMA-TPA	7.0(3)	6.2(6)	14(15)	18(23)	<b>6.2</b> (8)	15/15
GP1-CMAES	8.8(9)	11(15)	12(15)	12(17)	16(21)	2/15
GP5-CMAES	12(11)	17(20)	13(13)	15(14)	16(9)	2/15
IPOPCMAv3p	7.9(8)	14(24)	11(16)	12(8)	34(37)	1/15
LHD-10xDef	8.9(12)	18(15)	38(99)	36(28)	<b>6.9</b> (11)	1/15
LHD-2xDefa	7.5(7)	8.3(18)	12(18)	37(45)	$\infty$ 100	0/15
RAND-2xDef	5.6(6)	16(17)	11(13)	11(15)	<b>6.6</b> (13)	1/15
RF1-CMAES	17(34)	19(11)	17(17)	28(27)	10(4)	3/15
RF5-CMAES	12(31)	12(10)	15(17)	20(40)	$\infty$ 504	0/15
Sifeg	7.3(2)	6.8(6)	6.5(6)	7.2(5)	31(22)	14/15
Sif	6.5(5)	6.2(4)	6.7(5)	7.6(4)	25(22)	15/15
Srr	5.0(3)	5.1(4)	5.1(3)	6.3(4)	28(57)	14/15

Table 21: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f20</b>	<i>4.0e+3</i> :1.9	<i>2.5e+2</i> :2.8	<i>4.0e+0</i> :6.3	<i>2.5e+0</i> :21	<i>6.3e-1</i> :139	15/15
BSifeg	<b>2.1</b> (2)	14(4)	17(32)	10(22)	28(47)	15/15
BSif	<b>2.1</b> (2)	13(3)	19(32)	8.0(3)	62(71)	12/15
BSqi	<b>2.1</b> (2)	12(1)	19(24)	8.1(14)	16(40)	15/15
BSrr	<b>2.1</b> (2)	14(5)	16(1)	8.3(9)	18(17)	15/15
CMA-CSA	<b>2.4</b> (1)	<b>3.0</b> (3)	<b>2.4</b> (2)	<b>1.6</b> (2)	<b>6.0</b> (7)	15/15
CMA-MSR	<b>1.7</b> (2)	<b>1.9</b> (2)	<b>2.6</b> (4)	<b>2.2</b> (0.9)	13(19)	15/15
CMA-TPA	3.2(3)	4.2(2)	4.0(5)	<b>2.1</b> (2)	11(13)	15/15
GP1-CMAES	<b>1.9</b> (3)	<b>2.3</b> (2)	<b>1.6</b> (0.9)	<b>1.6</b> (0.8)	<b>4.3</b> (4)	8/15
GP5-CMAES	<b>2.0</b> (3)	<b>2.0</b> (1)	<b>2.2</b> (2)	<b>2.0</b> (0.3)	8.1(8)	5/15
IPOPCMAv3p	<b>2.3</b> (2)	<b>2.5</b> (3)	<b>2.3</b> (3)	<b>1.5</b> (2)	16(21)	3/15
LHD-10xDefa	<b>1.8</b> (2)	4.0(3)	3.3(2)	<b>2.1</b> (2)	<b>5.1</b> (4)	2/15
LHD-2xDefa	<b>1.8</b> (2)	<b>2.0</b> (1)	<b>2.1</b> (0.8)	<b>1.7</b> (2)	11(14)	1/15
RAND-2xDef	<b>1.3</b> (0.7)	<b>2.8</b> (2)	<b>2.5</b> (1)	<b>1.9</b> (0.4)	11(10)	1/15
RF1-CMAES	<b>2.1</b> (2)	<b>2.7</b> (3)	3.2(4)	3.5(2)	16(11)	3/15
RF5-CMAES	<b>2.6</b> (3)	21(8)	27(23)	12(18)	26(33)	2/15
Sifeg	<b>2.1</b> (1)	3.6(3)	3.6(0.9)	<b>1.8</b> (2)	17(12)	15/15
Sif	<b>2.1</b> (2)	3.7(2)	3.7(4)	<b>1.9</b> (1)	20(28)	15/15
Srr	<b>2.1</b> (2)	3.5(3)	3.0(2)	<b>1.8</b> (2)	16(71)	15/15

Table 22: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f21</b>	<i>1.0e+1:1.7</i>	<i>6.3e+0:2.6</i>	<i>2.5e+0:7.9</i>	<i>1.6e+0:30</i>	<i>4.0e-1:105</i>	15/15
BSifeg	<b>2.1</b> (1)	<b>3.0</b> (2)	3.0(6)	<b>2.2</b> (4)	42(163)	13/15
BSif	<b>2.1</b> (2)	<b>2.9</b> (2)	<b>3.0</b> (2)	<b>2.9</b> (5)	62(180)	12/15
BSqi	<b>2.1</b> (1)	<b>2.5</b> (2)	3.4(8)	<b>2.4</b> (4)	53(124)	13/15
BSrr	<b>2.1</b> (2)	<b>2.9</b> (2)	3.4(4)	<b>2.3</b> (4)	62(61)	12/15
CMA-CSA	<b>1.5</b> (1)	<b>2.4</b> (4)	5.2(13)	4.0(14)	4.5(8)	15/15
CMA-MSR	<b>1.9</b> (1)	<b>2.6</b> (1)	<b>1.7</b> (2)	12(35)	156(985)	14/15
CMA-TPA	<b>1.5</b> (2)	<b>2.7</b> (4)	<b>2.5</b> (2)	5.2(12)	37(165)	15/15
GP1-CMAES	<b>1.8</b> (2)	<b>2.1</b> (1)	<b>1.6</b> (2)	10(12)	6.2(14)	7/15
GP5-CMAES	<b>1.5</b> (0.6)	<b>2.5</b> (2)	3.8(1)	6.4(6)	8.9(8)	6/15
IPOPCMAv3p	<b>1.6</b> (0.9)	<b>2.0</b> (3)	<b>1.9</b> (0.9)	3.4(6)	3.7(9)	9/15
LHD-10xDef	<b>1.4</b> (2)	<b>1.8</b> (2)	<b>1.2</b> (2)	<b>1.2</b> (1)	<b>0.74</b> (0.7)	12/15
LHD-2xDefa	<b>1.4</b> (2)	<b>1.7</b> (2)	<b>1.3</b> (0.8)	<b>0.75</b> (0.5)	<b>0.45</b> (0.5)	14/15
RAND-2xDef	<b>1.5</b> (0.9)	<b>2.8</b> (3)	<b>1.5</b> (0.9)	<b>0.90</b> (0.6)	<b>0.49</b> (0.2)	14/15
RF1-CMAES	<b>1.2</b> (0.6)	<b>3.0</b> (4)	7.5(32)	13(26)	20(37)	3/15
RF5-CMAES	<b>1.7</b> (2)	<b>2.1</b> (3)	<b>1.2</b> (0.9)	4.4(4)	11(6)	5/15
Sifeg	<b>2.1</b> (1)	<b>2.3</b> (2)	<b>1.3</b> (0.7)	32(2)	88(96)	12/15
Sif	<b>2.1</b> (1)	<b>2.3</b> (2)	<b>1.3</b> (0.7)	49(4)	98(79)	11/15
Srr	<b>2.1</b> (1)	<b>2.3</b> (2)	<b>1.3</b> (0.8)	21(1)	107(79)	11/15

Table 23: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f22</b>	<i>4.0e+1:1.3</i>	<i>1.6e+1:3.2</i>	<i>6.3e+0:9.3</i>	<i>1.6e+0:25</i>	<i>1.0e-1:168</i>	15/15
BSifeg	<b>1.9</b> (3)	<b>1.9</b> (2)	3.9(2)	18(12)	94(77)	9/15
BSif	<b>1.9</b> (3)	<b>1.9</b> (2)	3.6(7)	37(107)	80(115)	10/15
BSqi	<b>1.9</b> (2)	<b>1.9</b> (2)	4.8(5)	14(5)	91(161)	9/15
BSrr	<b>1.9</b> (2)	<b>1.9</b> (2)	5.5(9)	26(38)	85(90)	10/15
CMA-CSA	<b>1.8</b> (2)	<b>1.9</b> (3)	5.6(2)	17(34)	14(5)	15/15
CMA-MSR	<b>1.9</b> (2)	<b>2.2</b> (3)	7.3(22)	22(11)	18(52)	15/15
CMA-TPA	<b>1.7</b> (1)	<b>1.4</b> (1)	<b>1.9</b> (2)	14(24)	7.6(5)	15/15
GP1-CMAES	<b>1.3</b> (0.4)	<b>1.1</b> (1)	10(14)	6.1(15)	6.8(8)	5/15
GP5-CMAES	<b>1.6</b> (2)	<b>1.4</b> (1)	3.6(14)	4.1(6)	<b>2.1</b> (2)	11/15
IPOPCMAv3p	<b>1.7</b> (0.8)	<b>1.3</b> (1)	<b>2.3</b> (4)	4.8(16)	4.2(6)	7/15
LHD-10xDef	<b>1.3</b> (1.0)	<b>1.2</b> (0.9)	<b>1.3</b> (1)	<b>1.8</b> (1)	<b>0.81</b> (0.7)	9/15
LHD-2xDefa	<b>1.3</b> (1)	<b>1.9</b> (2)	<b>1.3</b> (2)	<b>1.5</b> (1)	<b>1.9</b> (2)	4/15
RAND-2xDef	<b>1.3</b> (0.6)	<b>1.3</b> (1)	<b>1.2</b> (0.7)	<b>1.3</b> (1)	<b>0.58</b> (0.8)	10/15
RF1-CMAES	<b>1.6</b> (0.8)	<b>1.3</b> (2)	6.3(4)	12(15)	12(8)	3/15
RF5-CMAES	<b>1.6</b> (1.0)	<b>1.6</b> (0.9)	8.5(26)	13(20)	12(11)	3/15
Sifeg	<b>2.0</b> (4)	<b>2.1</b> (3)	<b>2.3</b> (0.5)	8.9(22)	84(96)	10/15
Sif	<b>2.0</b> (0)	<b>2.3</b> (1)	<b>2.3</b> (2)	10(41)	103(119)	9/15
Srr	<b>2.0</b> (2)	<b>2.0</b> (2)	<b>2.4</b> (4)	27(9)	89(149)	11/15



Table 24: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>4.0e+1:1.5</i>	<i>2.5e+1:2.6</i>	<i>1.0e+1:7.8</i>	<i>4.0e+0:55</i>	<i>2.5e+0:103</i>	5/5
BSifeg	<b>2.0</b> (3)	<b>1.6</b> (2)	<b>1.9</b> (1)	<b>1.3</b> (2)	<b>0.91</b> (0.7)	15/15
BSif	<b>2.0</b> (3)	<b>1.6</b> (2)	<b>1.9</b> (2)	<b>1.3</b> (2)	<b>1.0</b> (0.9)	15/15
BSqi	<b>2.0</b> (2)	<b>1.6</b> (2)	<b>1.8</b> (2)	<b>1.6</b> (1)	<b>1.3</b> (1)	15/15
BSrr	<b>2.0</b> (3)	<b>1.6</b> (1)	<b>2.1</b> (1)	<b>1.5</b> (1.0)	<b>1.1</b> (0.8)	15/15
CMA-CSA	<b>1.3</b> (2)	<b>1.1</b> (0.6)	3.2(2)	<b>3.0</b> (2)	<b>2.8</b> (6)	15/15
CMA-MSR	<b>1.7</b> (1.0)	<b>2.3</b> (3)	<b>2.2</b> (3)	6.3(6)	4.8(6)	15/15
CMA-TPA	<b>1.1</b> (0.2)	<b>1.2</b> (1)	<b>1.9</b> (3)	3.2(4)	4.8(2)	15/15
GP1-CMAES	<b>1.2</b> (0.8)	<b>1.6</b> (2)	<b>2.2</b> (3)	3.0(3)	4.4(8)	10/15
GP5-CMAES	<b>1.7</b> (2)	<b>1.7</b> (1.0)	<b>2.0</b> (2)	<b>2.9</b> (5)	<b>2.2</b> (2)	13/15
IPOPCMAv3p	<b>1.3</b> (0.7)	<b>1.0</b> (0.6)	<b>0.99</b> (2)	<b>1.8</b> (1)	<b>2.8</b> (3)	13/15
LHD-10xDef	<b>1.6</b> (1.0)	<b>1.1</b> (0.7)	<b>1.5</b> (1.0)	<b>1.7</b> (2)	<b>1.8</b> (1)	6/15
LHD-2xDefa	<b>1.8</b> (1)	<b>2.1</b> (3)	<b>2.4</b> (3)	<b>1.6</b> (2)	4.5(7)	3/15
RAND-2xDef	<b>1.0</b> (1.0)	<b>1.4</b> (1)	<b>2.0</b> (2)	<b>1.5</b> (0.9)	4.2(5)	3/15
RF1-CMAES	<b>1.7</b> (1)	<b>1.4</b> (1)	<b>1.8</b> (3)	3.5(4)	<b>2.4</b> (1)	14/15
RF5-CMAES	<b>1.8</b> (1)	<b>1.4</b> (1)	<b>1.5</b> (2)	<b>1.8</b> (3)	<b>1.9</b> (2)	14/15
Sifeg	<b>1.9</b> (3)	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>1.9</b> (2)	<b>2.2</b> (2)	15/15
Sif	<b>1.9</b> (3)	<b>1.5</b> (2)	<b>1.8</b> (2)	<b>1.8</b> (2)	<b>2.2</b> (2)	15/15
Srr	<b>1.9</b> (2)	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>1.9</b> (2)	<b>2.3</b> (3)	15/15

Table 25: 02-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f24</i></b>	<i>4.0e+1:1.1</i>	<i>2.5e+1:2.7</i>	<i>1.6e+1:7.7</i>	<i>6.3e+0:44</i>	<i>2.5e+0:275</i>	5/5
BSifeg	<b>2.1</b> (3)	<b>2.3</b> (2)	<b>1.8</b> (3)	<b>2.4</b> (1)	6.3(1.0)	14/15
BSif	<b>2.1</b> (4)	<b>2.3</b> (2)	<b>1.6</b> (2)	<b>2.3</b> (2)	8.3(28)	15/15
BSqi	<b>2.1</b> (0.9)	<b>2.3</b> (0.8)	<b>2.9</b> (0.5)	<b>2.9</b> (3)	11(29)	14/15
BSrr	<b>2.1</b> (4)	<b>2.3</b> (2)	<b>1.9</b> (6)	<b>2.6</b> (2)	6.4(18)	14/15
CMA-CSA	<b>2.3</b> (3)	<b>2.2</b> (2)	<b>1.8</b> (1)	<b>1.2</b> (1)	3.3(6)	15/15
CMA-MSR	3.1(4)	<b>2.4</b> (2)	<b>1.6</b> (2)	3.8(0.6)	5.6(7)	15/15
CMA-TPA	<b>1.6</b> (0.5)	<b>2.2</b> (3)	<b>1.3</b> (1)	<b>2.3</b> (5)	4.1(3)	15/15
GP1-CMAES	<b>1.6</b> (1)	<b>1.7</b> (2)	<b>1.9</b> (3)	<b>1.8</b> (6)	<b>3.3</b> (2)	7/15
GP5-CMAES	<b>1.8</b> (0)	<b>1.9</b> (2)	<b>1.4</b> (3)	3.4(6)	<b>2.9</b> (4)	7/15
IPOPCMAv3p	<b>1.6</b> (0.9)	<b>2.1</b> (4)	<b>1.5</b> (1)	<b>1.2</b> (1)	3.9(6)	6/15
LHD-10xDef	<b>1.9</b> (1)	<b>1.4</b> (1)	<b>1.5</b> (2)	<b>1.5</b> (1)	$\infty$ 100	0/15
LHD-2xDefa	<b>1.8</b> (1)	<b>1.6</b> (0.8)	<b>2.0</b> (3)	<b>2.6</b> (4)	$\infty$ 100	0/15
RAND-2xDef	<b>1.2</b> (0.9)	<b>2.4</b> (2)	<b>1.8</b> (1)	<b>1.9</b> (3)	<b>2.5</b> (4)	2/15
RF1-CMAES	<b>1.4</b> (0.2)	<b>1.8</b> (3)	<b>1.3</b> (1)	<b>0.80</b> (0.6)	5.3(7)	4/15
RF5-CMAES	<b>1.8</b> (2)	<b>1.2</b> (0.5)	<b>1.2</b> (1)	<b>2.5</b> (3)	13(20)	2/15
Sifeg	<b>2.1</b> (3)	<b>2.4</b> (2)	<b>1.4</b> (0.6)	<b>2.3</b> (0.5)	4.9(2)	15/15
Sif	<b>2.1</b> (3)	<b>2.4</b> (3)	<b>1.4</b> (0.6)	<b>2.1</b> (2)	5.1(13)	15/15
Srr	<b>2.1</b> (2)	<b>2.4</b> (2)	<b>1.4</b> (0.8)	<b>2.1</b> (1)	7.4(4)	15/15

Table 26: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>1.6e+1</i> :3.0	<i>1.0e+1</i> :3.6	<i>1.0e-8</i> :8.0	<i>1.0e-8</i> :8.0	<i>1.0e-8</i> :8.0	15/15
BSifeg	<b>1.7</b> (2)	<b>1.5</b> (1)	<b>2.1</b> (0.3)	<b>2.1</b> (0.3)	<b>2.1</b> (0.3)	15/15
BSif	<b>1.7</b> (2)	<b>1.5</b> (2)	<b>2.1</b> (0.3)	<b>2.1</b> (0.3)	<b>2.1</b> (0.2)	15/15
BSqi	<b>1.7</b> (1)	<b>1.5</b> (1)	<b>2.1</b> (0.3)	<b>2.1</b> (0.2)	<b>2.1</b> (0.3)	15/15
BSrr	<b>1.7</b> (1)	<b>1.5</b> (1)	<b>2.1</b> (0.2)	<b>2.1</b> (0.2)	<b>2.1</b> (0.3)	15/15
CMA-CSA	5.4(2)	5.6(5)	52(3)	52(4)	52(4)	15/15
CMA-MSR	<b>2.1</b> (2)	<b>2.4</b> (3)	83(8)	83(9)	83(12)	15/15
CMA-TPA	<b>2.9</b> (2)	3.4(3)	55(20)	55(14)	55(18)	15/15
GP1-CMAES	<b>2.4</b> (2)	3.2(2)	31(3)	31(5)	31(5)	15/15
GP5-CMAES	<b>2.2</b> (2)	<b>2.8</b> (2)	46(36)	46(29)	46(36)	15/15
IPOPCMAv3p	<b>2.7</b> (4)	<b>2.8</b> (2)	52(7)	52(8)	52(6)	15/15
LHD-10xDef	<b>2.1</b> (2)	3.6(4)	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
LHD-2xDefa	<b>2.1</b> (2)	<b>2.2</b> (2)	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
RAND-2xDef	<b>1.8</b> (2)	<b>2.3</b> (2)	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
RF1-CMAES	<b>2.4</b> (2)	<b>2.3</b> (1)	133(108)	133(106)	133(74)	9/15
RF5-CMAES	12(41)	11(2)	$\infty$	$\infty$	$\infty$ <i>753</i>	0/15
Sifeg	<b>1.7</b> (2)	<b>1.5</b> (1)	7.5(0.7)	7.5(1)	7.5(1)	15/15
Sif	<b>1.7</b> (2)	<b>1.5</b> (1.0)	7.5(1)	7.5(0.7)	7.5(0.8)	15/15
Srr	<b>1.7</b> (1)	<b>1.5</b> (1)	7.2(0.6)	7.2(0.8)	7.2(0.9)	15/15

Table 27: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>6.3e+6</i> :1.5	<i>6.3e+5</i> :4.3	<i>4.0e+4</i> :10	<i>1.0e+2</i> :32	<i>1.0e-8</i> :49	15/15
BSifeg	3.7(4)	<b>2.8</b> (0.4)	<b>1.4</b> (0.2)	<b>0.66</b> (0.3)	<b>1.2</b> (0.3)	15/15
BSif	3.7(4)	<b>2.8</b> (0.9)	<b>1.4</b> (0.5)	<b>0.68</b> (0.2)	<b>1.2</b> (0.1)	15/15
BSqi	3.7(4)	<b>2.8</b> (0.4)	<b>1.4</b> (0.2)	<b>0.62</b> (0.1)	<b>1.1</b> (0.3)	15/15
BSrr	3.7(4)	<b>2.8</b> (1)	<b>1.4</b> (0.5)	<b>0.66</b> (0.0)	<b>1.3</b> (0.2)	15/15
CMA-CSA	<b>1.5</b> (0.3)	<b>1.4</b> (0.7)	3.5(4)	7.3(2)	18(2)	15/15
CMA-MSR	<b>2.3</b> (1.0)	<b>1.3</b> (0.5)	3.1(5)	6.9(2)	22(3)	15/15
CMA-TPA	<b>2.2</b> (1.0)	<b>2.0</b> (3)	3.3(5)	7.2(2)	19(3)	15/15
GP1-CMAES	3.1(3)	<b>2.5</b> (2)	<b>2.4</b> (1)	5.4(1)	45(38)	5/15
GP5-CMAES	3.1(3)	<b>1.9</b> (0.9)	<b>2.3</b> (1)	<b>2.5</b> (1.0)	21(28)	8/15
IPOPCMAv3p	<b>3.0</b> (4)	<b>2.3</b> (2)	<b>2.4</b> (3)	8.9(6)	$\infty$ 751	0/15
LHD-10xDef	<b>1.0</b> (0.3)	<b>1.2</b> (1)	<b>2.7</b> (3)	70(92)	$\infty$ 150	0/15
LHD-2xDefa	<b>1.2</b> (1.0)	<b>1.2</b> (1)	<b>1.3</b> (1)	70(89)	$\infty$ 150	0/15
RAND-2xDef	<b>1.2</b> (1.0)	<b>1.0</b> (1)	<b>2.3</b> (1)	16(16)	$\infty$ 150	0/15
RF1-CMAES	<b>2.2</b> (2)	<b>1.3</b> (1)	15(2)	60(69)	$\infty$ 751	0/15
RF5-CMAES	<b>1.9</b> (3)	<b>1.4</b> (1)	7.0(1)	167(184)	$\infty$ 760	0/15
Sifeg	3.7(4)	<b>2.9</b> (2)	<b>1.9</b> (0.8)	<b>1.1</b> (0.1)	<b>1.7</b> (0.3)	15/15
Sif	3.7(4)	<b>2.9</b> (0.4)	<b>1.9</b> (0.8)	<b>1.2</b> (0.4)	<b>1.6</b> (0.3)	15/15
Srr	3.7(4)	<b>2.9</b> (0.2)	<b>1.9</b> (1)	<b>1.0</b> (0.1)	<b>1.7</b> (0.1)	15/15

Table 28: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>1.0e+2</i> :2:2	<i>6.3e+1</i> :6.1	<i>4.0e+1</i> :10	<i>1.6e+1</i> :32	<i>4.0e+0</i> :319	15/15
BSifeg	3.1(3)	<b>1.6</b> (1.0)	<b>1.3</b> (0.2)	<b>0.64</b> (0.3)	<b>0.18</b> (0.1)	15/15
BSif	3.1(3)	<b>1.6</b> (1.0)	<b>1.3</b> (0.2)	<b>0.64</b> (0.4)	<b>0.19</b> (0.1)	15/15
BSqi	3.1(2)	<b>1.6</b> (0.9)	<b>1.3</b> (0.2)	<b>0.62</b> (0.2)	<b>0.19</b> (0.1)	15/15
BSrr	3.1(2)	<b>1.6</b> (0.9)	<b>1.3</b> (0.2)	<b>0.60</b> (0.2)	<b>0.19</b> (0.1)	15/15
CMA-CSA	3.5(4)	<b>2.1</b> (2)	<b>2.5</b> (2)	3.2(2)	3.3(3)	15/15
CMA-MSR	3.0(3)	<b>1.8</b> (2)	<b>2.5</b> (2)	5.2(2)	<b>2.7</b> (3)	15/15
CMA-TPA	<b>3.0</b> (0.9)	<b>1.8</b> (2)	<b>2.3</b> (2)	<b>2.3</b> (2)	<b>2.6</b> (2)	15/15
GP1-CMAES	<b>2.0</b> (3)	<b>1.6</b> (2)	<b>1.9</b> (2)	3.7(2)	<b>1.1</b> (0.9)	13/15
GP5-CMAES	<b>1.9</b> (2)	<b>1.4</b> (1)	<b>1.5</b> (0.9)	<b>1.4</b> (0.6)	<b>1.6</b> (2)	11/15
IPOPCMAv3p	<b>2.8</b> (3)	<b>2.3</b> (3)	3.5(3)	<b>2.9</b> (3)	<b>1.9</b> (3)	10/15
LHD-10xDef	<b>2.9</b> (2)	<b>1.7</b> (1)	4.1(2)	4.0(0.3)	3.5(4)	2/15
LHD-2xDefa	<b>1.6</b> (0.9)	<b>1.3</b> (1)	<b>1.4</b> (1)	<b>1.7</b> (0.5)	<b>1.2</b> (1)	5/15
RAND-2xDef	<b>1.7</b> (1)	<b>1.1</b> (1)	<b>1.6</b> (1.0)	<b>1.6</b> (1.0)	<b>1.2</b> (1)	5/15
RF1-CMAES	<b>2.7</b> (2)	<b>2.6</b> (2)	<b>2.3</b> (0.6)	5.9(12)	6.8(13)	4/15
RF5-CMAES	<b>2.4</b> (1)	8.2(1)	9.2(28)	14(26)	11(18)	3/15
Sifeg	3.1(3)	<b>1.6</b> (0.6)	<b>1.4</b> (0.3)	<b>0.72</b> (0.1)	<b>0.21</b> (0.0)	15/15
Sif	3.1(2)	<b>1.6</b> (0.2)	<b>1.4</b> (0.3)	<b>0.72</b> (0.3)	<b>0.22</b> (0.1)	15/15
Srr	3.1(3)	<b>1.6</b> (1)	<b>1.4</b> (0.3)	<b>0.69</b> (0.5)	<b>0.20</b> (0.0)	15/15

Table 29: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>1.0e+2:5.4</i>	<i>6.3e+1:10</i>	<i>6.3e+1:10</i>	<i>2.5e+1:36</i>	<i>4.0e+0:617</i>	15/15
BSifeg	<b>2.3</b> (1)	<b>2.0</b> (2)	<b>2.0</b> (2)	<b>1.1</b> (0.6)	<b>0.16</b> (0.1)	15/15
BSif	<b>2.2</b> (3)	<b>2.1</b> (2)	<b>2.1</b> (2)	<b>1.1</b> (0.6)	<b>0.16</b> (0.1)	15/15
BSqi	<b>2.2</b> (3)	<b>2.0</b> (2)	<b>2.0</b> (1)	<b>1.1</b> (0.5)	<b>0.17</b> (0.0)	15/15
BSrr	<b>2.3</b> (3)	<b>2.0</b> (1)	<b>2.0</b> (2)	<b>1.1</b> (0.6)	<b>0.16</b> (0.1)	15/15
CMA-CSA	<b>1.9</b> (3)	<b>1.7</b> (2)	<b>1.7</b> (0.8)	<b>1.7</b> (1)	3.9(5)	15/15
CMA-MSR	<b>3.0</b> (0.6)	<b>2.1</b> (2)	<b>2.1</b> (1)	<b>2.4</b> (0.9)	7.0(7)	15/15
CMA-TPA	<b>1.9</b> (2)	<b>2.1</b> (2)	<b>2.1</b> (2)	<b>2.7</b> (2)	4.0(4)	15/15
GP1-CMAES	<b>2.5</b> (3)	<b>2.3</b> (1)	<b>2.3</b> (2)	<b>2.0</b> (0.6)	8.3(10)	2/15
GP5-CMAES	3.1(0.9)	6.0(2)	6.0(5)	4.6(11)	5.5(5)	3/15
IPOPCMAv3p	<b>1.9</b> (1)	<b>2.5</b> (2)	<b>2.5</b> (2)	3.5(1.0)	8.3(13)	2/15
LHD-10xDef	<b>1.0</b> (0.9)	<b>2.1</b> (1)	<b>2.1</b> (4)	<b>2.9</b> (2)	$\infty$ 150	0/15
LHD-2xDefa	<b>1.2</b> (2)	<b>1.4</b> (2)	<b>1.4</b> (2)	<b>2.5</b> (3)	3.6(5)	1/15
RAND-2xDef	<b>1.2</b> (0.7)	<b>2.1</b> (2)	<b>2.1</b> (1)	<b>2.1</b> (3)	$\infty$ 150	0/15
RF1-CMAES	<b>1.4</b> (2)	3.2(3)	3.2(3)	33(16)	$\infty$ 751	0/15
RF5-CMAES	19(0.3)	16(15)	16(28)	37(26)	$\infty$ 753	0/15
Sifeg	<b>2.1</b> (2)	<b>1.7</b> (0.9)	<b>1.7</b> (0.5)	<b>0.81</b> (0.5)	<b>0.14</b> (0.0)	15/15
Sif	<b>2.1</b> (2)	<b>1.8</b> (0.5)	<b>1.8</b> (1)	<b>0.85</b> (0.2)	<b>0.14</b> (0.1)	15/15
Srr	<b>2.1</b> (2)	<b>1.7</b> (1)	<b>1.7</b> (1)	<b>0.80</b> (0.3)	<b>0.14</b> (0.1)	15/15

Table 30: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f5</b>	<i>4.0e+1</i> :2.2	<i>2.5e+1</i> :4.8	<i>1.0e-8</i> :6.6	<i>1.0e-8</i> :6.6	<i>1.0e-8</i> :6.6	15/15
BSifeg	3.5(1)	<b>1.9</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
BSif	3.5(0.5)	<b>1.9</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
BSqi	3.5(0.9)	<b>1.9</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
BSrr	3.5(0.7)	<b>1.9</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
CMA-CSA	3.1(3)	<b>2.4</b> (5)	5.5(2)	5.5(4)	5.5(3)	15/15
CMA-MSR	<b>3.0</b> (2)	<b>2.0</b> (1)	4.9(2)	4.9(3)	4.9(3)	15/15
CMA-TPA	<b>1.8</b> (2)	<b>1.9</b> (1)	3.9(2)	3.9(2)	3.9(2)	15/15
GP1-CMAES	3.7(3)	<b>2.2</b> (1)	24(56)	24(6)	24(28)	14/15
GP5-CMAES	3.2(2)	<b>2.4</b> (1)	4.7(3)	4.7(3)	4.7(4)	15/15
IPOPCMAv3p	4.3(4)	3.1(4)	10(13)	10(16)	10(13)	15/15
LHD-10xDef	<b>1.5</b> (2)	<b>2.2</b> (2)	13(0.4)	13(0.4)	13(0.4)	15/15
LHD-2xDefa	<b>1.8</b> (1)	<b>2.0</b> (2)	3.1(0.8)	3.1(0.4)	3.1(0.4)	15/15
RAND-2xDef	<b>2.2</b> (0.9)	<b>2.2</b> (1)	3.1(0.4)	3.1(0.4)	3.1(0.4)	15/15
RF1-CMAES	3.7(5)	<b>2.2</b> (2)	19(41)	19(22)	19(40)	15/15
RF5-CMAES	3.8(2)	11(32)	150(114)	150(263)	150(97)	7/15
Sifeg	3.5(0.6)	<b>1.9</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.1)	15/15
Sif	3.5(0.7)	<b>1.9</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15
Srr	3.5(0.5)	<b>1.9</b> (0.3)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.2)	15/15

Table 31: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>6.3e+4</i> :1.8	<i>6.3e+3</i> :3.7	<i>4.0e+1</i> :13	<i>1.0e+1</i> :34	<i>6.3e-4</i> :159	15/15
BSifeg	<b>1.9</b> (3)	<b>1.2</b> (1)	79(273)	146(132)	1254(864)	2/15
BSif	<b>1.9</b> (2)	<b>1.2</b> (2)	99(184)	209(699)	$\infty$ 3e4	0/15
BSqi	<b>1.9</b> (2)	<b>1.2</b> (0.7)	30(19)	231(9)	853(961)	3/15
BSrr	<b>1.9</b> (2)	<b>1.2</b> (1)	119(211)	114(178)	1324(805)	2/15
CMA-CSA	<b>1.7</b> (3)	<b>1.3</b> (0.3)	<b>1.6</b> (0.5)	<b>1.5</b> (2)	<b>2.6</b> (0.7)	15/15
CMA-MSR	<b>2.3</b> (6)	<b>2.1</b> (10)	<b>2.1</b> (2)	<b>2.8</b> (1)	3.6(0.5)	15/15
CMA-TPA	<b>2.4</b> (4)	<b>2.2</b> (2)	3.0(2)	3.1(0.7)	<b>3.0</b> (0.9)	15/15
GP1-CMAES	3.7(6)	<b>2.9</b> (3)	<b>1.6</b> (1)	<b>2.7</b> (3)	$\infty$ 751	0/15
GP5-CMAES	3.7(6)	3.3(4)	3.4(4)	<b>2.5</b> (2)	$\infty$ 760	0/15
IPOPCMAv3p	4.0(2)	3.8(3)	<b>2.8</b> (4)	<b>2.8</b> (2)	<b>3.2</b> (0.7)	15/15
LHD-10xDef	<b>0.81</b> (0.8)	<b>1.6</b> (0.5)	<b>2.0</b> (1)	4.2(6)	$\infty$ 150	0/15
LHD-2xDefa	<b>0.85</b> (0.3)	<b>0.85</b> (0.5)	<b>1.4</b> (2)	4.8(6)	$\infty$ 150	0/15
RAND-2xDef	<b>0.96</b> (0.8)	<b>1.1</b> (0.5)	<b>2.6</b> (3)	3.1(3)	$\infty$ 150	0/15
RF1-CMAES	<b>2.7</b> (4)	<b>2.3</b> (2)	<b>2.7</b> (1)	13(33)	$\infty$ 751	0/15
RF5-CMAES	3.2(2)	34(103)	23(48)	42(54)	$\infty$ 760	0/15
Sifeg	<b>1.9</b> (2)	<b>1.2</b> (1)	9.4(11)	81(244)	798(891)	3/15
Sif	<b>1.9</b> (3)	<b>1.2</b> (1)	25(75)	106(430)	$\infty$ 3e4	0/15
Srr	<b>1.9</b> (2)	<b>1.2</b> (1)	35(25)	75(104)	543(577)	4/15



Table 32: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f7</i></b>	<i>2.5e+2</i> :1.5	<i>6.3e+1</i> :4.2	<i>1.0e+1</i> :11	<i>2.5e+0</i> :38	<i>4.0e-1</i> :174	15/15
BSifeg	<b>1.7</b> (1.0)	34(241)	49(133)	142(494)	119(208)	10/15
BSif	<b>1.7</b> (2)	34(241)	61(45)	235(400)	233(252)	7/15
BSqi	<b>1.7</b> (3)	34(1)	167(178)	215(402)	131(196)	10/15
BSrr	<b>1.7</b> (2)	34(121)	131(443)	325(814)	158(233)	9/15
CMA-CSA	<b>1.9</b> (1)	<b>2.4</b> (2)	<b>2.8</b> (2)	<b>1.9</b> (1)	<b>0.89</b> (1)	15/15
CMA-MSR	<b>2.2</b> (2)	<b>1.8</b> (2)	3.5(3)	<b>2.1</b> (2)	<b>1.3</b> (1)	15/15
CMA-TPA	<b>3.0</b> (2)	<b>1.8</b> (2)	3.8(6)	<b>2.7</b> (1)	<b>1.4</b> (1)	15/15
GP1-CMAES	<b>1.4</b> (0.2)	<b>1.3</b> (0.7)	<b>2.0</b> (2)	<b>1.5</b> (2)	<b>0.56</b> (0.6)	15/15
GP5-CMAES	<b>2.1</b> (3)	<b>2.3</b> (2)	<b>2.0</b> (1)	<b>1.1</b> (0.8)	<b>0.63</b> (1)	15/15
IPOPCMAv3p	<b>2.8</b> (2)	3.9(3)	4.9(5)	<b>2.8</b> (3)	<b>1.2</b> (0.7)	15/15
LHD-10xDef	<b>1.2</b> (0.7)	<b>1.8</b> (2)	3.7(4)	<b>2.1</b> (1)	<b>1.9</b> (2)	6/15
LHD-2xDefa	<b>1.8</b> (1.0)	<b>1.8</b> (2)	<b>1.9</b> (1)	<b>1.5</b> (2)	<b>0.98</b> (0.8)	9/15
RAND-2xDef	<b>1.7</b> (1)	<b>1.2</b> (1)	<b>2.4</b> (2)	<b>1.6</b> (2)	<b>0.90</b> (0.9)	10/15
RF1-CMAES	<b>2.0</b> (2)	3.3(1.0)	7.5(7)	3.8(6)	<b>2.1</b> (5)	12/15
RF5-CMAES	<b>2.5</b> (3)	<b>2.7</b> (2)	10(24)	20(11)	31(36)	2/15
Sifeg	<b>1.7</b> (0.5)	<b>1.9</b> (2)	37(45)	205(380)	122(76)	11/15
Sif	<b>1.7</b> (2)	<b>2.0</b> (2)	61(0.6)	234(188)	131(277)	10/15
Srr	<b>1.7</b> (3)	<b>1.9</b> (2)	97(0.7)	297(543)	154(280)	9/15

Table 33: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>1.0e+4</i> :1.8	<i>1.6e+3</i> :4.0	<i>1.0e+2</i> :15	<i>6.3e+0</i> :31	<i>1.0e-1</i> :152	15/15
BSifeg	<b>1.7</b> (2)	<b>2.4</b> (1)	6.6(14)	7.3(14)	398(343)	6/15
BSif	<b>1.7</b> (1)	<b>2.4</b> (1)	6.0(10)	6.1(11)	266(223)	7/15
BSqi	<b>1.7</b> (1)	<b>2.4</b> (1)	4.8(10)	6.7(11)	789(1355)	3/15
BSrr	<b>1.7</b> (3)	<b>2.4</b> (2)	4.2(12)	4.5(5)	595(363)	4/15
CMA-CSA	4.8(7)	4.1(5)	3.2(2)	3.1(1)	<b>3.3</b> (1)	15/15
CMA-MSR	3.4(2)	3.2(4)	3.4(2)	4.0(3)	4.5(1)	15/15
CMA-TPA	<b>2.6</b> (3)	<b>2.5</b> (4)	<b>2.9</b> (2)	3.5(2)	<b>3.7</b> (1.0)	15/15
GP1-CMAES	3.2(4)	<b>2.6</b> (3)	<b>2.7</b> (2)	<b>2.9</b> (2)	13(8)	5/15
GP5-CMAES	<b>2.9</b> (2)	<b>2.7</b> (3)	<b>2.1</b> (1.0)	3.0(7)	<b>4.4</b> (4)	10/15
IPOPCMAv3p	3.9(3)	3.3(2)	3.2(1)	3.2(1)	5.5(3)	10/15
LHD-10xDef	<b>2.3</b> (1)	<b>2.9</b> (2)	5.0(3)	10(8)	$\infty$ 150	0/15
LHD-2xDefa	<b>1.5</b> (0.8)	<b>2.0</b> (2)	<b>1.8</b> (0.5)	3.3(3)	$\infty$ 150	0/15
RAND-2xDef	<b>2.0</b> (1)	<b>2.2</b> (2)	<b>1.9</b> (1)	3.0(2)	$\infty$ 150	0/15
RF1-CMAES	<b>2.0</b> (0.8)	<b>2.7</b> (3)	4.0(9)	13(20)	$\infty$ 751	0/15
RF5-CMAES	<b>2.6</b> (4)	<b>1.9</b> (4)	19(22)	53(52)	$\infty$ 753	0/15
Sifeg	<b>1.7</b> (2)	<b>2.4</b> (0.8)	<b>1.4</b> (1)	<b>1.8</b> (2)	123(135)	11/15
Sif	<b>1.7</b> (1)	<b>2.4</b> (0.8)	<b>1.3</b> (0.2)	<b>2.1</b> (3)	261(107)	7/15
Srr	<b>1.7</b> (1)	<b>2.4</b> (1)	<b>1.3</b> (2)	<b>1.7</b> (2)	211(359)	8/15

Table 34: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>1.0e+1:21</i>	<i>6.3e+0:25</i>	<i>4.0e+0:32</i>	<i>2.5e+0:48</i>	<i>6.3e-3:152</i>	15/15
BSifeg	14(30)	12(25)	48(152)	107(222)	$\infty$ <i>3e4</i>	0/15
BSif	12(21)	11(6)	39(15)	179(220)	$\infty$ <i>3e4</i>	0/15
BSqi	8.5(14)	7.7(12)	50(13)	88(15)	1267(1585)	2/15
BSrr	8.0(15)	8.2(15)	41(9)	75(17)	$\infty$ <i>3e4</i>	0/15
CMA-CSA	3.8(0.9)	3.7(1)	3.2(2)	<b>3.2</b> (4)	<b>4.3</b> (3)	15/15
CMA-MSR	5.8(3)	6.9(13)	7.0(7)	7.3(7)	<b>5.9</b> (3)	15/15
CMA-TPA	4.3(2)	4.6(2)	4.9(1)	6.0(6)	<b>5.4</b> (2)	15/15
GP1-CMAES	3.5(1)	4.0(6)	5.5(1)	7.7(8)	35(40)	2/15
GP5-CMAES	<b>2.4</b> (1.0)	<b>2.5</b> (1)	<b>3.2</b> (1)	4.0(0.9)	12(22)	5/15
IPOPCMAv3p	3.5(3)	3.5(2)	<b>3.2</b> (2)	<b>3.3</b> (4)	8.2(6)	8/15
LHD-10xDef	10(12)	16(14)	16(11)	22(28)	$\infty$ <i>150</i>	0/15
LHD-2xDefa	<b>2.5</b> (2)	<b>2.9</b> (2)	3.3(2)	5.8(3)	$\infty$ <i>150</i>	0/15
RAND-2xDef	<b>2.6</b> (1)	3.3(3)	<b>3.0</b> (1)	<b>4.0</b> (4)	$\infty$ <i>150</i>	0/15
RF1-CMAES	8.1(20)	7.8(16)	9.1(24)	12(17)	$\infty$ <i>751</i>	0/15
RF5-CMAES	37(38)	34(52)	33(34)	32(31)	$\infty$ <i>753</i>	0/15
Sifeg	<b>1.9</b> (0.8)	<b>1.8</b> (2)	63(76)	73(209)	$\infty$ <i>3e4</i>	0/15
Sif	<b>1.8</b> (1)	<b>1.7</b> (2)	40(0.8)	87(211)	$\infty$ <i>3e4</i>	0/15
Srr	<b>1.5</b> (0.4)	<b>1.4</b> (1)	101(184)	135(249)	$\infty$ <i>2e4</i>	0/15

Table 35: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>6.3e+6</i> :1.7	<i>1.6e+5</i> :4.4	<i>4.0e+4</i> :12	<i>4.0e+2</i> :37	<i>1.0e+0</i> :152	15/15
BSifeg	<b>1.0</b> (0.3)	<b>2.5</b> (1)	4.7(13)	411(417)	1211(992)	1/15
BSif	<b>1.0</b> (0.3)	<b>2.5</b> (1)	5.7(0.2)	578(334)	1253(1696)	1/15
BSqi	<b>1.0</b> (0.3)	<b>2.5</b> (1)	6.9(0.2)	304(351)	725(915)	2/15
BSrr	<b>1.0</b> (0.3)	<b>2.5</b> (1)	5.4(0.3)	691(454)	1155(1570)	1/15
CMA-CSA	<b>1.4</b> (2)	<b>2.3</b> (2)	<b>2.8</b> (2)	4.8(2)	<b>3.0</b> (1.0)	15/15
CMA-MSR	<b>1.4</b> (2)	<b>3.0</b> (1)	<b>2.0</b> (2)	<b>4.0</b> (2)	3.4(1)	15/15
CMA-TPA	<b>1.2</b> (0.9)	3.2(3)	<b>1.9</b> (1)	<b>3.2</b> (2)	3.1(0.9)	15/15
GP1-CMAES	<b>2.6</b> (0.6)	<b>2.7</b> (3)	<b>2.4</b> (2)	4.3(2)	<b>2.8</b> (1)	15/15
GP5-CMAES	<b>1.3</b> (0.4)	<b>1.8</b> (3)	<b>1.6</b> (1)	<b>2.3</b> (1)	<b>1.1</b> (0.4)	15/15
IPOPCMAv3p	<b>2.2</b> (3)	<b>2.7</b> (4)	<b>2.0</b> (1)	5.8(5)	4.4(6)	13/15
LHD-10xDef	<b>1.4</b> (1)	<b>2.4</b> (2)	<b>2.9</b> (3)	14(16)	$\infty$ 150	0/15
LHD-2xDefa	<b>1.2</b> (0.6)	3.0(2)	<b>1.8</b> (1)	11(11)	$\infty$ 150	0/15
RAND-2xDef	<b>1.3</b> (2)	<b>3.0</b> (3)	<b>2.1</b> (1)	8.4(12)	$\infty$ 150	0/15
RF1-CMAES	<b>1.5</b> (2)	<b>2.4</b> (2)	7.8(32)	34(55)	$\infty$ 751	0/15
RF5-CMAES	<b>2.0</b> (2)	3.2(3)	<b>1.5</b> (1)	49(79)	$\infty$ 753	0/15
Sifeg	<b>1.0</b> (1)	<b>2.7</b> (1)	<b>1.5</b> (0.3)	173(211)	467(452)	1/15
Sif	<b>1.0</b> (1)	<b>2.7</b> (1)	<b>1.5</b> (0.4)	109(121)	482(552)	1/15
Srr	<b>1.0</b> (0.3)	<b>2.7</b> (0.8)	<b>1.5</b> (0.4)	105(181)	194(326)	2/15

Table 36: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>2.5e+6</i> :1.9	<i>4.0e+5</i> :4.5	<i>6.3e+4</i> :9.4	<i>2.5e+1</i> :36	<i>2.5e-1</i> :174	15/15
BSifeg	<b>1.6</b> (1)	<b>2.0</b> (1)	<b>1.2</b> (0.7)	138(224)	1140(884)	1/15
BSif	<b>1.6</b> (1)	<b>2.0</b> (1.0)	<b>1.2</b> (0.7)	168(241)	365(243)	3/15
BSqi	<b>1.6</b> (3)	<b>2.0</b> (1)	<b>1.2</b> (0.2)	141(245)	$\infty$ 2e4	0/15
BSrr	<b>1.6</b> (1)	<b>2.0</b> (1)	<b>1.2</b> (0.2)	126(274)	1061(1784)	1/15
CMA-CSA	<b>1.0</b> (0.8)	<b>1.1</b> (1)	<b>1.3</b> (2)	<b>6.2</b> (4)	3.0(0.8)	15/15
CMA-MSR	<b>2.0</b> (2)	<b>2.6</b> (2)	<b>1.8</b> (2)	10(5)	<b>3.0</b> (0.5)	15/15
CMA-TPA	<b>1.5</b> (2)	<b>1.5</b> (1)	<b>1.5</b> (1)	7.8(5)	3.1(0.9)	15/15
GP1-CMAES	<b>2.5</b> (3)	<b>2.1</b> (2)	<b>1.7</b> (1)	<b>6.7</b> (6)	<b>2.8</b> (0.6)	15/15
GP5-CMAES	<b>2.3</b> (2)	<b>1.9</b> (1)	<b>1.9</b> (0.6)	<b>2.7</b> (1)	<b>1.2</b> (0.2)	15/15
IPOPCMAv3p	<b>1.8</b> (2)	<b>2.3</b> (2)	<b>1.9</b> (2)	11(8)	13(9)	5/15
LHD-10xDef	<b>1.9</b> (1)	<b>2.4</b> (4)	<b>2.4</b> (3)	30(44)	$\infty$ 150	0/15
LHD-2xDefa	<b>1.8</b> (2)	<b>2.1</b> (2)	<b>1.5</b> (1)	11(16)	$\infty$ 150	0/15
RAND-2xDef	<b>1.4</b> (1)	<b>1.4</b> (1)	<b>1.4</b> (0.9)	11(12)	$\infty$ 150	0/15
RF1-CMAES	<b>1.6</b> (2)	<b>1.3</b> (1)	<b>1.3</b> (0.9)	34(48)	61(90)	1/15
RF5-CMAES	<b>2.3</b> (2)	<b>1.9</b> (1)	<b>1.9</b> (1)	15(25)	$\infty$ 753	0/15
Sifeg	<b>1.7</b> (2)	<b>2.0</b> (1)	<b>1.4</b> (0.9)	50(104)	$\infty$ 7533	0/15
Sif	<b>1.7</b> (1)	<b>2.0</b> (1)	<b>1.4</b> (0.3)	66(123)	$\infty$ 7579	0/15
Srr	<b>1.7</b> (4)	<b>2.0</b> (1)	<b>1.4</b> (0.5)	60(177)	189(350)	3/15

Table 37: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>1.0e+8</i> :1.5	<i>1.0e+7</i> :3.6	<i>6.3e+5</i> :13	<i>6.3e+2</i> :31	<i>1.0e+0</i> :168	15/15
BSifeg	<b>1.1</b> (0.7)	<b>1.3</b> (1.0)	<b>1.1</b> (0.2)	10(7)	48(52)	11/15
BSif	<b>1.1</b> (1.0)	<b>1.3</b> (1)	<b>1.1</b> (0.3)	8.6(17)	80(72)	9/15
BSqi	<b>1.1</b> (2)	<b>1.3</b> (2)	<b>1.1</b> (0.4)	43(0.1)	71(83)	11/15
BSrr	<b>1.1</b> (0.7)	<b>1.3</b> (0.6)	<b>1.1</b> (0.4)	27(8)	46(128)	10/15
CMA-CSA	<b>1.2</b> (2)	<b>2.2</b> (1)	<b>1.6</b> (1)	5.1(2)	5.1(3)	15/15
CMA-MSR	<b>1.7</b> (2)	<b>1.9</b> (2)	3.2(2)	7.1(2)	6.7(14)	15/15
CMA-TPA	<b>1.7</b> (2)	<b>2.5</b> (2)	3.1(2)	5.6(2)	<b>5.0</b> (7)	15/15
GP1-CMAES	<b>1.0</b> (1)	<b>1.7</b> (2)	<b>2.3</b> (2)	<b>4.2</b> (3)	<b>4.3</b> (3)	10/15
GP5-CMAES	<b>1.2</b> (0.3)	<b>2.5</b> (2)	<b>2.3</b> (1)	5.6(1)	<b>4.9</b> (10)	8/15
IPOPCMAv3p	<b>1.4</b> (1)	<b>2.6</b> (3)	<b>2.9</b> (3)	5.3(2)	5.9(6)	8/15
LHD-10xDef	<b>0.96</b> (1.0)	<b>1.6</b> (2)	4.2(3)	$\infty$	$\infty$ 150	0/15
LHD-2xDefa	<b>1.1</b> (0.7)	<b>1.8</b> (2)	<b>1.6</b> (0.8)	4.7(3)	13(12)	1/15
RAND-2xDef	<b>1</b> (0.3)	<b>1.5</b> (0.9)	<b>1.6</b> (0.9)	4.2(5)	$\infty$ 150	0/15
RF1-CMAES	<b>1.0</b> (3)	<b>1.6</b> (2)	<b>2.4</b> (2)	5.1(2)	20(20)	3/15
RF5-CMAES	<b>1.2</b> (0.5)	10(34)	18(26)	65(104)	$\infty$ 753	0/15
Sifeg	<b>1.1</b> (0)	<b>1.3</b> (2)	<b>1.2</b> (0.4)	<b>2.9</b> (0.6)	20(18)	9/15
Sif	<b>1.1</b> (1)	<b>1.3</b> (0.9)	<b>1.4</b> (0.3)	5.8(13)	20(26)	9/15
Srr	<b>1.1</b> (0)	<b>1.3</b> (1.0)	<b>1.3</b> (0.3)	<b>3.4</b> (11)	19(33)	10/15

Table 38: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>1.0e+3</i> :1.6	<i>4.0e+2</i> :6.8	<i>2.5e+2</i> :11	<i>4.0e+1</i> :30	<i>2.5e-3</i> :182	15/15
BSifeg	<b>1.7</b> (1)	<b>1.6</b> (0.7)	<b>1.4</b> (0.9)	89(513)	$\infty$ <i>3e4</i>	0/15
BSif	<b>1.7</b> (2)	<b>1.6</b> (1)	<b>1.4</b> (0.5)	59(19)	$\infty$ <i>3e4</i>	0/15
BSqi	<b>1.7</b> (2)	<b>1.6</b> (0.7)	<b>1.3</b> (0.3)	26(68)	$\infty$ <i>3e4</i>	0/15
BSrr	<b>1.7</b> (3)	<b>1.6</b> (0.8)	<b>1.4</b> (0.7)	50(165)	$\infty$ <i>2e4</i>	0/15
CMA-CSA	<b>3.0</b> (4)	<b>2.2</b> (3)	<b>1.8</b> (2)	3.7(2)	<b>3.4</b> (0.5)	15/15
CMA-MSR	<b>2.4</b> (3)	<b>1.8</b> (2)	<b>2.0</b> (1)	4.2(2)	3.9(0.6)	15/15
CMA-TPA	<b>1.8</b> (0.9)	<b>1.8</b> (2)	<b>2.6</b> (5)	3.5(2)	<b>3.9</b> (0.7)	15/15
GP1-CMAES	<b>0.75</b> (0.3)	<b>1.7</b> (1)	<b>1.5</b> (0.8)	<b>2.0</b> (0.9)	19(16)	3/15
GP5-CMAES	<b>2.0</b> (2)	<b>1.4</b> (2)	<b>1.2</b> (0.9)	<b>1.4</b> (0.4)	<b>3.2</b> (3)	11/15
IPOPCMAv3p	<b>1.6</b> (3)	<b>1.7</b> (2)	<b>1.9</b> (0.8)	3.4(2)	12(7)	5/15
LHD-10xDef	<b>1.6</b> (4)	<b>1.5</b> (0.6)	<b>2.9</b> (3)	3.1(0.7)	$\infty$ <i>150</i>	0/15
LHD-2xDefa	<b>1.2</b> (0.8)	<b>1.1</b> (0.8)	<b>1.3</b> (0.8)	<b>1.3</b> (0.6)	$\infty$ <i>150</i>	0/15
RAND-2xDef	<b>1.4</b> (0.9)	<b>0.99</b> (1)	<b>1.1</b> (0.9)	<b>1.5</b> (2)	$\infty$ <i>150</i>	0/15
RF1-CMAES	<b>1.9</b> (2)	<b>1.6</b> (1)	<b>1.8</b> (2)	4.2(0.7)	$\infty$ <i>751</i>	0/15
RF5-CMAES	<b>1.9</b> (2)	<b>2.0</b> (2)	<b>2.5</b> (5)	21(11)	$\infty$ <i>760</i>	0/15
Sifeg	<b>1.7</b> (3)	<b>1.5</b> (1)	<b>1.3</b> (0.3)	169(270)	$\infty$ <i>2e4</i>	0/15
Sif	<b>1.7</b> (1)	<b>1.5</b> (1)	<b>1.3</b> (0.4)	76(0.9)	$\infty$ <i>2e4</i>	0/15
Srr	<b>1.7</b> (1)	<b>1.5</b> (0.9)	<b>1.3</b> (0.2)	58(45)	$\infty$ <i>2e4</i>	0/15

Table 39: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>1.0e+1:2.2</i>	<i>6.3e+0:4.2</i>	<i>2.5e+0:10</i>	<i>6.3e-2:31</i>	<i>2.5e-6:160</i>	15/15
BSifeg	<b>1.8</b> (1)	<b>2.1</b> (3)	<b>2.7</b> (1)	5.0(8)	$\infty$ <i>3e4</i>	0/15
BSif	<b>1.8</b> (2)	<b>2.2</b> (1)	4.3(10)	5.5(7)	$\infty$ <i>3e4</i>	0/15
BSqi	<b>1.8</b> (2)	<b>2.3</b> (2)	<b>2.4</b> (0.9)	4.2(6)	$\infty$ <i>3e4</i>	0/15
BSrr	<b>1.8</b> (2)	<b>1.9</b> (2)	<b>2.5</b> (1)	5.6(9)	$\infty$ <i>3e4</i>	0/15
CMA-CSA	3.8(3)	3.1(1)	<b>2.3</b> (2)	4.1(0.7)	<b>4.0</b> (0.5)	15/15
CMA-MSR	<b>2.5</b> (2)	<b>1.8</b> (2)	<b>2.4</b> (2)	5.3(2)	<b>4.4</b> (0.9)	15/15
CMA-TPA	4.4(5)	3.7(3)	3.4(2)	4.5(2)	<b>3.8</b> (0.5)	15/15
GP1-CMAES	3.9(5)	<b>2.7</b> (3)	<b>2.2</b> (1)	<b>2.7</b> (0.8)	$\infty$ <i>751</i>	0/15
GP5-CMAES	3.3(4)	<b>2.3</b> (2)	<b>2.0</b> (1)	<b>1.9</b> (0.6)	68(40)	1/15
IPOPCMAv3p	<b>2.2</b> (3)	<b>2.3</b> (4)	<b>2.7</b> (2)	4.0(1)	23(38)	3/15
LHD-10xDef	<b>1.5</b> (2)	<b>1.4</b> (3)	<b>2.0</b> (2)	4.0(0.4)	$\infty$ <i>150</i>	0/15
LHD-2xDefa	<b>1.9</b> (1)	<b>1.6</b> (1)	<b>1.6</b> (0.9)	<b>1.8</b> (0.9)	$\infty$ <i>150</i>	0/15
RAND-2xDef	<b>2.3</b> (2)	<b>1.5</b> (0.7)	<b>1.5</b> (1)	<b>2.3</b> (1.0)	$\infty$ <i>150</i>	0/15
RF1-CMAES	<b>2.9</b> (5)	<b>2.7</b> (4)	4.7(8)	16(30)	$\infty$ <i>751</i>	0/15
RF5-CMAES	<b>1.9</b> (2)	<b>1.1</b> (1.0)	20(57)	47(43)	$\infty$ <i>753</i>	0/15
Sifeg	<b>1.8</b> (2)	<b>1.7</b> (1)	<b>2.0</b> (1)	<b>2.6</b> (2)	$\infty$ <i>3e4</i>	0/15
Sif	<b>1.8</b> (2)	<b>1.7</b> (2)	<b>2.0</b> (2)	<b>3.0</b> (3)	$\infty$ <i>3e4</i>	0/15
Srr	<b>1.8</b> (2)	<b>1.7</b> (1)	<b>1.9</b> (1)	<b>1.9</b> (1)	$\infty$ <i>3e4</i>	0/15



Table 40: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>1.6e+2</i> :1.6	<i>6.3e+1</i> :5.6	<i>4.0e+1</i> :12	<i>1.6e+1</i> :68	<i>6.3e+0</i> :221	15/15
BSifeg	<b>1.7</b> (2)	<b>1.7</b> (0.9)	<b>2.6</b> (0.4)	43(44)	72(50)	11/15
BSif	<b>1.7</b> (1)	<b>1.7</b> (2)	<b>1.9</b> (4)	44(53)	59(104)	13/15
BSqi	<b>1.7</b> (2)	<b>1.7</b> (1)	3.4(9)	51(119)	64(117)	12/15
BSrr	<b>1.7</b> (2)	<b>1.7</b> (1)	3.3(10)	31(5)	56(96)	13/15
CMA-CSA	<b>3.0</b> (4)	<b>2.7</b> (3)	<b>2.1</b> (1)	<b>1.3</b> (0.5)	<b>0.85</b> (0.5)	15/15
CMA-MSR	<b>1.7</b> (1)	<b>1.6</b> (0.8)	<b>1.4</b> (1)	<b>1.4</b> (1)	3.7(3)	15/15
CMA-TPA	<b>1.9</b> (1)	<b>1.5</b> (2)	<b>2.2</b> (2)	<b>1.4</b> (0.8)	<b>0.91</b> (0.5)	15/15
GP1-CMAES	4.4(3)	<b>2.9</b> (2)	<b>2.3</b> (1)	<b>1.0</b> (0.2)	<b>1.9</b> (2)	11/15
GP5-CMAES	<b>2.8</b> (3)	<b>2.0</b> (1)	<b>1.7</b> (0.7)	<b>0.67</b> (0.8)	<b>1.6</b> (2)	13/15
IPOPCMAv3p	4.2(11)	<b>2.5</b> (3)	<b>1.8</b> (2)	<b>1.4</b> (0.4)	<b>1.1</b> (0.5)	14/15
LHD-10xDef	<b>1.9</b> (1)	<b>2.2</b> (2)	3.3(2)	<b>2.0</b> (1)	3.3(4)	3/15
LHD-2xDefa	<b>2.2</b> (2)	<b>1.3</b> (1)	<b>1.3</b> (1)	<b>0.68</b> (0.4)	<b>1.1</b> (0.7)	7/15
RAND-2xDef	<b>1.4</b> (0.9)	<b>0.99</b> (0.8)	<b>0.98</b> (0.5)	<b>0.74</b> (0.5)	<b>0.57</b> (0.3)	12/15
RF1-CMAES	<b>2.4</b> (3)	<b>2.3</b> (3)	<b>1.7</b> (0.7)	<b>0.79</b> (0.7)	<b>2.0</b> (6)	11/15
RF5-CMAES	<b>2.4</b> (2)	18(3)	13(2)	5.5(9)	11(14)	4/15
Sifeg	<b>1.7</b> (2)	<b>1.6</b> (1)	<b>0.97</b> (0.6)	17(0.3)	36(78)	13/15
Sif	<b>1.7</b> (1)	<b>1.6</b> (1)	<b>0.97</b> (0.4)	23(83)	45(26)	13/15
Srr	<b>1.7</b> (2)	<b>1.6</b> (1.0)	<b>0.95</b> (0.6)	11(0.3)	32(50)	15/15

Table 41: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>6.3e+1:1.5</i>	<i>2.5e+1:8.2</i>	<i>1.6e+1:10</i>	<i>1.0e+1:41</i>	<i>2.5e+0:208</i>	15/15
BSifeg	<b>1.6</b> (1)	<b>1.5</b> (1)	<b>1.9</b> (1.0)	<b>1.6</b> (2)	24(7)	14/15
BSif	<b>1.6</b> (1)	<b>1.5</b> (1)	<b>2.7</b> (7)	<b>2.0</b> (1)	20(41)	15/15
BSqi	<b>1.6</b> (1)	<b>1.5</b> (1)	<b>1.8</b> (1)	<b>2.0</b> (2)	13(23)	15/15
BSrr	<b>1.6</b> (1)	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>1.5</b> (1)	10(2)	15/15
CMA-CSA	<b>2.8</b> (3)	<b>1.5</b> (1)	4.4(5)	<b>1.7</b> (1)	<b>3.0</b> (5)	15/15
CMA-MSR	<b>1.7</b> (1)	3.3(3)	7.7(4)	6.7(11)	4.1(5)	15/15
CMA-TPA	<b>1.7</b> (2)	<b>1.8</b> (2)	3.4(7)	3.2(4)	<b>2.7</b> (4)	15/15
GP1-CMAES	<b>2.0</b> (2)	<b>1.6</b> (2)	<b>2.9</b> (2)	<b>1.3</b> (1)	<b>2.7</b> (6)	10/15
GP5-CMAES	<b>2.1</b> (2)	<b>1.2</b> (2)	<b>1.4</b> (2)	<b>0.78</b> (0.9)	<b>2.1</b> (4)	12/15
IPOPCMAv3p	<b>1.5</b> (1)	<b>1.7</b> (1)	<b>2.2</b> (1)	<b>1.6</b> (2)	<b>1.9</b> (2)	12/15
LHD-10xDef	<b>1.7</b> (1)	<b>0.76</b> (0.8)	<b>2.1</b> (4)	<b>0.99</b> (0.9)	<b>1.0</b> (1.0)	8/15
LHD-2xDefa	<b>1.3</b> (0)	<b>1.1</b> (0.7)	<b>2.6</b> (2)	<b>1.0</b> (1)	<b>0.53</b> (0.5)	11/15
RAND-2xDef	<b>1.9</b> (2)	<b>1.6</b> (1)	<b>1.8</b> (2)	<b>1.4</b> (0.7)	<b>1.0</b> (0.4)	8/15
RF1-CMAES	<b>2.5</b> (4)	<b>1.8</b> (2)	<b>2.8</b> (3)	<b>1.1</b> (1)	<b>2.6</b> (3)	10/15
RF5-CMAES	<b>2.6</b> (2)	<b>1.4</b> (2)	6.4(35)	<b>2.8</b> (0.4)	<b>2.6</b> (4)	10/15
Sifeg	<b>1.6</b> (1)	<b>1.9</b> (2)	<b>2.7</b> (2)	<b>1.1</b> (0.6)	6.3(21)	15/15
Sif	<b>1.6</b> (1)	<b>1.8</b> (2)	<b>2.6</b> (1)	<b>1.0</b> (0.7)	3.6(4)	15/15
Srr	<b>1.6</b> (1)	<b>1.9</b> (2)	3.0(1)	<b>1.2</b> (0.7)	4.2(8)	15/15

Table 42: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.6e+1</i> :1.8	<i>1.0e+1</i> :3.6	<i>6.3e+0</i> :14	<i>2.5e+0</i> :34	<i>2.5e-1</i> :189	5/5
BSifeg	4.3(11)	3.6(1)	<b>1.4</b> (3)	30(105)	107(81)	10/15
BSif	3.3(11)	<b>2.9</b> (2)	<b>1.2</b> (0.2)	18(65)	114(177)	10/15
BSqi						

Table 43: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>6.3e+1</i> :1.8	<i>4.0e+1</i> :4.8	<i>2.5e+1</i> :13	<i>1.0e+1</i> :40	<i>6.3e-1</i> :184	15/15
BSifeg	<b>2.7</b> (2)	<b>1.9</b> (2)	<b>1.5</b> (2)	<b>1.6</b> (0.3)	334(420)	5/15
BSif	<b>2.7</b> (3)	<b>1.9</b> (1)	<b>1.5</b> (3)	<b>1.3</b> (2)	218(273)	7/15
BSqi	<b>2.7</b> (2)	<b>1.9</b> (2)	<b>1.5</b> (2)	<b>1.1</b> (3)	158(197)	9/15
BSrr	<b>2.7</b> (2)	<b>1.9</b> (2)	<b>1.3</b> (0.8)	17(60)	187(356)	7/15
CMA-CSA	3.9(4)	<b>2.7</b> (2)	<b>1.7</b> (2)	<b>1.4</b> (1)	<b>3.6</b> (1)	15/15
CMA-MSR	4.6(5)	<b>2.7</b> (4)	<b>1.8</b> (2)	<b>1.4</b> (1.0)	4.7(17)	15/15
CMA-TPA	6.1(9)	3.7(5)	<b>2.4</b> (1)	<b>1.7</b> (1)	<b>3.8</b> (2)	15/15
GP1-CMAES	4.2(4)	<b>2.2</b> (0.8)	<b>1.7</b> (2)	<b>1.3</b> (0.5)	3.8(7)	9/15
GP5-CMAES	5.8(4)	14(78)	14(21)	5.6(12)	<b>2.7</b> (3)	11/15
IPOPCMAv3p	3.3(3)	4.2(4)	<b>2.6</b> (1)	<b>1.7</b> (3)	5.4(4)	8/15
LHD-10xDef	<b>2.9</b> (4)	<b>1.6</b> (2)	<b>1.4</b> (2)	<b>2.1</b> (0.2)	12(15)	1/15
LHD-2xDefa	<b>2.6</b> (0.8)	<b>1.8</b> (1)	<b>1.2</b> (0.7)	<b>0.93</b> (0.6)	3.9(5)	3/15
RAND-2xDef	3.4(3)	<b>2.0</b> (2)	<b>1.3</b> (1)	<b>0.97</b> (1)	6.0(7)	2/15
RF1-CMAES	4.4(9)	3.3(4)	5.6(2)	7.7(19)	17(16)	3/15
RF5-CMAES	3.5(3)	<b>2.1</b> (0.8)	<b>1.1</b> (1)	5.1(5)	58(77)	1/15
Sifeg	<b>2.7</b> (3)	<b>2.1</b> (1)	<b>1.8</b> (3)	<b>1.5</b> (1)	139(166)	10/15
Sif	<b>2.7</b> (3)	<b>2.1</b> (1)	4.8(15)	3.7(0.9)	153(143)	9/15
Srr	<b>2.7</b> (3)	<b>2.1</b> (1)	<b>1.7</b> (1)	<b>1.2</b> (1)	94(119)	11/15

Table 44: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:81</i>	<i>1.0e-1:109</i>	<i>6.3e-2:109</i>	<i>4.0e-2:119</i>	<i>1.6e-2:1230</i>	15/15
BSifeg	<b>12</b> <sup>(18)</sup>	<b>17</b> <sup>(46)</sup>	<b>35</b> <sup>(50)</sup>	<b>62</b> <sup>(61)</sup>	54 <sup>(36)</sup>	5/15
BSif	<b>19</b> <sup>(18)</sup>	<b>36</b> <sup>(58)</sup>	<b>66</b> <sup>(179)</sup>	<b>139</b> <sup>(103)</sup>	<b>42</b> <sup>(51)</sup>	6/15
BSqi	19 <sup>(10)</sup>	45 <sup>(15)</sup>	62 <sup>(56)</sup>	<b>99</b> <sup>(193)</sup>	<b>37</b> <sup>(64)</sup>	7/15
BSrr	<b>23</b> <sup>(24)</sup>	<b>33</b> <sup>(51)</sup>	<b>78</b> <sup>(127)</sup>	<b>149</b> <sup>(256)</sup>	<b>115</b> <sup>(55)</sup>	3/15
CMA-CSA	30 <sup>(31)</sup>	39 <sup>(48)</sup>	59 <sup>(54)</sup>	<b>59</b> <sup>(45)</sup>	<b>12</b> <sup>(14)</sup>	15/15
CMA-MSR	69 <sup>(83)</sup>	96 <sup>(148)</sup>	274 <sup>(546)</sup>	<b>677</b> <sup>(1164)</sup>	131 <sup>(193)</sup>	12/15
CMA-TPA	28 <sup>(15)</sup>	41 <sup>(49)</sup>	<b>46</b> <sup>(68)</sup>	<b>66</b> <sup>(55)</sup>	<b>7.5</b> <sup>(4)</sup>	15/15
GP1-CMAES	43 <sup>(31)</sup>	48 <sup>(31)</sup>	<b>48</b> <sup>(21)</sup>	92 <sup>(129)</sup>	$\infty$ <i>753</i>	0/15
GP5-CMAES	68 <sup>(48)</sup>	104 <sup>(86)</sup>	104 <sup>(117)</sup>	$\infty$	$\infty$ <i>762</i>	0/15
IPOPCMAv3p	28 <sup>(47)</sup>	$\infty$	$\infty$	$\infty$	$\infty$ <i>751</i>	0/15
LHD-10xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
LHD-2xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
RAND-2xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>150</i>	0/15
RF1-CMAES	23 <sup>(22)</sup>	24 <sup>(13)</sup>	100 <sup>(105)</sup>	93 <sup>(87)</sup>	$\infty$ <i>751</i>	0/15
RF5-CMAES	44 <sup>(61)</sup>	$\infty$	$\infty$	$\infty$	$\infty$ <i>755</i>	0/15
Sifeg	22 <sup>(25)</sup>	<b>19</b> <sup>(33)</sup>	70 <sup>(135)</sup>	176 <sup>(205)</sup>	170 <sup>(346)</sup>	2/15
Sif	20 <sup>(51)</sup>	36 <sup>(61)</sup>	54 <sup>(96)</sup>	169 <sup>(173)</sup>	48 <sup>(76)</sup>	6/15
Srr	<b>15</b> <sup>(23)</sup>	<b>21</b> <sup>(35)</sup>	62 <sup>(95)</sup>	133 <sup>(119)</sup>	48 <sup>(14)</sup>	6/15

Table 45: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f20</i></b>	<i>4.0e+3:3.5</i>	<i>2.5e+3:4.3</i>	<i>4.0e+0:13</i>	<i>1.6e+0:41</i>	<i>1.0e+0:385</i>	5/5
BSifeg	<b>2.4</b> (2)	<b>2.2</b> (2)	4.4(0.2)	5.3(6)	13(24)	15/15
BSif	<b>2.4</b> (2)	<b>2.2</b> (2)	4.0(9)	6.4(9)	17(13)	15/15
BSqi	<b>2.4</b> (2)	<b>2.2</b> (2)	<b>2.8</b> (5)	5.4(6)	11(16)	15/15
BSrr	<b>2.4</b> (2)	<b>2.2</b> (2)	<b>2.0</b> (1)	4.7(6)	14(27)	14/15
CMA-CSA	<b>2.0</b> (2)	<b>1.6</b> (2)	<b>2.2</b> (1.0)	11(13)	<b>4.5</b> (2)	15/15
CMA-MSR	<b>1.7</b> (0.5)	<b>1.7</b> (2)	<b>2.6</b> (2)	20(35)	13(16)	15/15
CMA-TPA	<b>1.7</b> (1)	<b>2.4</b> (2)	<b>2.9</b> (1)	10(10)	7.6(10)	15/15
GP1-CMAES	<b>2.0</b> (3)	<b>1.8</b> (0.6)	<b>2.4</b> (2)	8.6(15)	<b>3.7</b> (2)	6/15
GP5-CMAES	<b>1.2</b> (0.6)	<b>1.2</b> (2)	<b>2.0</b> (1)	5.4(5)	<b>2.0</b> (3)	9/15
IPOPCMAv3p	<b>1.4</b> (1)	<b>1.5</b> (1)	<b>2.8</b> (2)	12(18)	4.5(9)	5/15
LHD-10xDef	<b>0.79</b> (0.5)	<b>1.1</b> (2)	4.3(3)	$\infty$	$\infty$ 150	0/15
LHD-2xDefa	<b>1.4</b> (1)	<b>1.3</b> (0.9)	<b>1.8</b> (1)	17(17)	$\infty$ 150	0/15
RAND-2xDef	<b>1.2</b> (2)	<b>1.4</b> (2)	<b>1.9</b> (1)	13(15)	$\infty$ 150	0/15
RF1-CMAES	<b>1.6</b> (2)	<b>1.7</b> (0.9)	6.4(13)	17(9)	5.9(6)	4/15
RF5-CMAES	<b>1.8</b> (2)	<b>2.0</b> (2)	33(24)	63(42)	$\infty$ 760	0/15
Sifeg	<b>2.5</b> (2)	<b>2.3</b> (2)	<b>2.0</b> (1.0)	<b>3.3</b> (4)	7.3(9)	15/15
Sif	<b>2.5</b> (2)	<b>2.3</b> (2)	<b>2.2</b> (3)	<b>3.8</b> (3)	10(25)	15/15
Srr	<b>2.5</b> (2)	<b>2.3</b> (1.0)	<b>1.9</b> (0.7)	<b>2.7</b> (0.9)	9.0(26)	15/15

Table 46: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f21</b>	<i>1.6e+1:2.5</i>	<i>1.0e+1:5.9</i>	<i>6.3e+0:14</i>	<i>2.5e+0:41</i>	<i>1.6e+0:167</i>	15/15
BSifeg	<b>2.8</b> (3)	<b>1.6</b> (1)	152(524)	117(70)	84(90)	12/15
BSif	<b>2.8</b> (3)	<b>1.6</b> (1)	152(7)	249(439)	114(154)	10/15
BSqi	<b>2.8</b> (2)	<b>1.6</b> (1)	152(521)	167(259)	150(139)	9/15
BSrr	<b>2.8</b> (3)	<b>1.6</b> (1)	150(0.9)	113(46)	130(135)	10/15
CMA-CSA	<b>2.2</b> (3)	<b>1.3</b> (1)	5.8(17)	5.1(1)	6.9(3)	15/15
CMA-MSR	<b>2.9</b> (5)	<b>2.1</b> (2)	<b>2.8</b> (5)	6.7(1.0)	5.9(8)	15/15
CMA-TPA	<b>2.7</b> (3)	<b>1.6</b> (2)	<b>2.3</b> (4)	<b>1.6</b> (2)	<b>1.9</b> (3)	15/15
GP1-CMAES	<b>1.1</b> (2)	<b>0.93</b> (0.8)	4.9(28)	5.3(19)	7.1(8)	6/15
GP5-CMAES	<b>2.2</b> (2)	<b>1.4</b> (2)	<b>1.3</b> (1)	<b>1.2</b> (0.5)	<b>2.4</b> (2)	11/15
IPOPCMAv3p	<b>2.5</b> (3)	<b>1.9</b> (1)	<b>1.4</b> (2)	<b>1.6</b> (1)	<b>2.5</b> (2)	11/15
LHD-10xDef	<b>1.2</b> (0.8)	<b>1.7</b> (2)	<b>1.3</b> (2)	<b>1.4</b> (0.9)	<b>0.66</b> (0.2)	14/15
LHD-2xDefa	<b>2.2</b> (2)	<b>1.3</b> (0.8)	<b>1.6</b> (2)	<b>1.1</b> (0.7)	<b>0.89</b> (1)	10/15
RAND-2xDef	<b>1.5</b> (0.6)	<b>1.2</b> (2)	<b>1.1</b> (0.8)	<b>1.1</b> (1)	<b>0.80</b> (0.8)	10/15
RF1-CMAES	<b>2.3</b> (2)	<b>2.1</b> (2)	<b>1.9</b> (1)	<b>2.5</b> (9)	4.4(8)	8/15
RF5-CMAES	<b>1.9</b> (2)	<b>1.9</b> (1)	5.8(0.7)	5.2(6)	7.3(11)	7/15
Sifeg	<b>2.8</b> (3)	<b>1.9</b> (2)	151(522)	92(561)	95(145)	11/15
Sif	<b>2.8</b> (3)	<b>2.1</b> (2)	152(523)	101(1)	104(204)	10/15
Srr	<b>2.8</b> (3)	<b>1.9</b> (2)	151(522)	62(183)	142(147)	9/15

Table 47: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f22</b>	<i>4.0e+1:2.9</i>	<i>2.5e+1:5.2</i>	<i>1.0e+1:18</i>	<i>6.3e+0:33</i>	<i>1.0e+0:170</i>	5/5
BSifeg	<b>3.0</b> (2)	<b>2.1</b> (3)	7.6(2)	79(214)	87(138)	11/15
BSif	<b>2.6</b> (2)	<b>2.0</b> (2)	10(30)	171(237)	219(410)	7/15
BSqi	3.1(3)	<b>2.2</b> (3)	4.8(6)	85(265)	130(261)	10/15
BSrr	3.2(6)	<b>2.2</b> (5)	3.9(9)	87(180)	146(210)	9/15
CMA-CSA	<b>1.8</b> (2)	<b>1.7</b> (2)	<b>1.4</b> (1)	3.0(7)	11(20)	15/15
CMA-MSR	<b>2.0</b> (1)	<b>2.3</b> (3)	<b>2.0</b> (2)	6.8(1)	5.9(25)	15/15
CMA-TPA	<b>1.8</b> (2)	<b>2.0</b> (4)	<b>1.8</b> (3)	<b>1.5</b> (2)	19(50)	15/15
GP1-CMAES	<b>1.4</b> (0.9)	<b>2.0</b> (1)	<b>1.7</b> (2)	5.2(12)	3.8(9)	9/15
GP5-CMAES	<b>1.5</b> (1)	<b>1.5</b> (3)	4.2(3)	6.4(6)	10(15)	5/15
IPOPCMAv3p	<b>2.7</b> (3)	<b>2.6</b> (3)	<b>2.1</b> (1)	<b>1.8</b> (0.9)	10(24)	5/15
LHD-10xDef	<b>2.8</b> (2)	<b>2.1</b> (1)	<b>1.7</b> (1)	<b>1.9</b> (1)	<b>0.88</b> (0.9)	11/15
LHD-2xDefa	<b>1.4</b> (1)	<b>1.7</b> (0.9)	<b>1.4</b> (0.7)	<b>1.4</b> (1.0)	<b>2.2</b> (3)	5/15
RAND-2xDef	<b>1.6</b> (0.6)	<b>2.2</b> (1)	<b>0.97</b> (0.6)	<b>1.3</b> (1)	<b>1.1</b> (1.0)	9/15
RF1-CMAES	<b>1.1</b> (1)	<b>0.96</b> (0.5)	<b>1.7</b> (1)	7.1(24)	5.5(8)	7/15
RF5-CMAES	12(1)	14(0.8)	6.9(19)	10(27)	11(11)	5/15
Sifeg	<b>2.3</b> (3)	<b>1.8</b> (2)	<b>1.8</b> (3)	31(3)	61(62)	13/15
Sif	<b>2.3</b> (3)	<b>1.8</b> (3)	3.2(8)	45(12)	67(162)	12/15
Srr	<b>2.3</b> (2)	<b>1.8</b> (1)	<b>1.5</b> (4)	<b>1.6</b> (2)	66(172)	12/15



Table 48: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>1.0e+1:2.6</i>	<i>6.3e+0:16</i>	<i>4.0e+0:44</i>	<i>2.5e+0:79</i>	<i>1.6e+0:198</i>	15/15
BSifeg	3.8(2)	<b>1.4</b> (1)	<b>1.2</b> (1)	<b>2.2</b> (4)	<b>1.5</b> (2)	15/15
BSif	3.8(2)	<b>1.4</b> (1)	<b>1.6</b> (2)	<b>2.7</b> (3)	<b>2.0</b> (2)	15/15
BSqi	3.7(3)	<b>1.2</b> (1)	<b>1.1</b> (2)	<b>1.8</b> (3)	<b>1.4</b> (1)	15/15
BSrr	3.9(3)	<b>1.4</b> (1)	<b>1.4</b> (1)	<b>1.6</b> (1)	<b>1.3</b> (1)	15/15
CMA-CSA	<b>3.3</b> (6)	<b>1.5</b> (2)	<b>1.4</b> (2)	<b>2.8</b> (2)	8.5(9)	15/15
CMA-MSR	<b>2.6</b> (2)	<b>2.2</b> (1)	3.4(2)	5.6(4)	4.8(7)	15/15
CMA-TPA	4.2(6)	3.3(6)	7.6(3)	6.5(3)	4.2(2)	15/15
GP1-CMAES	<b>3.3</b> (4)	<b>1.7</b> (0.7)	<b>2.3</b> (2)	3.5(4)	4.3(6)	10/15
GP5-CMAES	5.7(7)	<b>1.7</b> (2)	<b>2.1</b> (4)	<b>2.1</b> (2)	<b>1.3</b> (1)	14/15
IPOPCMAv3p	4.3(7)	<b>1.5</b> (2)	<b>1.7</b> (2)	3.1(4)	4.7(4)	9/15
LHD-10xDef	6.4(3)	<b>2.0</b> (2)	<b>2.3</b> (1)	8.5(9)	11(20)	1/15
LHD-2xDefa	4.0(4)	<b>1.3</b> (0.8)	3.6(5)	3.5(6)	$\infty$ 150	0/15
RAND-2xDef	4.5(4)	<b>2.7</b> (4)	<b>2.9</b> (3)	7.7(8)	11(14)	1/15
RF1-CMAES	5.1(3)	<b>1.7</b> (1)	<b>1.9</b> (1)	<b>2.5</b> (4)	6.9(5)	6/15
RF5-CMAES	3.5(2)	<b>1.4</b> (1)	<b>1.6</b> (1)	5.4(7)	7.9(6)	6/15
Sifeg	3.7(4)	<b>1.9</b> (2)	<b>2.3</b> (2)	3.9(2)	<b>2.9</b> (2)	15/15
Sif	3.7(2)	<b>1.7</b> (3)	<b>2.3</b> (2)	3.8(3)	<b>2.8</b> (1)	15/15
Srr	3.7(4)	<b>1.7</b> (3)	<b>2.2</b> (2)	3.9(2)	<b>2.3</b> (1)	15/15

Table 49: 03-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f24</i></b>	<i>4.0e+1:4.6</i>	<i>2.5e+1:13</i>	<i>1.6e+1:47</i>	<i>1.6e+1:47</i>	<i>6.3e+0:382</i>	15/15
BSifeg	<b>1.5</b> (1)	<b>2.2</b> (0.5)	<b>2.5</b> (4)	<b>2.5</b> (4)	17(35)	14/15
BSif	<b>1.6</b> (0.5)	<b>2.4</b> (1)	<b>2.3</b> (1)	<b>2.3</b> (2)	24(49)	12/15
BSqi	<b>1.6</b> (1)	<b>1.7</b> (1)	<b>2.6</b> (3)	<b>2.6</b> (1)	13(29)	14/15
BSrr	<b>1.5</b> (1)	<b>1.7</b> (0.7)	<b>2.5</b> (5)	<b>2.5</b> (4)	8.1(21)	15/15
CMA-CSA	<b>1.8</b> (2)	<b>2.1</b> (2)	<b>1.5</b> (0.5)	<b>1.5</b> (0.9)	<b>2.0</b> (3)	15/15
CMA-MSR	<b>1.7</b> (0.8)	<b>2.6</b> (2)	<b>1.6</b> (0.9)	<b>1.6</b> (2)	3.4(4)	15/15
CMA-TPA	<b>1.4</b> (1)	<b>2.0</b> (1)	<b>1.3</b> (2)	<b>1.3</b> (0.3)	<b>2.0</b> (0.7)	15/15
GP1-CMAES	<b>2.2</b> (2)	<b>2.2</b> (1)	<b>1.7</b> (0.8)	<b>1.7</b> (0.9)	<b>2.0</b> (3)	9/15
GP5-CMAES	<b>1.5</b> (2)	<b>2.4</b> (2)	<b>1.2</b> (1)	<b>1.2</b> (2)	<b>2.3</b> (4)	8/15
IPOPCMAv3p	<b>2.0</b> (2)	<b>2.3</b> (3)	<b>1.8</b> (1)	<b>1.8</b> (1)	<b>1.5</b> (0.9)	12/15
LHD-10xDef	<b>2.1</b> (2)	3.3(3)	3.0(4)	3.0(4)	5.8(5)	1/15
LHD-2xDefa	<b>1.2</b> (2)	<b>2.2</b> (3)	<b>1.7</b> (0.7)	<b>1.7</b> (2)	5.6(9)	1/15
RAND-2xDef	<b>0.93</b> (1)	<b>2.3</b> (1)	<b>2.2</b> (3)	<b>2.2</b> (0.9)	5.7(8)	1/15
RF1-CMAES	<b>1.9</b> (4)	<b>2.4</b> (2)	<b>1.3</b> (0.8)	<b>1.3</b> (0.7)	<b>1.6</b> (1)	10/15
RF5-CMAES	<b>1.2</b> (1)	<b>1.3</b> (0.8)	5.2(5)	5.2(11)	<b>2.3</b> (3)	9/15
Sifeg	<b>1.4</b> (2)	<b>1.7</b> (0.6)	<b>1.3</b> (0.9)	<b>1.3</b> (1)	6.1(34)	14/15
Sif	<b>1.4</b> (1)	<b>1.6</b> (0.6)	<b>1.4</b> (1)	<b>1.4</b> (1)	6.2(3)	15/15
Srr	<b>1.4</b> (2)	<b>1.8</b> (1.0)	<b>1.3</b> (0.6)	<b>1.3</b> (0.6)	11(34)	14/15

Table 50: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>2.5e+1</i> :4.8	<i>1.6e+1</i> :7.6	<i>1.0e-8</i> :12	<i>1.0e-8</i> :12	<i>1.0e-8</i> :12	15/15
BSifeg	<b>1.8</b> (2)	<b>1.7</b> (0.8)	<b>2.2</b> (0.1)	<b>2.2</b> (0.1)	<b>2.2</b> (0.1)	15/15
BSif	<b>1.8</b> (2)	<b>1.7</b> (1)	<b>2.2</b> (0.2)	<b>2.2</b> (0.1)	<b>2.2</b> (0.2)	15/15
BSqi	<b>1.8</b> (2)	<b>1.7</b> (1)	<b>2.2</b> (0.1)	<b>2.2</b> (0.1)	<b>2.2</b> (0.2)	15/15
BSrr	<b>1.8</b> (2)	<b>1.7</b> (0.9)	<b>2.2</b> (0.0)	<b>2.2</b> (0.2)	<b>2.2</b> (0.2)	15/15
CMA-CSA	4.3(3)	3.6(2)	58(5)	58(2)	58(5)	15/15
CMA-MSR	3.0(2)	3.1(3)	90(7)	90(9)	90(9)	15/15
CMA-TPA	<b>2.7</b> (4)	<b>2.5</b> (3)	52(9)	52(4)	52(10)	15/15
GP1-CMAES	<b>2.5</b> (2)	<b>2.2</b> (2)	36(6)	36(5)	36(5)	15/15
GP5-CMAES	<b>2.3</b> (2)	<b>2.1</b> (1)	92(54)	92(86)	92(122)	11/15
IPOPCMAv3p	3.0(4)	<b>2.9</b> (4)	59(5)	59(9)	59(7)	15/15
LHD-10xDef	<b>2.8</b> (1)	3.8(6)	$\infty$	$\infty$	$\infty$ 250	0/15
LHD-2xDefa	<b>2.6</b> (2)	<b>2.8</b> (1)	$\infty$	$\infty$	$\infty$ 250	0/15
RAND-2xDef	<b>2.0</b> (1)	<b>2.2</b> (1)	$\infty$	$\infty$	$\infty$ 250	0/15
RF1-CMAES	3.7(3)	<b>3.0</b> (1)	1520(1031)	1520(2191)	1520(799)	1/15
RF5-CMAES	<b>2.2</b> (3)	<b>2.4</b> (1)	$\infty$	$\infty$	$\infty$ 1252	0/15
Sifeg	<b>1.8</b> (2)	<b>1.7</b> (1)	8.9(0.9)	8.9(1.0)	8.9(1)	15/15
Sif	<b>1.8</b> (2)	<b>1.7</b> (0.7)	8.7(1)	8.7(1)	8.7(0.9)	15/15
Srr	<b>1.8</b> (1)	<b>1.7</b> (1)	8.4(1)	8.4(1)	8.4(1)	15/15

Table 51: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>1.6e+6</i> :2.9	<i>4.0e+5</i> :11	<i>4.0e+4</i> :15	<i>6.3e+2</i> :58	<i>1.0e-8</i> :95	15/15
BSifeg	6.0(3)	<b>1.8</b> (1)	<b>1.5</b> (0.2)	<b>0.52</b> (0.2)	<b>1.1</b> (0.1)	15/15
BSif	6.0(4)	<b>1.8</b> (1)	<b>1.5</b> (0.2)	<b>0.53</b> (0.3)	<b>1.1</b> (0.2)	15/15
BSqi	6.0(4)	<b>1.8</b> (1)	<b>1.5</b> (0.2)	<b>0.49</b> (0.1)	<b>0.92</b> (0.2)	15/15
BSrr	6.0(2)	<b>1.8</b> (1)	<b>1.5</b> (0.2)	<b>0.52</b> (0.2)	<b>1.1</b> (0.2)	15/15
CMA-CSA	<b>2.3</b> (2)	<b>1.8</b> (2)	6.1(4)	7.5(2)	18(0.9)	15/15
CMA-MSR	<b>2.5</b> (2)	<b>1.9</b> (2)	5.9(4)	7.4(3)	21(1)	15/15
CMA-TPA	3.7(6)	<b>2.1</b> (2)	3.9(3)	7.7(3)	18(3)	15/15
GP1-CMAES	<b>2.1</b> (1.0)	<b>1.9</b> (2)	4.0(3)	5.8(4)	$\infty$ <i>1258</i>	0/15
GP5-CMAES	<b>2.5</b> (3)	<b>1.7</b> (2)	3.2(1)	<b>2.7</b> (1)	94(92)	2/15
IPOPCMAv3p	3.1(4)	<b>1.5</b> (2)	5.6(3)	10(9)	$\infty$ <i>1258</i>	0/15
LHD-10xDef	<b>1.1</b> (0.7)	<b>1.2</b> (2)	8.4(6)	65(37)	$\infty$ <i>250</i>	0/15
LHD-2xDefa	<b>1.3</b> (1)	<b>0.79</b> (2)	4.3(2)	32(47)	$\infty$ <i>250</i>	0/15
RAND-2xDef	<b>1.6</b> (1)	<b>1.0</b> (0.6)	3.3(2)	62(33)	$\infty$ <i>250</i>	0/15
RF1-CMAES	<b>2.9</b> (4)	<b>2.7</b> (2)	6.8(5)	51(50)	$\infty$ <i>1258</i>	0/15
RF5-CMAES	<b>2.1</b> (1)	7.1(23)	25(29)	$\infty$	$\infty$ <i>1260</i>	0/15
Sifeg	6.4(4)	<b>2.0</b> (1)	<b>2.1</b> (0.6)	<b>0.84</b> (0.2)	<b>1.4</b> (0.1)	15/15
Sif	6.4(2)	<b>2.0</b> (0.2)	<b>2.1</b> (0.6)	<b>0.82</b> (0.1)	<b>1.4</b> (0.3)	15/15
Srr	6.4(3)	<b>2.0</b> (0.6)	<b>2.1</b> (0.5)	<b>0.79</b> (0.1)	<b>1.5</b> (0.2)	15/15

Table 52: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>1.6e+2:4.1</i>	<i>1.0e+2:15</i>	<i>6.3e+1:23</i>	<i>2.5e+1:73</i>	<i>1.0e+1:716</i>	15/15
BSifeg	<b>2.6</b> (2)	<b>1.2</b> (0.2)	<b>0.98</b> (0.1)	<b>0.46</b> (0.1)	<b>0.11</b> (0.1)	15/15
BSif	<b>2.6</b> (2)	<b>1.2</b> (0.2)	<b>0.98</b> (0.1)	<b>0.46</b> (0.1)	<b>0.11</b> (0.0)	15/15
BSqi	<b>2.6</b> (2)	<b>1.2</b> (0.5)	<b>0.98</b> (0.1)	<b>0.46</b> (0.1)	<b>0.10</b> (0.1)	15/15
BSrr	<b>2.6</b> (2)	<b>1.2</b> (0.4)	<b>0.98</b> (0.1)	<b>0.46</b> (0.1)	<b>0.09</b> (0.1)	15/15
CMA-CSA	4.2(5)	<b>2.4</b> (2)	<b>2.6</b> (2)	<b>2.5</b> (1)	<b>1.4</b> (0.3)	15/15
CMA-MSR	3.3(3)	<b>2.4</b> (1)	3.4(2)	6.7(14)	<b>1.7</b> (2)	15/15
CMA-TPA	3.5(7)	<b>2.2</b> (1)	<b>2.6</b> (2)	<b>2.5</b> (1)	<b>0.81</b> (0.7)	15/15
GP1-CMAES	<b>2.8</b> (3)	<b>1.5</b> (2)	<b>2.3</b> (0.7)	<b>2.5</b> (5)	<b>1.6</b> (1)	11/15
GP5-CMAES	3.0(2)	<b>1.3</b> (0.9)	<b>1.6</b> (1)	<b>2.2</b> (0.5)	<b>2.6</b> (3)	8/15
IPOPCMAv3p	<b>2.7</b> (2)	<b>1.4</b> (2)	<b>2.5</b> (0.8)	3.1(1)	<b>1.1</b> (0.9)	12/15
LHD-10xDef	<b>2.1</b> (3)	<b>2.8</b> (2)	3.7(2)	3.6(0.5)	<b>1.0</b> (0.8)	5/15
LHD-2xDefa	<b>2.1</b> (2)	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>2.1</b> (3)	<b>2.5</b> (4)	2/15
RAND-2xDef	<b>2.3</b> (2)	<b>1.4</b> (1)	<b>1.6</b> (0.4)	<b>2.2</b> (0.5)	<b>0.58</b> (0.3)	7/15
RF1-CMAES	<b>1.9</b> (3)	<b>1.6</b> (1)	<b>2.2</b> (0.8)	<b>2.4</b> (1)	3.0(3)	6/15
RF5-CMAES	3.4(3)	<b>1.6</b> (1)	4.6(19)	14(15)	6.1(7)	4/15
Sifeg	<b>2.6</b> (2)	<b>1.2</b> (0.5)	<b>0.99</b> (0.1)	<b>0.57</b> (0.4)	<b>0.13</b> (0.1)	15/15
Sif	<b>2.6</b> (2)	<b>1.2</b> (0.3)	<b>0.99</b> (0.1)	<b>0.57</b> (0.2)	<b>0.13</b> (0.1)	15/15
Srr	<b>2.6</b> (2)	<b>1.2</b> (0.3)	<b>0.99</b> (0.2)	<b>0.56</b> (0.1)	<b>0.12</b> (0.0)	15/15

Table 53: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>2.5e+2</i> :2.6	<i>1.6e+2</i> :10	<i>1.0e+2</i> :19	<i>4.0e+1</i> :65	<i>1.6e+1</i> :434	15/15
BSifeg	<b>2.1</b> (2)	<b>0.90</b> (0.8)	<b>1.4</b> (0.8)	<b>1.0</b> (0.6)	<b>0.25</b> (0.1)	15/15
BSif	<b>2.1</b> (3)	<b>0.90</b> (0.7)	<b>1.4</b> (0.5)	<b>1.1</b> (0.5)	<b>0.26</b> (0.1)	15/15
BSqi	<b>2.1</b> (2)	<b>0.90</b> (1)	<b>1.3</b> (0.4)	<b>1.3</b> (0.8)	<b>0.28</b> (0.2)	15/15
BSrr	<b>2.1</b> (2)	<b>0.90</b> (0.9)	<b>1.3</b> (1.0)	<b>1.1</b> (0.4)	<b>0.23</b> (0.1)	15/15
CMA-CSA	4.6(9)	<b>2.9</b> (4)	3.0(2)	4.3(1)	<b>2.3</b> (3)	15/15
CMA-MSR	4.2(6)	<b>2.7</b> (4)	<b>2.3</b> (1)	<b>2.8</b> (2)	<b>2.0</b> (3)	15/15
CMA-TPA	4.7(5)	<b>2.5</b> (1)	3.4(2)	<b>3.0</b> (2)	<b>2.4</b> (2)	15/15
GP1-CMAES	<b>2.7</b> (2)	<b>2.4</b> (2)	<b>2.6</b> (3)	5.1(8)	3.2(2)	9/15
GP5-CMAES	<b>1.6</b> (1)	<b>1.6</b> (1)	<b>3.0</b> (2)	5.2(6)	7.5(7)	5/15
IPOPCMAv3p	<b>2.3</b> (3)	<b>1.5</b> (1)	<b>2.4</b> (1)	<b>2.4</b> (1)	<b>1.2</b> (0.9)	14/15
LHD-10xDef	3.9(2)	3.2(3)	5.1(3)	8.3(6)	$\infty$ 250	0/15
LHD-2xDefa	<b>2.2</b> (3)	<b>1.5</b> (1)	3.0(2)	6.8(11)	$\infty$ 250	0/15
RAND-2xDef	<b>2.8</b> (3)	<b>2.2</b> (2)	3.1(2)	4.2(3)	8.4(13)	1/15
RF1-CMAES	<b>2.4</b> (3)	<b>1.9</b> (0.8)	<b>2.5</b> (2)	7.9(10)	12(20)	3/15
RF5-CMAES	<b>2.7</b> (4)	<b>1.9</b> (1)	4.9(11)	31(26)	$\infty$ 1252	0/15
Sifeg	<b>2.1</b> (2)	<b>0.92</b> (1.0)	<b>1.3</b> (0.4)	<b>0.85</b> (0.3)	<b>0.21</b> (0.1)	15/15
Sif	<b>2.1</b> (3)	<b>0.92</b> (0.7)	<b>1.3</b> (0.5)	<b>0.85</b> (0.3)	<b>0.21</b> (0.1)	15/15
Srr	<b>2.1</b> (2)	<b>0.92</b> (1)	<b>1.3</b> (0.8)	<b>0.83</b> (0.2)	<b>0.20</b> (0.0)	15/15

Table 54: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f5</b>	<i>6.3e+1</i> :4.0	<i>4.0e+1</i> :10	<i>1.0e-8</i> :10	<i>1.0e-8</i> :10	<i>1.0e-8</i> :10	15/15
BSifeg	<b>2.9</b> (0.7)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
BSif	<b>2.9</b> (0.4)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
BSqi	<b>2.9</b> (0.9)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
BSrr	<b>2.9</b> (0.4)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
CMA-CSA	<b>1.9</b> (2)	<b>1.8</b> (0.7)	5.2(2)	5.2(2)	5.2(2)	15/15
CMA-MSR	<b>2.2</b> (2)	<b>1.8</b> (1)	5.9(3)	5.9(2)	5.9(1)	15/15
CMA-TPA	<b>2.6</b> (3)	<b>1.9</b> (2)	5.1(2)	5.1(2)	5.1(2)	15/15
GP1-CMAES	<b>2.0</b> (2)	<b>1.5</b> (1.0)	26(9)	26(20)	26(37)	15/15
GP5-CMAES	3.0(1)	<b>1.7</b> (0.1)	6.4(4)	6.4(4)	6.4(3)	15/15
IPOPCMAv3p	3.0(3)	<b>2.2</b> (1)	21(12)	21(20)	21(14)	15/15
LHD-10xDef	3.2(5)	4.6(5)	13(0.2)	13(0.2)	13(0.2)	15/15
LHD-2xDefa	<b>1.9</b> (1)	<b>1.8</b> (1)	3.5(2)	3.5(2)	3.5(3)	15/15
RAND-2xDef	<b>2.0</b> (2)	<b>2.0</b> (1.0)	3.1(0.2)	3.1(0.2)	3.1(0.2)	15/15
RF1-CMAES	<b>2.3</b> (2)	<b>1.7</b> (0.9)	45(26)	45(35)	45(26)	15/15
RF5-CMAES	<b>2.8</b> (3)	<b>1.9</b> (2)	137(220)	137(56)	137(117)	10/15
Sifeg	<b>2.9</b> (0.8)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
Sif	<b>2.9</b> (0.3)	<b>1.4</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15
Srr	<b>2.9</b> (0.8)	<b>1.4</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	<b>1.5</b> (0.1)	15/15

Table 55: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>1.0e+5</i> :3.0	<i>2.5e+4</i> :8.4	<i>1.0e+2</i> :16	<i>2.5e+1</i> :54	<i>2.5e-1</i> :254	15/15
BSifeg	<b>1.2</b> (0.9)	<b>1.2</b> (0.8)	<b>2.3</b> (3)	66(371)	210(215)	9/15
BSif	<b>1.2</b> (1)	<b>1.2</b> (1.0)	<b>2.9</b> (6)	79(83)	1315(1887)	2/15
BSqi	<b>1.2</b> (2)	<b>1.2</b> (0.8)	3.6(0.8)	71(214)	228(417)	8/15
BSrr	<b>1.2</b> (2)	<b>1.2</b> (1)	<b>2.3</b> (1)	66(403)	226(149)	8/15
CMA-CSA	<b>2.0</b> (2)	<b>1.6</b> (0.9)	<b>2.9</b> (1)	<b>2.7</b> (2)	<b>1.9</b> (0.5)	15/15
CMA-MSR	3.2(3)	<b>1.9</b> (1)	3.5(4)	3.3(1)	<b>2.1</b> (0.5)	15/15
CMA-TPA	<b>2.9</b> (2)	<b>2.0</b> (2)	5.9(3)	3.5(2)	<b>2.0</b> (0.2)	15/15
GP1-CMAES	<b>2.2</b> (3)	<b>1.4</b> (1)	<b>2.3</b> (2)	<b>2.2</b> (2)	74(77)	1/15
GP5-CMAES	<b>3.0</b> (3)	<b>1.8</b> (1)	<b>2.8</b> (7)	3.7(7)	$\infty$ 1260	0/15
IPOPCMAv3p	3.1(4)	<b>1.8</b> (1)	3.3(3)	<b>3.1</b> (3)	<b>2.2</b> (0.6)	15/15
LHD-10xDef	<b>1.6</b> (2)	<b>2.2</b> (4)	5.5(4)	3.6(3)	$\infty$ 250	0/15
LHD-2xDefa	<b>1.7</b> (2)	<b>1.3</b> (1)	3.2(5)	4.9(5)	$\infty$ 250	0/15
RAND-2xDef	<b>2.3</b> (2)	<b>1.8</b> (1)	<b>2.8</b> (4)	9.0(8)	$\infty$ 250	0/15
RF1-CMAES	<b>3.0</b> (3)	<b>2.0</b> (2)	4.5(5)	8.5(4)	$\infty$ 1258	0/15
RF5-CMAES	3.6(4)	<b>2.4</b> (3)	19(54)	154(117)	$\infty$ 1260	0/15
Sifeg	<b>1.2</b> (1)	<b>1.2</b> (0.9)	5.3(0.8)	36(10)	120(143)	12/15
Sif	<b>1.2</b> (2)	<b>1.2</b> (1.0)	8.2(26)	64(388)	458(237)	5/15
Srr	<b>1.2</b> (1)	<b>1.2</b> (1)	6.7(21)	34(112)	101(59)	11/15



Table 56: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f7</b>	<i>1.6e+2:4.2</i>	<i>1.0e+2:6.2</i>	<i>2.5e+1:20</i>	<i>4.0e+0:54</i>	<i>1.0e+0:324</i>	15/15
BSifeg	34(249)	24(2)	55(128)	620(1442)	754(1633)	3/15
BSif	34(2)	24(85)	64(137)	600(462)	1037(1119)	2/15
BSqi	34(1)	24(2)	68(76)	488(365)	726(522)	3/15
BSrr	35(127)	46(168)	96(0.6)	669(912)	1050(649)	2/15
CMA-CSA	<b>2.0</b> (2)	<b>2.8</b> (1)	3.6(3)	3.9(1.0)	<b>1.3</b> (1.0)	15/15
CMA-MSR	3.5(4)	3.7(3)	3.2(3)	4.5(8)	<b>1.1</b> (1.0)	15/15
CMA-TPA	<b>2.5</b> (3)	<b>2.3</b> (2)	<b>2.5</b> (2)	<b>2.7</b> (1)	<b>0.98</b> (0.1)	15/15
GP1-CMAES	<b>1.7</b> (1)	<b>2.0</b> (1)	<b>2.1</b> (1)	4.7(2)	<b>1.4</b> (1.0)	15/15
GP5-CMAES	<b>2.2</b> (2)	<b>2.5</b> (2)	<b>1.9</b> (0.9)	<b>1.2</b> (0.6)*	<b>0.82</b> (0.9)	15/15
IPOPCMAv3p	3.3(2)	3.4(4)	3.3(2)	<b>3.5</b> (0.9)	<b>1.5</b> (0.7)	14/15
LHD-10xDef	<b>1.5</b> (1)	<b>2.2</b> (3)	5.2(2)	4.8(3)	5.5(7)	2/15
LHD-2xDefa	<b>1.4</b> (1)	<b>2.0</b> (3)	<b>1.8</b> (2)	8.0(8)	11(11)	1/15
RAND-2xDef	<b>1.3</b> (1.0)	<b>1.7</b> (2)	<b>2.5</b> (3)	9.3(7)	11(24)	1/15
RF1-CMAES	<b>1.9</b> (2)	<b>2.6</b> (1)	<b>2.7</b> (2)	15(15)	10(9)	5/15
RF5-CMAES	<b>2.5</b> (3)	<b>2.7</b> (2)	5.3(13)	33(23)	17(16)	3/15
Sifeg	<b>1.6</b> (3)	<b>2.0</b> (3)	<b>1.5</b> (2)	396(707)	276(160)	6/15
Sif	<b>1.6</b> (2)	<b>2.0</b> (2)	8.1(26)	296(420)	204(167)	8/15
Srr	<b>1.6</b> (3)	<b>2.1</b> (2)	8.3(27)	317(429)	306(449)	6/15

Table 57: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>1.0e+4</i> :4.6	<i>6.3e+3</i> :6.8	<i>1.0e+3</i> :18	<i>6.3e+1</i> :54	<i>1.6e+0</i> :258	15/15
BSifeg	<b>1.6</b> (0.3)	<b>1.8</b> (1)	<b>1.0</b> (0.1)	13(30)	38(40)	15/15
BSif	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.0</b> (0.2)	34(73)	64(66)	14/15
BSqi	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.0</b> (0.4)	8.2(11)	35(49)	14/15
BSrr	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.0</b> (0.1)	12(12)	37(37)	14/15
CMA-CSA	<b>2.6</b> (1)	<b>2.8</b> (1)	<b>2.8</b> (1)	<b>2.7</b> (1)	<b>4.9</b> (1)	15/15
CMA-MSR	<b>2.2</b> (3)	<b>2.0</b> (4)	<b>2.6</b> (3)	4.2(1)	<b>3.4</b> (2)	15/15
CMA-TPA	3.4(6)	<b>2.6</b> (6)	<b>2.7</b> (2)	4.0(1)	5.8(5)	15/15
GP1-CMAES	<b>2.8</b> (3)	<b>2.2</b> (3)	<b>2.3</b> (1)	<b>2.1</b> (0.9)	7.2(11)	8/15
GP5-CMAES	<b>2.1</b> (1)	<b>1.9</b> (2)	<b>1.9</b> (1)	<b>2.5</b> (2)	70(35)	1/15
IPOPCMAv3p	3.1(3)	<b>2.8</b> (2)	<b>2.1</b> (1.0)	3.8(2)	<b>4.9</b> (4)	11/15
LHD-10xDef	<b>2.7</b> (3)	<b>2.8</b> (2)	5.2(3)	12(8)	$\infty$ 250	0/15
LHD-2xDefa	<b>2.4</b> (1)	<b>2.3</b> (2)	<b>1.5</b> (0.9)	3.6(9)	$\infty$ 250	0/15
RAND-2xDef	3.1(2)	<b>2.3</b> (2)	<b>1.5</b> (0.6)	3.1(2)	$\infty$ 250	0/15
RF1-CMAES	<b>2.6</b> (2)	<b>2.3</b> (2)	3.1(2)	7.8(12)	36(38)	2/15
RF5-CMAES	<b>2.3</b> (2)	<b>2.0</b> (1)	<b>2.8</b> (3)	56(29)	$\infty$ 1252	0/15
Sifeg	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.1</b> (0.1)	<b>2.2</b> (3)	17(22)	15/15
Sif	<b>1.6</b> (2)	<b>1.8</b> (1)	<b>1.1</b> (0.5)	3.4(1)	48(43)	14/15
Srr	<b>1.6</b> (1)	<b>1.8</b> (1)	<b>1.1</b> (0.1)	<b>1.7</b> (1)	21(34)	15/15

Table 58: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>2.5e+1:20</i>	<i>1.6e+1:26</i>	<i>1.0e+1:35</i>	<i>4.0e+0:62</i>	<i>1.6e-2:256</i>	15/15
BSifeg	19(58)	16(75)	14(16)	223(484)	$\infty$ 5e4	0/15
BSif	57(363)	45(279)	36(15)	416(392)	$\infty$ 5e4	0/15
BSqi	15(6)	13(0.9)	11(28)	181(58)	$\infty$ 5e4	0/15
BSrr	17(13)	14(20)	15(14)	248(306)	$\infty$ 4e4	0/15
CMA-CSA	<b>7.5</b> (2)	<b>6.7</b> (2)	<b>5.7</b> (0.6)	<b>6.6</b> (7)	<b>7.1</b> (4)	15/15
CMA-MSR	10(4)	8.5(2)	7.2(1)	7.9(3)	<b>6.9</b> (7)	15/15
CMA-TPA	7.8(3)	<b>6.8</b> (3)	<b>5.4</b> (2)	<b>4.6</b> (2)	<b>5.0</b> (1)	15/15
GP1-CMAES	12(10)	10(15)	8.2(7)	14(24)	$\infty$ 1258	0/15
GP5-CMAES	15(5)	14(12)	13(19)	27(17)	70(55)	1/15
IPOPCMAv3p	10(3)	8.7(3)	7.5(2)	<b>7.2</b> (10)	36(18)	2/15
LHD-10xDef	185(180)	144(128)	$\infty$	$\infty$	$\infty$ 250	0/15
LHD-2xDefa	12(3)	12(7)	25(40)	$\infty$	$\infty$ 250	0/15
RAND-2xDef	11(5)	11(9)	20(3)	60(85)	$\infty$ 250	0/15
RF1-CMAES	38(82)	36(51)	30(15)	48(42)	$\infty$ 1258	0/15
RF5-CMAES	106(204)	126(50)	257(205)	$\infty$	$\infty$ 1252	0/15
Sifeg	<b>7.5</b> (6)	6.9(14)	5.8(4)	102(220)	$\infty$ 5e4	0/15
Sif	36(105)	28(93)	24(4)	221(505)	$\infty$ 5e4	0/15
Srr	<b>6.2</b> (2)	<b>5.3</b> (6)	<b>4.5</b> (7)	95(237)	$\infty$ 4e4	0/15

Table 59: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>2.5e+6</i> :2.9	<i>6.3e+5</i> :7.0	<i>2.5e+5</i> :17	<i>6.3e+3</i> :54	<i>2.5e+1</i> :297	15/15
BSifeg	<b>1.8</b> (2)	<b>2.1</b> (0.9)	12(41)	463(716)	$\infty$ 3e4	0/15
BSif	<b>1.8</b> (2)	<b>2.1</b> (1)	9.2(0.7)	481(550)	$\infty$ 3e4	0/15
BSqi	<b>1.8</b> (2)	<b>2.1</b> (1)	7.1(0.4)	325(448)	$\infty$ 3e4	0/15
BSrr	<b>1.8</b> (1)	<b>2.1</b> (1)	10(0.6)	529(749)	$\infty$ 2e4	0/15
CMA-CSA	<b>2.5</b> (2)	<b>1.8</b> (1)	<b>1.5</b> (0.8)	4.0(1)	<b>2.7</b> (0.6)	15/15
CMA-MSR	<b>2.3</b> (1)	<b>2.0</b> (3)	<b>1.6</b> (1)	4.0(3)	<b>2.9</b> (0.8)	15/15
CMA-TPA	<b>1.9</b> (3)	<b>2.3</b> (2)	<b>1.4</b> (2)	<b>3.3</b> (2)	<b>2.3</b> (1)	15/15
GP1-CMAES	<b>1.2</b> (2)	<b>0.94</b> (1.0)	<b>0.85</b> (0.6)	<b>2.9</b> (2)	<b>2.0</b> (0.4)	15/15
GP5-CMAES	<b>2.4</b> (3)	<b>1.6</b> (1)	<b>1.0</b> (1)	<b>1.6</b> (0.6)	<b>0.95</b> (0.2)	15/15
IPOPCMAv3p	<b>1.8</b> (1)	<b>2.2</b> (2)	<b>1.6</b> (2)	4.7(2)	4.4(5)	11/15
LHD-10xDef	<b>1.5</b> (2)	<b>1.7</b> (0.9)	<b>1.4</b> (2)	12(9)	$\infty$ 250	0/15
LHD-2xDefa	<b>1.9</b> (2)	<b>1.4</b> (1)	<b>1.6</b> (1)	12(13)	$\infty$ 250	0/15
RAND-2xDef	<b>2.3</b> (2)	<b>2.1</b> (2)	<b>1.5</b> (0.9)	3.5(1)	$\infty$ 250	0/15
RF1-CMAES	3.2(4)	<b>2.3</b> (2)	<b>1.6</b> (0.8)	10(18)	63(90)	1/15
RF5-CMAES	<b>2.7</b> (2)	<b>1.7</b> (2)	4.5(0.4)	43(28)	$\infty$ 1260	0/15
Sifeg	<b>1.8</b> (2)	<b>1.9</b> (1)	<b>1.5</b> (1)	76(134)	$\infty$ 1e4	0/15
Sif	<b>1.8</b> (2)	<b>1.9</b> (2)	<b>1.4</b> (1)	97(142)	$\infty$ 1e4	0/15
Srr	<b>1.8</b> (2)	<b>1.9</b> (1)	<b>1.4</b> (1)	93(70)	$\infty$ 1e4	0/15

Table 60: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>1.0e+6</i> :3.0	<i>6.3e+4</i> :6.2	<i>6.3e+2</i> :16	<i>6.3e+1</i> :74	<i>6.3e-1</i> :298	15/15
BSifeg	<b>2.4</b> (3)	<b>2.2</b> (1)	<b>1.5</b> (0.5)	116(123)	$\infty$ <i>3e4</i>	0/15
BSif	<b>2.4</b> (1)	<b>2.2</b> (1)	<b>1.5</b> (0.5)	93(86)	$\infty$ <i>3e4</i>	0/15
BSqi	<b>2.4</b> (2)	<b>2.2</b> (1)	<b>1.5</b> (0.6)	64(103)	$\infty$ <i>4e4</i>	0/15
BSrr	<b>2.4</b> (1)	<b>2.2</b> (1)	<b>1.5</b> (0.6)	85(79)	$\infty$ <i>3e4</i>	0/15
CMA-CSA	<b>1.5</b> (1)	<b>2.0</b> (2)	3.8(2)	6.0(4)	<b>3.0</b> (0.5)	15/15
CMA-MSR	3.2(4)	3.1(2)	6.6(2)	7.3(3)	3.5(0.5)	15/15
CMA-TPA	<b>2.8</b> (7)	3.6(0.8)	4.4(2)	5.7(4)	<b>3.2</b> (0.4)	15/15
GP1-CMAES	<b>1.4</b> (0.9)	<b>2.4</b> (3)	4.5(3)	<b>2.3</b> (2)	5.1(4)	11/15
GP5-CMAES	<b>1.5</b> (1)	<b>2.5</b> (2)	<b>2.9</b> (2)	<b>1.9</b> (1)	<b>2.3</b> (5)	14/15
IPOPCMAv3p	<b>2.5</b> (4)	<b>2.9</b> (2)	5.1(3)	5.3(6)	$\infty$ <i>1258</i>	0/15
LHD-10xDef	<b>1.7</b> (2)	3.1(3)	6.1(6)	5.2(9)	$\infty$ <i>250</i>	0/15
LHD-2xDefa	<b>1.5</b> (1)	<b>3.0</b> (2)	4.1(3)	<b>3.5</b> (4)	$\infty$ <i>250</i>	0/15
RAND-2xDef	<b>1.6</b> (0.6)	3.6(3)	5.8(4)	8.7(7)	$\infty$ <i>250</i>	0/15
RF1-CMAES	<b>2.2</b> (1)	<b>2.6</b> (2)	3.9(2)	5.1(12)	$\infty$ <i>1258</i>	0/15
RF5-CMAES	<b>2.2</b> (3)	<b>2.3</b> (3)	<b>3.0</b> (2)	11(11)	$\infty$ <i>1260</i>	0/15
Sifeg	<b>2.4</b> (2)	<b>2.3</b> (2)	<b>1.8</b> (0.7)	11(10)	$\infty$ <i>2e4</i>	0/15
Sif	<b>2.4</b> (2)	<b>2.3</b> (2)	<b>1.8</b> (0.5)	24(30)	$\infty$ <i>2e4</i>	0/15
Srr	<b>2.4</b> (2)	<b>2.3</b> (1)	<b>1.7</b> (0.8)	23(0.2)	$\infty$ <i>2e4</i>	0/15

Table 61: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>4.0e+7</i> :3.6	<i>1.6e+7</i> :7.6	<i>4.0e+6</i> :19	<i>1.6e+4</i> :52	<i>1.0e+0</i> :268	15/15
BSifeg	<b>1.3</b> (1)	<b>2.0</b> (1)	<b>1.2</b> (1)	8.1(5)	144(213)	6/15
BSif	<b>1.3</b> (1)	<b>2.1</b> (1)	<b>1.4</b> (0.2)	11(9)	157(334)	6/15
BSqi	<b>1.3</b> (2)	<b>2.0</b> (0.8)	<b>1.1</b> (0.4)	6.7(15)	42(34)	12/15
BSrr	<b>1.3</b> (2)	<b>2.0</b> (1)	<b>1.2</b> (0.9)	14(8)	51(63)	10/15
CMA-CSA	3.5(3)	<b>2.9</b> (3)	<b>2.4</b> (2)	4.7(1)	7.1(3)	15/15
CMA-MSR	<b>2.1</b> (6)	3.1(4)	<b>2.9</b> (2)	5.7(1)	<b>5.4</b> (6)	15/15
CMA-TPA	<b>2.8</b> (2)	3.3(2)	4.0(4)	4.6(1)	<b>6.1</b> (1)	15/15
GP1-CMAES	<b>2.0</b> (2)	<b>2.5</b> (2)	<b>1.9</b> (0.6)	<b>3.7</b> (2)	<b>6.2</b> (6)	8/15
GP5-CMAES	3.1(2)	<b>2.9</b> (2)	<b>3.0</b> (2)	21(17)	8.5(15)	6/15
IPOPCMAv3p	<b>1.9</b> (3)	<b>2.9</b> (2)	3.0(3)	4.6(1.0)	10(12)	6/15
LHD-10xDef	<b>1.1</b> (1)	<b>2.8</b> (3)	4.5(2)	8.2(4)	$\infty$ 250	0/15
LHD-2xDefa	<b>1.5</b> (1)	<b>1.9</b> (1)	<b>1.4</b> (0.9)	<b>3.0</b> (1)	$\infty$ 250	0/15
RAND-2xDef	<b>1.4</b> (3)	<b>2.0</b> (2)	<b>1.5</b> (0.4)	<b>2.9</b> (0.8)	$\infty$ 250	0/15
RF1-CMAES	<b>2.1</b> (1)	3.2(3)	3.2(1)	5.1(4)	22(12)	3/15
RF5-CMAES	<b>1.9</b> (2)	<b>1.7</b> (2)	5.6(2)	117(171)	$\infty$ 1260	0/15
Sifeg	<b>1.3</b> (1)	8.2(48)	5.1(0.4)	10(17)	50(69)	5/15
Sif	<b>1.3</b> (0.9)	4.4(1)	<b>2.0</b> (0.4)	7.5(8)	56(58)	5/15
Srr	<b>1.3</b> (1)	6.9(20)	4.6(13)	11(22)	21(17)	9/15

Table 62: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>1.0e+3:2.8</i>	<i>6.3e+2:8.4</i>	<i>4.0e+2:17</i>	<i>6.3e+1:52</i>	<i>6.3e-2:264</i>	15/15
BSifeg	<b>1.5</b> (2)	<b>1.5</b> (0.9)	<b>1.1</b> (0.6)	223(318)	2385(2219)	1/15
BSif	<b>1.5</b> (3)	<b>1.5</b> (0.9)	<b>1.1</b> (0.7)	227(323)	$\infty$ <i>4e4</i>	0/15
BSqi	<b>1.5</b> (0.7)	<b>1.5</b> (0.9)	<b>1.1</b> (0.7)	208(285)	$\infty$ <i>4e4</i>	0/15
BSrr	<b>1.5</b> (3)	<b>1.5</b> (0.5)	<b>1.1</b> (1.0)	221(422)	1122(1443)	2/15
CMA-CSA	3.2(4)	3.1(3)	<b>3.0</b> (2)	3.9(3)	<b>4.0</b> (1)	15/15
CMA-MSR	3.8(3)	<b>2.5</b> (2)	3.5(1)	4.5(2)	<b>3.8</b> (0.5)	15/15
CMA-TPA	4.6(3)	<b>2.9</b> (3)	3.5(2)	3.8(2)	<b>4.3</b> (2)	15/15
GP1-CMAES	<b>2.3</b> (2)	<b>1.6</b> (1)	<b>2.0</b> (1)	<b>2.3</b> (0.7)	70(92)	1/15
GP5-CMAES	3.2(3)	<b>2.1</b> (2)	<b>1.6</b> (0.5)	<b>1.4</b> (0.3)	11(14)	5/15
IPOPCMAv3p	3.0(4)	<b>2.2</b> (3)	3.0(2)	3.9(0.6)	10(15)	7/15
LHD-10xDef	<b>2.6</b> (1)	<b>3.0</b> (3)	4.8(3)	<b>2.9</b> (0.5)	$\infty$ <i>250</i>	0/15
LHD-2xDefa	<b>2.1</b> (1)	<b>2.0</b> (1)	<b>1.9</b> (0.3)	<b>1.8</b> (0.4)	$\infty$ <i>250</i>	0/15
RAND-2xDef	<b>2.0</b> (1)	<b>1.8</b> (1)	<b>1.8</b> (0.9)	<b>1.7</b> (0.5)	$\infty$ <i>250</i>	0/15
RF1-CMAES	3.2(2)	<b>2.0</b> (1)	<b>2.4</b> (1)	8.1(19)	69(82)	1/15
RF5-CMAES	3.5(2)	<b>2.2</b> (2)	<b>2.1</b> (1)	35(21)	$\infty$ <i>1252</i>	0/15
Sifeg	<b>1.5</b> (3)	<b>1.5</b> (0.8)	<b>1.1</b> (0.8)	83(183)	2257(3322)	1/15
Sif	<b>1.5</b> (3)	<b>1.5</b> (0.9)	<b>1.1</b> (0.8)	118(282)	$\infty$ <i>4e4</i>	0/15
Srr						

Table 63: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>1.6e+1:3.0</i>	<i>1.0e+1:10</i>	<i>6.3e+0:15</i>	<i>2.5e-1:53</i>	<i>1.0e-5:251</i>	15/15
BSifeg	<b>3.0</b> (2)	<b>1.5</b> (0.7)	<b>1.4</b> (0.6)	8.7(7)	$\infty$ 5e4	0/15
BSif	<b>3.0</b> (3)	<b>1.5</b> (1.0)	<b>1.4</b> (1)	10(11)	$\infty$ 5e4	0/15
BSqi	<b>3.0</b> (3)	<b>1.5</b> (0.9)	<b>1.4</b> (0.8)	5.6(4)	$\infty$ 5e4	0/15
BSrr	<b>3.0</b> (3)	<b>1.5</b> (0.8)	<b>1.4</b> (1)	7.7(9)	$\infty$ 5e4	0/15
CMA-CSA	4.1(4)	<b>1.7</b> (3)	<b>2.6</b> (2)	3.2(1)	<b>3.9</b> (0.6)	15/15
CMA-MSR	4.3(4)	<b>2.5</b> (1)	<b>2.5</b> (1)	4.2(0.9)	<b>4.1</b> (0.6)	15/15
CMA-TPA	3.5(10)	<b>2.1</b> (1)	<b>2.7</b> (4)	3.6(1)	<b>4.0</b> (0.7)	15/15
GP1-CMAES	3.2(2)	<b>1.6</b> (1.0)	<b>1.9</b> (2)	<b>2.2</b> (0.9)	$\infty$ 1258	0/15
GP5-CMAES	4.0(4)	<b>1.8</b> (1)	<b>1.5</b> (2)	<b>1.6</b> (0.6)	$\infty$ 1260	0/15
IPOPCMAv3p	4.8(3)	<b>2.4</b> (3)	<b>2.4</b> (2)	3.8(0.5)	24(23)	3/15
LHD-10xDef	<b>2.0</b> (1)	<b>1.2</b> (1)	<b>2.2</b> (2)	3.2(0.4)	$\infty$ 250	0/15
LHD-2xDefa	<b>2.2</b> (3)	<b>1.5</b> (1)	<b>1.4</b> (0.6)	<b>2.0</b> (0.9)	$\infty$ 250	0/15
RAND-2xDef	3.0(2)	<b>1.4</b> (2)	<b>1.7</b> (0.9)	4.8(10)	$\infty$ 250	0/15
RF1-CMAES	3.2(5)	<b>2.1</b> (2)	<b>2.8</b> (4)	4.2(1)	$\infty$ 1258	0/15
RF5-CMAES	<b>2.8</b> (2)	<b>1.2</b> (1)	<b>2.0</b> (3)	81(163)	$\infty$ 1260	0/15
Sifeg	<b>3.0</b> (3)	<b>1.5</b> (1)	<b>1.4</b> (0.7)	<b>2.7</b> (3)	$\infty$ 5e4	0/15
Sif	<b>3.0</b> (3)	<b>1.5</b> (1)	<b>1.4</b> (0.7)	<b>2.8</b> (1)	$\infty$ 5e4	0/15
Srr	<b>3.0</b> (3)	<b>1.5</b> (1)	<b>1.4</b> (0.9)	<b>1.9</b> (1)	$\infty$ 5e4	0/15



Table 64: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>1.6e+2</i> :3.0	<i>1.0e+2</i> :13	<i>6.3e+1</i> :24	<i>4.0e+1</i> :55	<i>1.6e+1</i> :289	5/5
BSifeg	<b>2.9</b> (2)	3.1(8)	10(34)	70(255)	160(181)	9/15
BSif	<b>2.9</b> (3)	<b>1.8</b> (1)	27(7)	50(220)	228(268)	7/15
BSqi	<b>2.9</b> (2)	<b>2.7</b> (12)	26(80)	52(43)	184(139)	8/15
BSrr	<b>2.9</b> (3)	<b>2.6</b> (6)	10(14)	104(142)	237(276)	7/15
CMA-CSA	4.5(5)	<b>2.3</b> (1.0)	<b>2.6</b> (1.0)	<b>2.0</b> (1.0)	<b>1.4</b> (0.9)	15/15
CMA-MSR	5.1(6)	<b>2.3</b> (3)	<b>2.4</b> (2)	<b>2.0</b> (1)	<b>1.0</b> (0.5)	15/15
CMA-TPA	7.8(14)	<b>2.8</b> (3)	<b>2.5</b> (1)	<b>2.2</b> (0.8)	<b>1.2</b> (0.7)	15/15
GP1-CMAES	4.6(3)	<b>1.9</b> (1)	<b>1.9</b> (1)	<b>1.4</b> (0.5)	<b>1.2</b> (1)	15/15
GP5-CMAES	3.5(3)	<b>1.6</b> (1)	<b>1.6</b> (1)	<b>1.1</b> (0.4)	3.0(4)	11/15
IPOPCMAv3p	<b>2.3</b> (2)	<b>1.5</b> (0.6)	<b>1.6</b> (1.0)	<b>1.8</b> (1)	<b>1.3</b> (0.8)	15/15
LHD-10xDef	4.4(5)	<b>2.9</b> (3)	3.8(2)	<b>2.7</b> (0.5)	<b>1.3</b> (2)	9/15
LHD-2xDefa	<b>2.1</b> (1)	<b>1.5</b> (0.8)	<b>1.5</b> (0.5)	<b>1.5</b> (0.4)	<b>1.0</b> (1)	9/15
RAND-2xDef	3.7(3)	<b>1.6</b> (1)	<b>1.3</b> (0.6)	<b>1.4</b> (1.0)	<b>1.2</b> (2)	8/15
RF1-CMAES	5.4(4)	<b>2.2</b> (1)	<b>2.4</b> (1)	<b>1.7</b> (1)	<b>1.3</b> (2)	14/15
RF5-CMAES	3.5(5)	<b>1.6</b> (0.8)	<b>2.4</b> (3)	7.0(9)	5.7(8)	8/15
Sifeg	<b>2.9</b> (3)	<b>1.2</b> (1.0)	<b>1.0</b> (0.4)	<b>0.90</b> (0.4)	52(63)	14/15
Sif	<b>2.9</b> (3)	<b>1.2</b> (0.7)	<b>1.0</b> (0.3)	<b>0.87</b> (0.7)	51(78)	13/15
Srr	<b>2.9</b> (2)	<b>1.2</b> (0.9)	<b>1.0</b> (0.2)	<b>0.85</b> (0.6)	39(56)	14/15

Table 65: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>4.0e+1:4.8</i>	<i>2.5e+1:16</i>	<i>1.6e+1:46</i>	<i>1.0e+1:120</i>	<i>4.0e+0:334</i>	15/15
BSifeg	<b>1.7</b> (2)	<b>1.4</b> (0.9)	<b>0.85</b> (0.8)	<b>1.3</b> (2)	40(46)	15/15
BSif	<b>1.7</b> (1)	<b>1.4</b> (1.0)	<b>1.0</b> (1)	10(35)	32(25)	15/15
BSqi	<b>1.7</b> (2)	<b>1.4</b> (0.7)	<b>1.1</b> (0.4)	<b>2.5</b> (6)	22(37)	15/15
BSrr	<b>1.7</b> (2)	<b>1.4</b> (0.7)	<b>1.1</b> (1)	<b>1.4</b> (0.8)	30(21)	15/15
CMA-CSA	3.7(4)	<b>2.9</b> (5)	3.1(3)	<b>2.2</b> (1)	<b>1.5</b> (0.7)	15/15
CMA-MSR	<b>2.0</b> (1)	<b>2.2</b> (2)	<b>1.9</b> (2)	5.9(11)	4.6(9)	15/15
CMA-TPA	<b>2.3</b> (1)	<b>2.9</b> (3)	<b>3.0</b> (2)	<b>1.7</b> (2)	<b>1.8</b> (0.6)	15/15
GP1-CMAES	<b>1.6</b> (1)	<b>1.3</b> (1)	<b>0.90</b> (0.8)	<b>1.2</b> (0.9)	<b>1.4</b> (2)	13/15
GP5-CMAES	<b>2.0</b> (2)	<b>1.5</b> (0.4)	<b>2.7</b> (4)	<b>1.3</b> (2)	<b>1.9</b> (2)	13/15
IPOPCMAv3p	<b>1.4</b> (0.6)	<b>1.2</b> (0.9)	<b>1.5</b> (1)	<b>2.4</b> (2)	<b>2.9</b> (3)	11/15
LHD-10xDef	<b>1.4</b> (0.7)	<b>1.6</b> (1)	<b>1.9</b> (2)	<b>1.5</b> (0.5)	<b>1.4</b> (0.8)	7/15
LHD-2xDefa	<b>2.5</b> (2)	<b>1.4</b> (0.6)	<b>1.6</b> (1)	<b>2.2</b> (2)	11(19)	1/15
RAND-2xDef	<b>1.3</b> (0.6)	<b>1.2</b> (1)	<b>1.8</b> (2)	<b>1.7</b> (3)	<b>1.3</b> (1)	7/15
RF1-CMAES	<b>1.3</b> (1)	<b>0.90</b> (1)	<b>1.3</b> (2)	<b>1.8</b> (2)	<b>2.1</b> (2)	11/15
RF5-CMAES	<b>2.5</b> (3)	<b>1.3</b> (1)	<b>1.1</b> (1)	<b>1.7</b> (5)	3.2(5)	9/15
Sifeg	<b>1.7</b> (1)	<b>1.6</b> (2)	<b>0.89</b> (0.7)	<b>0.62</b> (0.4)	7.2(6)	15/15
Sif	<b>1.7</b> (1)	<b>1.6</b> (1)	<b>0.89</b> (0.4)	<b>0.69</b> (0.5)	7.7(6)	15/15
Srr	<b>1.7</b> (1)	<b>1.6</b> (1)	<b>0.88</b> (0.5)	<b>0.68</b> (0.6)	3.4(10)	15/15

Table 66: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.0e+1:5.2</i>	<i>6.3e+0:26</i>	<i>4.0e+0:57</i>	<i>2.5e+0:110</i>	<i>6.3e-1:412</i>	15/15
BSifeg	6.3(21)	5.5(14)	174(222)	189(123)	268(547)	5/15
BSif	7.0(3)	298(478)	322(447)	188(116)	157(92)	7/15
BSqi	4.1(4)	139(944)	141(444)	160(229)	150(162)	7/15
BSrr	4.3(3)	6.4(7)	182(447)	137(183)	229(260)	6/15
CMA-CSA	4.2(5)	<b>1.8</b> (1)	<b>1.5</b> (1.0)	<b>1.0</b> (0.4)	<b>0.61</b> (0.3)	15/15
CMA-MSR	4.2(2)	<b>2.0</b> (2)	<b>1.5</b> (0.6)	<b>1.1</b> (0.5)	<b>0.60</b> (0.1)	15/15
CMA-TPA	24(72)	6.0(3)	3.5(1)	<b>2.1</b> (0.7)	<b>1.5</b> (3)	15/15
GP1-CMAES	4.5(4)	<b>1.6</b> (1)	<b>1.1</b> (0.6)	<b>0.78</b> (0.1)	<b>0.45</b> (0.3)	15/15
GP5-CMAES	3.6(6)	<b>1.6</b> (2)	<b>1.6</b> (4)	<b>1.8</b> (0.1)	<b>2.5</b> (3)	10/15
IPOPCMAv3p	4.1(4)	<b>1.8</b> (0.9)	<b>1.3</b> (0.9)	<b>1.2</b> (0.5)	<b>0.81</b> (0.9)	14/15
LHD-10xDefa	<b>2.1</b> (1)	<b>2.4</b> (2)	<b>1.8</b> (1)	<b>1.4</b> (0.4)	4.4(5)	2/15
LHD-2xDefa	<b>2.4</b> (2)	<b>1.4</b> (0.6)	<b>1.0</b> (0.7)	<b>1.1</b> (2)	8.9(13)	1/15
RAND-2xDef	<b>2.3</b> (3)	<b>1.2</b> (1)	<b>1.4</b> (0.8)	<b>1.8</b> (2)	4.3(4)	2/15
RF1-CMAES	3.0(3)	<b>2.2</b> (2)	3.3(7)	3.9(11)	4.1(5)	7/15
RF5-CMAES	4.8(7)	8.6(2)	9.0(11)	10(8)	22(8)	2/15
Sifeg	3.9(2)	10(68)	76(84)	61(206)	109(171)	9/15
Sif	3.9(3)	<b>1.4</b> (1)	132(428)	112(142)	112(80)	9/15
Srr	3.9(3)	<b>1.5</b> (1)	99(343)	121(360)	191(303)	6/15

Table 67: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>6.3e+1</i> :3.4	<i>4.0e+1</i> :7.2	<i>2.5e+1</i> :20	<i>1.6e+1</i> :58	<i>1.6e+0</i> :318	15/15
BSifeg	<b>1.5</b> (3)	<b>2.2</b> (2)	75(529)	114(282)	184(219)	8/15
BSif	<b>1.5</b> (0.9)	<b>2.2</b> (3)	115(414)	120(119)	228(210)	7/15
BSqi	<b>1.5</b> (2)	<b>2.3</b> (3)	91(3)	90(299)	302(205)	6/15
BSrr	<b>1.5</b> (3)	<b>2.3</b> (2)	8.4(26)	106(168)	204(290)	7/15
CMA-CSA	4.4(6)	3.9(1)	<b>2.1</b> (1)	<b>1.4</b> (0.7)	<b>2.1</b> (2)	15/15
CMA-MSR	<b>1.6</b> (1.0)	<b>2.0</b> (2)	<b>2.0</b> (1)	<b>1.3</b> (0.7)	4.1(12)	15/15
CMA-TPA	<b>2.5</b> (1)	<b>2.7</b> (3)	<b>1.8</b> (2)	<b>1.1</b> (0.8)	<b>1.4</b> (2)	15/15
GP1-CMAES	<b>2.4</b> (4)	3.6(2)	<b>2.1</b> (2)	<b>1.2</b> (0.5)	<b>1.2</b> (1)	14/15
GP5-CMAES	<b>1.7</b> (0.9)	<b>3.0</b> (3)	5.2(11)	<b>2.1</b> (3)	5.8(6)	7/15
IPOPCMAv3p	<b>1.2</b> (0.7)	<b>1.2</b> (2)	<b>1.8</b> (2)	<b>1.3</b> (1)	<b>1.4</b> (0.3)	14/15
LHD-10xDef	<b>2.6</b> (5)	3.4(4)	3.3(3)	<b>2.0</b> (0.8)	12(12)	1/15
LHD-2xDefa	<b>1.3</b> (2)	<b>1.6</b> (2)	<b>2.2</b> (2)	<b>1.3</b> (0.6)	5.5(7)	2/15
RAND-2xDef	<b>1.4</b> (1)	<b>2.2</b> (2)	<b>1.7</b> (0.9)	<b>1.5</b> (1)	12(14)	1/15
RF1-CMAES	<b>1.5</b> (3)	<b>1.7</b> (2)	<b>1.3</b> (1)	<b>0.89</b> (0.9)	<b>2.2</b> (3)	11/15
RF5-CMAES	<b>2.2</b> (2)	<b>3.0</b> (4)	9.5(22)	7.6(8)	29(28)	2/15
Sifeg	<b>1.5</b> (3)	<b>2.1</b> (1)	6.1(0.4)	29(19)	145(192)	9/15
Sif	<b>1.5</b> (2)	<b>2.1</b> (2)	63(232)	40(145)	118(135)	10/15
Srr	<b>1.5</b> (3)	<b>2.2</b> (1)	3.6(10)	38(50)	67(191)	11/15

Table 68: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:172</i>	<i>1.0e-1:242</i>	<i>6.3e-2:675</i>	<i>4.0e-2:3078</i>	<i>2.5e-2:4946</i>	15/15
BSifeg	917(1787)	909(830)	1077(864)	$\infty$	$\infty$ <i>5e4</i>	0/15
BSif	732(937)	694(668)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
BSqi	969(780)	1440(975)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
BSrr	737(913)	925(869)	$\infty$	$\infty$	$\infty$ <i>5e4</i>	0/15
CMA-CSA	<b>154</b> (83)	<b>153</b> (146)	<b>70</b> (55)	<b>19</b> (26)	<b>15</b> (16)	15/15
CMA-MSR	<b>222</b> (95)	<b>306</b> (76)	<b>229</b> (559)	<b>139</b> (167)	<b>137</b> (100)	7/15
CMA-TPA	<b>91</b> (67)	<b>84</b> (68)	<b>39</b> (44)	<b>18</b> (18)	<b>14</b> (13)	15/15
GP1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1260</i>	0/15
GP5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1262</i>	0/15
IPOPCMAv3p	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1258</i>	0/15
LHD-10xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>250</i>	0/15
LHD-2xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>250</i>	0/15
RAND-2xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>250</i>	0/15
RF1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1258</i>	0/15
RF5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1262</i>	0/15
Sifeg	437(515)	477(723)	1039(1787)	$\infty$	$\infty$ <i>5e4</i>	0/15
Sif	521(333)	1385(2297)	1021(1558)	$\infty$	$\infty$ <i>5e4</i>	0/15
Srr	670(770)	671(1338)	1042(946)	$\infty$	$\infty$ <i>5e4</i>	0/15

Table 69: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f20</b>	<i>6.3e+3</i> :5.1	<i>4.0e+3</i> :8.4	<i>4.0e+1</i> :15	<i>2.5e+0</i> :69	<i>1.0e+0</i> :851	15/15
BSifeg	3.0(2)	<b>2.0</b> (1)	<b>1.9</b> (1)	<b>2.2</b> (3)	9.3(20)	14/15
BSif	3.0(2)	<b>2.0</b> (1)	<b>2.0</b> (0.5)	<b>2.1</b> (2)	23(35)	12/15
BSqi	3.0(1)	<b>2.0</b> (0.7)	<b>1.8</b> (1)	<b>2.3</b> (1)	8.7(27)	15/15
BSrr	3.0(2)	<b>2.0</b> (0.9)	<b>1.8</b> (2)	<b>1.5</b> (2)	11(30)	14/15
CMA-CSA	<b>2.3</b> (3)	<b>2.0</b> (1)	3.7(0.9)	<b>2.5</b> (0.9)	9.2(5)	15/15
CMA-MSR	3.3(5)	<b>2.4</b> (3)	4.9(2)	<b>2.8</b> (0.8)	1666(1444)	4/15
CMA-TPA	<b>2.8</b> (3)	<b>2.3</b> (2)	3.8(1)	3.1(2)	17(19)	15/15
GP1-CMAES	<b>1.9</b> (2)	<b>1.8</b> (1)	<b>3.0</b> (2)	4.2(2)	11(4)	2/15
GP5-CMAES	<b>2.5</b> (2)	<b>1.8</b> (2)	<b>2.1</b> (0.9)	<b>2.1</b> (1.0)	$\infty$ 1260	0/15
IPOPCMAv3p	<b>2.1</b> (3)	<b>1.8</b> (1)	4.1(2)	3.3(2)	21(21)	1/15
LHD-10xDef	<b>1.8</b> (2)	1.4(0.8)	6.3(4)	11(8)	$\infty$ 250	0/15
LHD-2xDefa	<b>2.8</b> (2)	<b>2.2</b> (1)	<b>2.2</b> (0.8)	7.6(8)	$\infty$ 250	0/15
RAND-2xDef	<b>2.0</b> (2)	<b>2.1</b> (2)	<b>2.6</b> (1.0)	3.3(2)	$\infty$ 250	0/15
RF1-CMAES	<b>2.9</b> (5)	<b>2.4</b> (3)	3.9(2)	5.6(9)	$\infty$ 1258	0/15
RF5-CMAES	<b>2.5</b> (2)	<b>1.8</b> (1)	25(26)	20(24)	$\infty$ 1260	0/15
Sifeg	3.0(2)	<b>2.1</b> (0.3)	<b>1.8</b> (0.6)	<b>1.1</b> (0.4)	<b>3.1</b> (0.6)	15/15
Sif	3.0(2)	<b>2.1</b> (1)	<b>1.8</b> (0.4)	<b>1.2</b> (0.3)	<b>6.6</b> (21)	14/15
Srr	3.0(2)	<b>2.1</b> (0.9)	<b>1.8</b> (1)	<b>0.83</b> (0.5)	<b>2.8</b> (6)	15/15

Table 70: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f21</i></b>	<i>4.0e+1</i> :3.9	<i>2.5e+1</i> :11	<i>1.6e+1</i> :31	<i>6.3e+0</i> :73	<i>1.6e+0</i> :347	5/5
BSifeg	<b>2.9</b> (3)	<b>1.6</b> (2)	11(0.4)	90(245)	141(232)	8/15
BSif	<b>2.9</b> (2)	<b>1.7</b> (1)	101(4)	183(253)	290(217)	5/15
BSqi	<b>2.9</b> (2)	<b>2.4</b> (0.9)	16(58)	85(226)	221(325)	6/15
BSrr	<b>2.9</b> (3)	<b>1.6</b> (2)	14(50)	73(23)	137(142)	9/15
CMA-CSA	<b>2.5</b> (2)	<b>1.9</b> (1)	<b>1.7</b> (2)	<b>1.8</b> (1)	92(2)	14/15
CMA-MSR	3.2(6)	<b>2.0</b> (0.8)	<b>1.7</b> (1)	3.8(2)	249(589)	13/15
CMA-TPA	<b>2.4</b> (2)	<b>2.1</b> (2)	<b>2.0</b> (0.9)	<b>2.0</b> (1.0)	45(148)	15/15
GP1-CMAES	<b>1.1</b> (1)	<b>1.4</b> (2)	<b>0.99</b> (0.5)	4.7(22)	4.9(6)	7/15
GP5-CMAES	<b>2.5</b> (2)	<b>1.7</b> (1)	<b>0.89</b> (0.4)	<b>1.4</b> (3)	4.7(10)	8/15
IPOPCMAv3p	<b>1.8</b> (2)	<b>1.6</b> (1)	<b>1.7</b> (2)	10(18)	15(20)	3/15
LHD-10xDef	<b>1.5</b> (1)	<b>1.7</b> (2)	<b>1.5</b> (2)	<b>2.2</b> (0.6)	<b>2.0</b> (3)	5/15
LHD-2xDefa	<b>1.7</b> (2)	<b>2.1</b> (2)	<b>1.3</b> (0.7)	<b>1.5</b> (0.9)	<b>1.7</b> (1)	5/15
RAND-2xDef	<b>1.4</b> (2)	<b>1.1</b> (1)	<b>1.3</b> (1.0)	<b>1.4</b> (0.9)	<b>3.3</b> (3)	3/15
RF1-CMAES	<b>2.0</b> (2)	<b>1.8</b> (0.9)	<b>1.4</b> (2)	4.1(5)	4.8(3)	7/15
RF5-CMAES	<b>1.8</b> (2)	<b>2.6</b> (2)	<b>2.9</b> (7)	7.5(8)	10(5)	5/15
Sifeg	<b>2.9</b> (2)	<b>1.4</b> (1)	<b>0.82</b> (0.6)	110(0.4)	195(505)	7/15
Sif	<b>2.9</b> (2)	<b>1.6</b> (1)	<b>0.93</b> (0.5)	158(341)	150(91)	8/15
Srr	<b>2.9</b> (2)	<b>1.4</b> (1)	<b>0.84</b> (0.5)	73(195)	179(411)	7/15

Table 71: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f22</b>	<i>6.3e+1</i> :3.6	<i>4.0e+1</i> :15	<i>2.5e+1</i> :32	<i>1.0e+1</i> :71	<i>1.6e+0</i> :341	5/5
BSifeg	3.5(2)	7.4(46)	15(80)	34(14)	88(126)	10/15
BSif	3.5(4)	5.0(0.6)	114(1)	102(180)	217(183)	7/15
BSqi	3.5(4)	3.8(10)	12(9)	31(43)	59(178)	13/15
BSrr	3.5(2)	5.5(16)	13(0.4)	37(178)	100(155)	10/15
CMA-CSA	<b>2.7</b> (2)	<b>1.6</b> (1)	<b>1.4</b> (0.9)	4.1(6)	151(274)	14/15
CMA-MSR	4.3(6)	<b>1.8</b> (2)	5.2(15)	14(16)	113(136)	15/15
CMA-TPA	3.7(3)	<b>1.9</b> (1)	<b>1.2</b> (0.6)	<b>2.5</b> (0.7)	253(236)	12/15
GP1-CMAES	<b>2.6</b> (3)	<b>1.4</b> (1)	<b>1.2</b> (0.9)	3.6(0.1)	10(10)	4/15
GP5-CMAES	<b>2.9</b> (2)	7.5(7)	4.6(3)	4.3(6)	11(17)	4/15
IPOPCMAv3p	<b>2.8</b> (1)	<b>2.2</b> (3)	<b>1.7</b> (1)	5.8(9)	6.3(9)	6/15
LHD-10xDefa	<b>2.2</b> (2)	<b>2.0</b> (0.8)	<b>2.3</b> (2)	<b>1.9</b> (0.5)	<b>2.5</b> (2)	4/15
LHD-2xDefa	3.3(3)	<b>1.8</b> (2)	<b>1.3</b> (0.8)	<b>1.4</b> (2)	<b>1.8</b> (3)	5/15
RAND-2xDef	<b>1.8</b> (2)	<b>1.5</b> (0.9)	<b>0.98</b> (0.6)	<b>0.79</b> (0.6)	<b>2.4</b> (6)	4/15
RF1-CMAES	3.1(5)	<b>2.0</b> (2)	<b>1.3</b> (1)	5.5(13)	3.2(5)	9/15
RF5-CMAES	<b>2.1</b> (4)	4.7(27)	<b>2.9</b> (2)	7.3(3)	24(16)	2/15
Sifeg	3.4(3)	<b>1.8</b> (2)	115(0.7)	123(212)	116(262)	9/15
Sif	3.4(3)	<b>1.7</b> (1)	5.8(18)	117(379)	125(83)	9/15
Srr	3.4(2)	<b>1.6</b> (1)	<b>2.5</b> (0.8)	62(177)	75(98)	11/15



Table 72: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>1.0e+1:3.0</i>	<i>6.3e+0:9.0</i>	<i>4.0e+0:33</i>	<i>2.5e+0:84</i>	<i>1.0e+0:518</i>	15/15
BSifeg	<b>2.6</b> (2)	<b>2.5</b> (2)	<b>1.5</b> (0.8)	<b>1.7</b> (1.0)	4.3(5)	15/15
BSif	<b>2.6</b> (3)	<b>2.5</b> (1)	<b>1.6</b> (2)	<b>1.9</b> (3)	3.3(5)	15/15
BSqi	<b>2.6</b> (2)	<b>2.4</b> (2)	<b>1.9</b> (3)	<b>2.0</b> (2)	6.6(6)	15/15
BSrr	<b>2.6</b> (2)	<b>2.5</b> (2)	<b>1.6</b> (1)	<b>2.0</b> (2)	3.7(6)	15/15
CMA-CSA	<b>2.3</b> (2)	3.2(3)	5.9(5)	8.9(8)	13(18)	15/15
CMA-MSR	<b>2.5</b> (4)	3.7(10)	3.1(3)	6.0(3)	3.2(4)	15/15
CMA-TPA	3.2(2)	3.8(5)	3.4(3)	12(5)	16(12)	15/15
GP1-CMAES	<b>1.9</b> (3)	<b>2.7</b> (2)	3.2(3)	6.5(4)	4.9(2)	6/15
GP5-CMAES	<b>2.4</b> (4)	<b>2.0</b> (2)	<b>2.4</b> (2)	3.0(4)	<b>2.2</b> (4)	11/15
IPOPCMAv3p	<b>2.3</b> (4)	<b>2.2</b> (3)	3.4(1)	3.8(3)	12(29)	3/15
LHD-10xDef	3.9(5)	3.4(3)	3.3(2)	4.3(8)	6.8(5)	1/15
LHD-2xDefa	3.1(4)	3.8(2)	3.8(3)	10(11)	$\infty$ 250	0/15
RAND-2xDef	<b>2.5</b> (1)	<b>2.7</b> (2)	<b>2.1</b> (2)	4.6(4)	7.1(7)	1/15
RF1-CMAES	<b>1.8</b> (2)	<b>2.0</b> (2)	<b>3.0</b> (2)	8.7(13)	$\infty$ 1260	0/15
RF5-CMAES	<b>2.4</b> (2)	<b>1.5</b> (3)	3.3(2)	4.0(3)	$\infty$ 1288	0/15
Sifeg	3.4(9)	<b>2.9</b> (3)	<b>1.7</b> (1)	<b>2.8</b> (2)	<b>2.7</b> (2)	15/15
Sif	3.4(2)	3.2(3)	<b>1.8</b> (1)	3.0(3)	<b>2.8</b> (3)	15/15
Srr	3.4(2)	3.2(3)	<b>2.3</b> (3)	3.4(3)	<b>2.5</b> (3)	15/15

Table 73: 05-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f24</i></b>	<i>6.3e+1:15</i>	<i>4.0e+1:37</i>	<i>4.0e+1:37</i>	<i>2.5e+1:118</i>	<i>1.6e+1:692</i>	15/15
BSifeg	<b>1.6</b> (0.4)	3.8(2)	3.8(6)	32(14)	20(19)	14/15
BSif	<b>1.6</b> (0.9)	<b>2.5</b> (7)	<b>2.5</b> (4)	37(52)	17(11)	14/15
BSqi	<b>2.8</b> (0.3)	<b>2.9</b> (3)	<b>2.9</b> (7)	31(3)	18(18)	14/15
BSrr	<b>1.5</b> (0.6)	3.3(2)	3.3(0.6)	41(100)	32(77)	11/15
CMA-CSA	<b>2.0</b> (1)	<b>2.1</b> (2)	<b>2.1</b> (0.9)	<b>1.5</b> (2)	<b>1.6</b> (2)	15/15
CMA-MSR	<b>2.2</b> (2)	<b>2.6</b> (0.6)	<b>2.6</b> (1)	<b>1.8</b> (0.8)	<b>0.93</b> (2)	15/15
CMA-TPA	<b>1.9</b> (1)	<b>1.9</b> (0.8)	<b>1.9</b> (1)	<b>1.9</b> (1.0)	<b>1.4</b> (1)	15/15
GP1-CMAES	<b>1.7</b> (1)	<b>1.7</b> (0.5)	<b>1.7</b> (0.9)	<b>1.3</b> (1.0)	<b>1.1</b> (1.0)	13/15
GP5-CMAES	<b>1.5</b> (1.0)	<b>1.1</b> (0.4)	<b>1.1</b> (0.4)	<b>2.5</b> (2)	<b>1.6</b> (2)	9/15
IPOPCMAv3p	<b>2.0</b> (1)	<b>2.3</b> (2)	<b>2.3</b> (1)	<b>1.6</b> (1)	<b>1.1</b> (0.7)	12/15
LHD-10xDef	<b>2.7</b> (2)	6.5(2)	6.5(9)	4.8(3)	$\infty$ 250	0/15
LHD-2xDefa	<b>1.9</b> (2)	3.4(4)	3.4(5)	$\infty$	$\infty$ 250	0/15
RAND-2xDef	<b>1.7</b> (2)	7.3(9)	7.3(6)	15(16)	$\infty$ 250	0/15
RF1-CMAES	<b>1.9</b> (1)	<b>2.4</b> (3)	<b>2.4</b> (3)	<b>2.4</b> (4)	<b>1.9</b> (2)	9/15
RF5-CMAES	<b>1.8</b> (2)	3.6(6)	3.6(6)	4.1(4)	<b>2.9</b> (2)	7/15
Sifeg	<b>1.8</b> (2)	<b>1.7</b> (2)	<b>1.7</b> (2)	13(2)	4.8(2)	15/15
Sif	<b>1.7</b> (1)	<b>1.7</b> (3)	<b>1.7</b> (2)	<b>2.9</b> (2)	4.8(11)	15/15
Srr	<b>1.8</b> (0.6)	<b>1.6</b> (1)	<b>1.6</b> (1)	7.3(3)	5.8(1.0)	15/15

Table 74: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>4.0e+1:8.0</i>	<i>2.5e+1:16</i>	<i>1.0e-8:23</i>	<i>1.0e-8:23</i>	<i>1.0e-8:23</i>	15/15
BSifeg	<b>3.2</b> (1.0)	<b>2.0</b> (0.2)	<b>2.4</b> (0.3)	<b>2.4</b> (0.3)	<b>2.4</b> (0.2)	15/15
BSif	<b>3.2</b> (0.9)	<b>2.0</b> (0.2)	<b>2.4</b> (0.2)	<b>2.4</b> (0.2)	<b>2.4</b> (0.2)	15/15
BSqi	<b>3.2</b> (0.8)	<b>2.0</b> (0.2)	<b>2.4</b> (0.2)	<b>2.4</b> (0.3)	<b>2.4</b> (0.2)	15/15
BSrr	<b>3.2</b> (0.7)	<b>2.0</b> (0.1)	<b>2.4</b> (0.2)	<b>2.4</b> (0.2)	<b>2.4</b> (0.2)	15/15
CMA-CSA	5.2(4)	3.7(1)	63(5)	63(7)	63(5)	15/15
CMA-MSR	4.4(2)	5.2(2)	87(5)	87(10)	87(5)	15/15
CMA-TPA	7.5(6)	5.5(3)	51(5)	51(4)	51(6)	15/15
GP1-CMAES	3.6(3)	<b>2.6</b> (0.7)	43(7)	43(8)	43(8)	15/15
GP5-CMAES	<b>3.0</b> (2)	<b>1.9</b> (1.0)	404(275)	404(741)	404(248)	4/15
IPOPCMAv3p	5.0(4)	3.9(2)	65(4)	65(3)	65(2)	15/15
LHD-10xDef	9.4(9)	12(5)	$\infty$	$\infty$	$\infty$ 500	0/15
LHD-2xDefa	5.0(2)	<b>2.9</b> (1)	$\infty$	$\infty$	$\infty$ 500	0/15
RAND-2xDef	4.2(2)	<b>2.9</b> (1.0)	$\infty$	$\infty$	$\infty$ 500	0/15
RF1-CMAES	4.3(2)	3.2(2)	522(508)	522(673)	522(761)	3/15
RF5-CMAES	3.9(2)	<b>2.7</b> (1)	$\infty$	$\infty$	$\infty$ 2514	0/15
Sifeg	<b>3.2</b> (1)	<b>2.0</b> (0.2)	12(2)	12(2)	12(1)	15/15
Sif	<b>3.2</b> (1)	<b>2.0</b> (0.2)	11(2)	11(2)	11(2)	15/15
Srr	<b>3.2</b> (0.9)	<b>2.0</b> (0.5)	11(2)	11(2)	11(2)	15/15

Table 75: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>2.5e+6</i> :5.6	<i>1.0e+6</i> :17	<i>1.0e+5</i> :33	<i>2.5e+3</i> :118	<i>1.0e-8</i> :196	15/15
BSifeg	5.4(4)	<b>2.4</b> (0.9)	<b>1.5</b> (0.3)	<b>0.54</b> (0.2)	<b>1.2</b> (0.2)	15/15
BSif	5.4(2)	<b>2.4</b> (1)	<b>1.5</b> (0.1)	<b>0.56</b> (0.1)	<b>1.2</b> (0.3)	15/15
BSqi	5.4(4)	<b>2.4</b> (0.9)	<b>1.5</b> (0.3)	<b>0.51</b> (0.1)	<b>1.2</b> (0.2)	15/15
BSrr	5.4(4)	<b>2.4</b> (1)	<b>1.5</b> (0.2)	<b>0.54</b> (0.2)	<b>1.2</b> (0.2)	15/15
CMA-CSA	<b>2.3</b> (2)	<b>2.1</b> (3)	7.4(3)	8.5(4)	23(1.0)	15/15
CMA-MSR	3.2(2)	<b>3.0</b> (2)	7.3(2)	8.7(4)	26(2)	15/15
CMA-TPA	<b>1.8</b> (2)	<b>1.8</b> (1)	5.8(3)	7.4(2)	23(1)	15/15
GP1-CMAES	<b>1.4</b> (1)	<b>1.1</b> (0.6)	4.8(3)	7.5(2)	$\infty$ <i>2502</i>	0/15
GP5-CMAES	<b>2.8</b> (3)	<b>1.9</b> (2)	3.5(1)	3.2(0.8)	$\infty$ <i>2502</i>	0/15
IPOPCMAv3p	<b>2.5</b> (3)	<b>2.0</b> (3)	6.0(3)	10(3)	$\infty$ <i>2502</i>	0/15
LHD-10xDef	<b>1.5</b> (0.8)	<b>1.2</b> (0.8)	9.0(3)	$\infty$	$\infty$ <i>500</i>	0/15
LHD-2xDefa	<b>1.5</b> (2)	<b>1.5</b> (1)	5.5(2)	$\infty$	$\infty$ <i>500</i>	0/15
RAND-2xDef	<b>1.8</b> (2)	<b>1.8</b> (1)	5.1(4)	$\infty$	$\infty$ <i>500</i>	0/15
RF1-CMAES	<b>2.3</b> (2)	<b>2.4</b> (2)	7.7(7)	58(30)	$\infty$ <i>2502</i>	0/15
RF5-CMAES	<b>2.4</b> (3)	<b>2.3</b> (1)	34(35)	317(661)	$\infty$ <i>2504</i>	0/15
Sifeg	5.5(4)	<b>2.6</b> (0.5)	<b>1.8</b> (0.3)	<b>0.69</b> (0.1)	<b>1.7</b> (0.2)	15/15
Sif	5.5(4)	<b>2.6</b> (0.9)	<b>1.8</b> (0.3)	<b>0.73</b> (0.1)	<b>1.7</b> (0.2)	15/15
Srr	5.5(4)	<b>2.6</b> (0.9)	<b>1.8</b> (0.2)	<b>0.68</b> (0.0)	<b>1.7</b> (0.2)	15/15

Table 76: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>4.0e+2:8.2</i>	<i>1.6e+2:37</i>	<i>1.0e+2:69</i>	<i>6.3e+1:147</i>	<i>2.5e+1:1129</i>	15/15
BSifeg	<b>2.9</b> (0.5)	<b>1.1</b> (0.1)	<b>0.69</b> (0.1)	<b>0.41</b> (0.1)	<b>0.11</b> (0.0)	15/15
BSif	<b>2.9</b> (0.9)	<b>1.1</b> (0.1)	<b>0.69</b> (0.1)	<b>0.43</b> (0.2)	<b>0.12</b> (0.0)	15/15
BSqi	<b>2.9</b> (0.9)	<b>1.1</b> (0.1)	<b>0.69</b> (0.1)	<b>0.41</b> (0.1)	<b>0.10</b> (0.0)	15/15
BSrr	<b>2.9</b> (0.8)	<b>1.1</b> (0.0)	<b>0.69</b> (0.1)	<b>0.42</b> (0.1)	<b>0.09</b> (0.0)	15/15
CMA-CSA	<b>2.6</b> (2)	<b>2.8</b> (2)	3.1(1)	<b>2.8</b> (0.7)	<b>1.4</b> (1)	15/15
CMA-MSR	<b>2.3</b> (2)	3.3(1)	3.1(1)	<b>2.8</b> (0.6)	<b>1.4</b> (2)	15/15
CMA-TPA	3.2(4)	3.3(2)	<b>2.8</b> (0.7)	<b>2.4</b> (1)	<b>1.1</b> (1)	15/15
GP1-CMAES	<b>1.8</b> (2)	<b>2.2</b> (0.8)	<b>2.2</b> (0.7)	<b>2.5</b> (1)	<b>1.8</b> (3)	11/15
GP5-CMAES	<b>1.9</b> (2)	<b>1.7</b> (0.6)	<b>1.6</b> (0.6)	6.6(7)	32(68)	1/15
IPOPCMAv3p	<b>2.8</b> (3)	<b>2.7</b> (1)	3.1(2)	3.4(1)	<b>1.3</b> (0.3)	13/15
LHD-10xDef	<b>2.3</b> (3)	5.7(0.1)	3.7(0.4)	<b>2.4</b> (0.2)	<b>2.1</b> (2)	3/15
LHD-2xDefa	<b>1.8</b> (2)	<b>2.2</b> (1)	<b>2.5</b> (1)	3.4(4)	$\infty$ 500	0/15
RAND-2xDef	<b>1.1</b> (0.7)	<b>1.8</b> (0.4)	<b>1.7</b> (0.3)	<b>1.8</b> (0.7)	<b>2.0</b> (2)	3/15
RF1-CMAES	<b>1.7</b> (2)	<b>1.9</b> (1)	<b>2.1</b> (0.7)	<b>2.1</b> (0.7)	<b>1.6</b> (2)	10/15
RF5-CMAES	<b>2.5</b> (1)	4.6(0.7)	5.4(6)	8.5(8)	31(34)	1/15
Sifeg	<b>2.9</b> (0.9)	<b>1.1</b> (0.1)	<b>0.74</b> (0.1)	<b>0.46</b> (0.1)	<b>0.14</b> (0.0)	15/15
Sif	<b>2.9</b> (0.5)	<b>1.1</b> (0.1)	<b>0.74</b> (0.1)	<b>0.48</b> (0.1)	<b>0.14</b> (0.0)	15/15
Srr	<b>2.9</b> (0.6)	<b>1.1</b> (0.1)	<b>0.74</b> (0.1)	<b>0.46</b> (0.1)	<b>0.14</b> (0.0)	15/15

Table 77: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>2.5e+2:21</i>	<i>1.6e+2:59</i>	<i>1.6e+2:59</i>	<i>6.3e+1:139</i>	<i>4.0e+1:854</i>	15/15
BSifeg	<b>1.6</b> (1)	<b>0.86</b> (0.4)	<b>0.86</b> (0.4)	<b>0.89</b> (0.3)	<b>0.20</b> (0.1)	15/15
BSif	<b>1.6</b> (1)	<b>0.86</b> (0.2)	<b>0.86</b> (0.2)	<b>0.97</b> (0.2)	<b>0.20</b> (0.0)	15/15
BSqi	<b>1.6</b> (0.9)	<b>0.86</b> (0.3)	<b>0.86</b> (0.1)	<b>0.92</b> (0.5)	<b>0.23</b> (0.1)	15/15
BSrr	<b>1.6</b> (0.6)	<b>0.86</b> (0.4)	<b>0.86</b> (0.5)	<b>0.85</b> (0.2)	<b>0.20</b> (0.1)	15/15
CMA-CSA	4.6(2)	<b>2.9</b> (1)	<b>2.9</b> (1)	4.3(2)	<b>1.3</b> (3)	15/15
CMA-MSR	5.3(3)	3.4(1)	3.4(0.9)	5.2(0.4)	<b>2.2</b> (1)	15/15
CMA-TPA	5.3(4)	<b>3.0</b> (1)	<b>3.0</b> (0.9)	5.4(0.7)	<b>2.3</b> (2)	15/15
GP1-CMAES	4.3(2)	3.5(1)	3.5(1)	11(6)	4.2(4)	8/15
GP5-CMAES	3.8(3)	3.1(3)	3.1(3)	$\infty$	$\infty$ <i>2516</i>	0/15
IPOPCMAv3p	4.4(4)	3.2(1)	3.2(1)	5.2(3)	<b>1.6</b> (0.3)	13/15
LHD-10xDef	12(4)	8.2(7)	8.2(6)	$\infty$	$\infty$ <i>500</i>	0/15
LHD-2xDefa	4.4(3)	3.8(2)	3.8(1)	53(72)	$\infty$ <i>500</i>	0/15
RAND-2xDef	4.2(2)	3.2(2)	3.2(1)	12(29)	8.7(11)	1/15
RF1-CMAES	4.8(2)	3.2(2)	3.2(2)	13(14)	42(111)	1/15
RF5-CMAES	17(46)	24(17)	24(19)	267(238)	$\infty$ <i>2504</i>	0/15
Sifeg	<b>1.7</b> (0.8)	<b>0.94</b> (0.3)	<b>0.94</b> (0.3)	<b>0.82</b> (0.2)	<b>0.17</b> (0.0)	15/15
Sif	<b>1.7</b> (1)	<b>0.94</b> (0.2)	<b>0.94</b> (0.4)	<b>0.82</b> (0.3)	<b>0.16</b> (0.0)	15/15
Srr	<b>1.7</b> (0.4)	<b>0.95</b> (0.2)	<b>0.95</b> (0.2)	<b>0.79</b> (0.1)	<b>0.16</b> (0.0)	15/15

Table 78: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f5</b>	<i>1.0e+2</i> :16	<i>6.3e+1</i> :19	<i>1.0e-8</i> :20	<i>1.0e-8</i> :20	<i>1.0e-8</i> :20	15/15
BSifeg	<b>1.5</b> (0.2)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSif	<b>1.5</b> (0.2)	<b>1.4</b> (0.2)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSqi	<b>1.5</b> (0.2)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSrr	<b>1.5</b> (0.2)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
CMA-CSA	<b>1.8</b> (2)	<b>2.4</b> (1)	6.1(1)	6.1(2)	6.1(1)	15/15
CMA-MSR	<b>1.6</b> (1)	<b>2.0</b> (1)	5.4(2)	5.4(1)	5.4(2)	15/15
CMA-TPA	<b>1.3</b> (0.8)	<b>2.1</b> (1)	5.0(2)	5.0(2)	5.0(1)	15/15
GP1-CMAES	<b>1.4</b> (0.8)	<b>1.9</b> (0.3)	42(26)	42(39)	42(30)	15/15
GP5-CMAES	<b>1.3</b> (0.9)	<b>1.6</b> (0.5)	5.4(4)	5.4(3)	5.4(2)	15/15
IPOPCMAv3p	<b>1.6</b> (1)	<b>2.8</b> (0.6)	29(11)	29(9)	29(6)	15/15
LHD-10xDef	4.5(6)	11(1.0)	12(0.3)	12(0.4)	12(0.2)	15/15
LHD-2xDefa	<b>2.4</b> (0.8)	<b>2.3</b> (0.3)	<b>3.0</b> (0.1)	<b>3.0</b> (0.2)	<b>3.0</b> (0.2)	15/15
RAND-2xDef	<b>2.6</b> (0.2)	<b>2.4</b> (0.1)	3.1(0.3)	3.1(0.2)	3.1(0.2)	15/15
RF1-CMAES	<b>1.7</b> (0.9)	<b>2.4</b> (1)	35(28)	35(19)	35(17)	15/15
RF5-CMAES	<b>1.4</b> (1)	<b>2.2</b> (0.9)	120(198)	120(86)	120(81)	10/15
Sifeg	<b>1.5</b> (0.3)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
Sif	<b>1.5</b> (0.2)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
Srr	<b>1.5</b> (0.2)	<b>1.4</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15

Table 79: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>1.6e+5</i> :7.0	<i>6.3e+4</i> :16	<i>4.0e+2</i> :36	<i>1.0e+2</i> :102	<i>4.0e+0</i> :504	15/15
BSifeg	<b>1.6</b> (2)	<b>1.4</b> (1)	<b>1.2</b> (0.8)	38(23)	1260(1610)	2/15
BSif	<b>1.6</b> (2)	<b>1.4</b> (1.0)	<b>1.4</b> (0.4)	64(103)	862(1268)	3/15
BSqi	<b>1.6</b> (1)	<b>1.4</b> (0.6)	<b>1.2</b> (0.8)	30(86)	255(280)	7/15
BSrr	<b>1.6</b> (1)	<b>1.4</b> (0.9)	<b>1.2</b> (0.9)	42(24)	694(177)	3/15
CMA-CSA	<b>1.6</b> (1)	<b>1.5</b> (1)	<b>1.8</b> (2)	3.6(1)	<b>1.8</b> (0.3)	15/15
CMA-MSR	<b>2.7</b> (4)	<b>1.8</b> (3)	<b>2.2</b> (1)	<b>2.8</b> (0.7)	<b>1.6</b> (0.4)	15/15
CMA-TPA	<b>2.4</b> (3)	<b>2.2</b> (1)	4.8(3)	3.8(1)	<b>1.8</b> (0.3)	15/15
GP1-CMAES	<b>2.6</b> (2)	<b>1.8</b> (1)	<b>2.2</b> (1)	<b>2.1</b> (0.5)	4.8(4)	11/15
GP5-CMAES	<b>2.4</b> (3)	<b>1.5</b> (1)	<b>1.3</b> (0.3)	5.7(8)	$\infty$ <i>2516</i>	0/15
IPOPCMAv3p	<b>2.7</b> (2)	<b>1.9</b> (4)	<b>2.8</b> (3)	3.0(2)	<b>1.7</b> (0.6)	15/15
LHD-10xDef	<b>1.9</b> (3)	4.1(2)	5.8(0.3)	7.2(8)	$\infty$ <i>500</i>	0/15
LHD-2xDefa	<b>2.1</b> (2)	<b>1.8</b> (1)	<b>1.5</b> (0.6)	6.3(9)	$\infty$ <i>500</i>	0/15
RAND-2						



Table 80: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f7</i></b>	<i>2.5e+2:9.2</i>	<i>1.6e+2:18</i>	<i>1.0e+2:33</i>	<i>1.0e+1:172</i>	<i>4.0e+0:678</i>	15/15
BSifeg	<b>2.2</b> (2)	<b>1.5</b> (0.9)	14(32)	1100(1642)	2095(2465)	1/15
BSif	<b>2.2</b> (2)	<b>1.5</b> (0.9)	14(16)	882(1047)	2193(1494)	1/15
BSqi	<b>2.2</b> (2)	<b>1.5</b> (1)	14(16)	931(1437)	1037(898)	2/15
BSrr	<b>2.2</b> (2)	<b>1.5</b> (0.8)	14(31)	894(1247)	$\infty$ <i>1e5</i>	0/15
CMA-CSA	4.2(5)	3.3(2)	<b>2.9</b> (1)	<b>2.3</b> (0.8)	<b>1.1</b> (0.8)	15/15
CMA-MSR	3.5(2)	3.1(2)	3.2(1)	<b>1.9</b> (0.5)	<b>0.83</b> (0.9)	15/15
CMA-TPA	<b>2.8</b> (2)	<b>2.8</b> (2)	<b>2.7</b> (2)	<b>1.7</b> (0.6)	<b>1.2</b> (1.0)	15/15
GP1-CMAES	3.2(2)	<b>2.3</b> (1)	<b>2.1</b> (0.9)	<b>1.6</b> (0.7)	<b>1.1</b> (1)	15/15
GP5-CMAES	<b>2.3</b> (2)	<b>1.7</b> (1)	<b>1.4</b> (0.6)	<b>1.0</b> (0.3)*	<b>0.79</b> (0.4)	15/15
IPOPCMAv3p	<b>2.8</b> (3)	<b>3.0</b> (3)	<b>2.5</b> (1)	<b>2.6</b> (3)	<b>0.85</b> (1)	15/15
LHD-10xDef	<b>2.4</b> (3)	4.5(4)	5.4(3)	10(5)	$\infty$ <i>500</i>	0/15
LHD-2xDefa	<b>2.3</b> (3)	<b>2.4</b> (2)	<b>2.3</b> (0.3)	43(20)	$\infty$ <i>500</i>	0/15
RAND-2xDef	3.2(3)	3.0(1)	<b>2.6</b> (1)	13(9)	$\infty$ <i>500</i>	0/15
RF1-CMAES	4.2(3)	3.6(3)	<b>3.0</b> (2)	13(26)	12(12)	4/15
RF5-CMAES	3.3(2)	<b>2.9</b> (2)	3.2(5)	31(47)	28(21)	2/15
Sifeg	<b>2.2</b> (2)	<b>1.6</b> (0.9)	5.5(0.3)	281(354)	363(508)	5/15
Sif	<b>2.2</b> (2)	<b>1.6</b> (0.9)	5.5(17)	166(150)	444(486)	4/15
Srr	<b>2.2</b> (2)	<b>1.6</b> (1)	5.5(0.7)	217(540)	220(211)	7/15

Table 81: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>1.6e+4</i> :15	<i>1.0e+4</i> :22	<i>1.6e+3</i> :34	<i>2.5e+2</i> :103	<i>4.0e+0</i> :727	15/15
BSifeg	<b>1.9</b> (0.1)	<b>1.5</b> (0.1)	<b>1.2</b> (0.1)	<b>1.3</b> (0.4)	51(29)	13/15
BSif	<b>1.9</b> (0.9)	<b>1.5</b> (0.9)	<b>1.2</b> (0.1)	<b>0.93</b> (0.1)	123(268)	10/15
BSqi	<b>1.9</b> (0.9)	<b>1.5</b> (0.5)	<b>1.2</b> (0.1)	<b>0.99</b> (2)	30(40)	15/15
BSrr	<b>1.9</b> (1)	<b>1.5</b> (0.4)	<b>1.2</b> (0.1)	<b>0.68</b> (0.4)	35(44)	13/15
CMA-CSA	4.2(5)	3.6(4)	5.0(3)	3.6(2)	<b>4.9</b> (4)	15/15
CMA-MSR	4.4(3)	3.9(3)	6.0(2)	3.3(1)	<b>5.3</b> (12)	15/15
CMA-TPA	3.8(4)	3.3(2)	4.0(1)	<b>2.2</b> (0.8)	5.4(5)	15/15
GP1-CMAES	<b>2.9</b> (2)	<b>2.5</b> (1)	3.1(0.4)	<b>2.3</b> (1)	12(16)	4/15
GP5-CMAES	<b>2.3</b> (0.9)	<b>1.7</b> (0.7)	<b>2.2</b> (0.7)	<b>1.8</b> (0.5)	$\infty$ 2516	0/15
IPOPCMAv3p	3.2(3)	<b>3.0</b> (3)	4.4(2)	<b>2.5</b> (0.6)	<b>4.1</b> (2)	11/15
LHD-10xDef	8.1(7)	7.1(4)	6.8(0.4)	3.2(0.5)	$\infty$ 500	0/15
LHD-2xDefa	3.3(0.3)	<b>2.3</b> (0.4)	<b>2.5</b> (0.4)	<b>2.5</b> (0.6)	$\infty$ 500	0/15
RAND-2xDef	3.3(0.2)	<b>2.5</b> (0.5)	<b>2.6</b> (0.9)	<b>2.4</b> (0.6)	$\infty$ 500	0/15
RF1-CMAES	4.1(2)	3.4(1)	4.3(2)	3.3(5)	$\infty$ 2502	0/15
RF5-CMAES	<b>2.9</b> (2)	<b>2.4</b> (1)	10(1)	15(18)	$\infty$ 2514	0/15
Sifeg	<b>1.9</b> (1)	<b>1.5</b> (0.1)	<b>1.3</b> (0.1)	<b>0.66</b> (0.2)	26(43)	15/15
Sif	<b>1.9</b> (1)	<b>1.5</b> (0.5)	<b>1.3</b> (0.1)	<b>0.68</b> (0.3)	31(66)	14/15
Srr	<b>1.9</b> (1)	<b>1.5</b> (0.4)	<b>1.3</b> (0.1)	<b>0.65</b> (0.1)	39(125)	13/15

Table 82: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>4.0e+1</i> :125	<i>2.5e+1</i> :148	<i>1.6e+1</i> :180	<i>1.0e+1</i> :200	<i>1.6e+0</i> :563	15/15
BSifeg	59(140)	53(131)	46(17)	47(169)	1100(1053)	2/15
BSif	239(371)	267(723)	239(393)	247(362)	2383(4152)	1/15
BSqi	47(120)	43(24)	38(81)	37(140)	1041(1197)	2/15
BSrr	47(38)	43(10)	37(24)	37(19)	1006(1142)	2/15
CMA-CSA	<b>3.5</b> (2)	<b>3.4</b> (2)	<b>3.1</b> (0.4)	<b>3.3</b> (0.5)	<b>5.2</b> (1)	15/15
CMA-MSR	4.5(2)	4.2(1.0)	3.8(1)	4.0(0.5)	<b>5.8</b> (4)	15/15
CMA-TPA	4.6(7)	<b>4.1</b> (4)	<b>3.6</b> (8)	<b>3.7</b> (2)	<b>5.0</b> (3)	15/15
GP1-CMAES	<b>4.3</b> (4)	4.2(0.6)	3.9(2)	4.3(1.0)	66(29)	1/15
GP5-CMAES	28(11)	71(76)	93(137)	84(139)	$\infty$ 2526	0/15
IPOPCMAv3p	<b>3.8</b> (2)	<b>3.5</b> (2)	<b>3.2</b> (0.4)	<b>3.5</b> (2)	33(101)	2/15
LHD-10xDef	19(16)	50(54)	42(31)	$\infty$	$\infty$ 500	0/15
LHD-2xDefa	11(9)	12(7)	$\infty$	$\infty$	$\infty$ 500	0/15
RAND-2xDef	14(15)	25(54)	$\infty$	$\infty$	$\infty$ 500	0/15
RF1-CMAES	14(13)	15(19)	13(14)	16(16)	$\infty$ 2502	0/15
RF5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ 2504	0/15
Sifeg	69(179)	59(151)	49(126)	46(114)	2334(2673)	1/15
Sif	52(180)	45(151)	38(125)	37(3)	1159(1546)	2/15
Srr	33(53)	28(55)	24(47)	22(4)	2211(2228)	1/15

Table 83: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>2.5e+6:6.0</i>	<i>1.0e+6:21</i>	<i>4.0e+5:38</i>	<i>2.5e+4:104</i>	<i>6.3e+2:512</i>	15/15
BSifeg	<b>1.9</b> (3)	<b>1.2</b> (1)	7.7(50)	481(363)	$\infty$ 7e4	0/15
BSif	<b>1.9</b> (2)	<b>1.2</b> (0.9)	7.5(25)	413(1203)	$\infty$ 7e4	0/15
BSqi	<b>1.9</b> (2)	<b>1.2</b> (1)	4.5(26)	438(558)	$\infty$ 8e4	0/15
BSrr	<b>1.9</b> (2)	<b>1.2</b> (1.0)	3.6(0.7)	334(281)	$\infty$ 5e4	0/15
CMA-CSA	<b>2.4</b> (2)	<b>1.1</b> (0.7)	<b>2.5</b> (3)	5.0(1)	<b>2.8</b> (0.6)	15/15
CMA-MSR	<b>2.8</b> (2)	<b>1.6</b> (1)	<b>2.2</b> (1)	3.5(0.9)	<b>2.7</b> (0.3)	15/15
CMA-TPA	<b>1.2</b> (2)	<b>1.4</b> (1)	<b>1.9</b> (1)	<b>3.5</b> (1.0)	<b>2.4</b> (0.7)	15/15
GP1-CMAES	<b>2.0</b> (2)	<b>1.2</b> (2)	<b>1.2</b> (0.9)	<b>2.9</b> (2)	<b>2.2</b> (0.6)	15/15
GP5-CMAES	3.2(3)	<b>1.5</b> (0.9)	<b>1.2</b> (0.9)	<b>1.8</b> (1)	<b>1.0</b> (0.5)	15/15
IPOPCMAv3p	<b>1.9</b> (1)	<b>1.2</b> (2)	<b>2.3</b> (2)	4.1(2)	3.1(0.7)	15/15
LHD-10xDef	<b>2.4</b> (4)	<b>1.6</b> (2)	3.7(2)	11(7)	$\infty$ 500	0/15
LHD-2xDefa	<b>2.1</b> (2)	<b>1.5</b> (1)	<b>1.9</b> (0.9)	6.6(7)	$\infty$ 500	0/15
RAND-2xDef	<b>1.5</b> (1)	<b>1.1</b> (1)	<b>1.4</b> (1)	12(22)	$\infty$ 500	0/15
RF1-CMAES	<b>1.4</b> (0.9)	<b>1.3</b> (1)	<b>1.7</b> (2)	7.6(8)	$\infty$ 2502	0/15
RF5-CMAES	<b>2.2</b> (2)	<b>1.2</b> (0.6)	<b>2.3</b> (2)	61(79)	$\infty$ 2504	0/15
Sifeg	<b>1.9</b> (1)	<b>1.1</b> (0.9)	<b>1.1</b> (0.4)	117(244)	$\infty$ 4e4	0/15
Sif	<b>1.9</b> (3)	<b>1.1</b> (0.8)	<b>1.1</b> (0.4)	139(186)	$\infty$ 4e4	0/15
Srr	<b>1.9</b> (3)	<b>1.1</b> (0.6)	<b>1.1</b> (0.4)	50(13)	$\infty$ 3e4	0/15

Table 84: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>4.0e+4</i> :6.4	<i>2.5e+3</i> :15	<i>6.3e+1</i> :217	<i>4.0e+1</i> :244	<i>2.5e+0</i> :675	15/15
BSifeg	<b>2.4</b> (1)	<b>2.2</b> (0.9)	1105(1450)	$\infty$	$\infty$ <i>7e4</i>	0/15
BSif	<b>2.4</b> (2)	<b>2.2</b> (1)	339(361)	2153(1833)	$\infty$ <i>8e4</i>	0/15
BSqi	<b>2.4</b> (1)	<b>2.2</b> (1)	363(529)	1107(417)	$\infty$ <i>8e4</i>	0/15
BSrr	<b>2.4</b> (1)	<b>2.2</b> (0.9)	503(409)	1283(718)	$\infty$ <i>4e4</i>	0/15
CMA-CSA	<b>1.5</b> (1.0)	4.0(3)	7.1(1)	6.6(0.6)	<b>2.9</b> (0.2)	15/15
CMA-MSR	3.8(4)	4.2(5)	6.5(0.9)	<b>6.3</b> (1)	<b>3.3</b> (0.2)	15/15
CMA-TPA	<b>2.1</b> (2)	3.1(2)	<b>5.8</b> (2)	<b>5.9</b> (1)	<b>3.0</b> (0.4)	15/15
GP1-CMAES	3.1(3)	3.3(2)	<b>6.4</b> (3)	7.8(1)	55(65)	1/15
GP5-CMAES	<b>2.9</b> (2)	<b>2.9</b> (2)	<b>3.5</b> (2)	<b>5.1</b> (1)	4.3(1)	11/15
IPOPCMAv3p	3.6(6)	4.1(3)	11(13)	18(10)	$\infty$ <i>2502</i>	0/15
LHD-10xDef	5.3(7)	5.3(4)	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
LHD-2xDefa	4.3(3)	3.7(3)	16(13)	$\infty$	$\infty$ <i>500</i>	0/15
RAND-2xDef	3.6(4)	3.9(3)	33(49)	$\infty$	$\infty$ <i>500</i>	0/15
RF1-CMAES	3.2(4)	4.3(3)	19(12)	153(192)	$\infty$ <i>2502</i>	0/15
RF5-CMAES	<b>2.4</b> (3)	3.2(2)	55(32)	154(201)	$\infty$ <i>2514</i>	0/15
Sifeg	<b>2.4</b> (2)	<b>2.3</b> (1)	225(495)	1601(2467)	$\infty$ <i>6e4</i>	0/15
Sif	<b>2.4</b> (2)	<b>2.3</b> (2)	244(228)	3570(4531)	$\infty$ <i>6e4</i>	0/15
Srr	<b>2.4</b> (1)	<b>2.3</b> (1)	208(235)	577(785)	$\infty$ <i>3e4</i>	0/15

Table 85: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>4.0e+7:15</i>	<i>2.5e+7:24</i>	<i>1.6e+7:34</i>	<i>1.0e+6:103</i>	<i>1.0e+1:515</i>	15/15
BSifeg	<b>2.2</b> (0.7)	<b>1.6</b> (0.3)	<b>1.3</b> (0.2)	<b>3.0</b> (11)	262(255)	5/15
BSif	<b>2.2</b> (0.1)	<b>1.6</b> (0.3)	<b>1.3</b> (0.3)	3.3(7)	353(240)	4/15
BSqi	<b>2.2</b> (0.6)	<b>1.6</b> (0.3)	<b>1.3</b> (0.1)	6.1(0.2)	42(61)	14/15
BSrr	<b>2.2</b> (0.3)	<b>1.6</b> (0.3)	<b>1.3</b> (0.3)	<b>2.8</b> (0.4)	62(108)	11/15
CMA-CSA	3.4(3)	3.3(2)	<b>2.7</b> (1)	<b>2.9</b> (1)	4.2(5)	15/15
CMA-MSR	3.9(3)	3.8(2)	3.7(1)	3.3(0.6)	4.9(4)	15/15
CMA-TPA	3.7(4)	4.2(3)	3.6(2)	<b>2.5</b> (0.5)	<b>3.6</b> (3)	15/15
GP1-CMAES	<b>2.3</b> (2)	<b>2.6</b> (1)	<b>3.0</b> (2)	<b>2.9</b> (3)	<b>2.9</b> (3)	13/15
GP5-CMAES	6.8(4)	13(9)	17(8)	28(34)	21(13)	3/15
IPOPCMAv3p	<b>3.0</b> (2)	3.2(2)	3.3(2)	<b>2.8</b> (0.7)	<b>2.8</b> (4)	13/15
LHD-10xDef	6.7(4)	8.6(2)	6.9(1)	6.2(8)	$\infty$ 500	0/15
LHD-2xDefa	3.6(2)	<b>2.8</b> (0.6)	<b>2.4</b> (0.8)	<b>2.6</b> (1)	$\infty$ 500	0/15
RAND-2xDef	<b>2.4</b> (2)	<b>2.3</b> (0.7)	<b>2.1</b> (1)	<b>2.2</b> (1)	$\infty$ 500	0/15
RF1-CMAES	4.4(4)	3.9(2)	3.1(1)	<b>2.5</b> (1)	4.2(3)	11/15
RF5-CMAES	3.5(4)	3.1(2)	3.2(3)	21(19)	$\infty$ 2504	0/15
Sifeg	<b>2.2</b> (0.4)	<b>1.6</b> (0.1)	<b>1.2</b> (0.2)	7.3(17)	74(104)	5/15
Sif	<b>2.2</b> (0.3)	<b>1.6</b> (0.2)	<b>1.2</b> (0.2)	4.1(6)	99(113)	4/15
Srr	<b>2.2</b> (0.8)	<b>1.6</b> (0.3)	<b>1.2</b> (0.0)	3.6(4)	20(33)	10/15

Table 86: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>1.0e+3:12</i>	<i>6.3e+2:32</i>	<i>4.0e+2:40</i>	<i>6.3e+1:154</i>	<i>2.5e+0:521</i>	15/15
BSifeg	<b>2.9</b> (0.8)	<b>1.4</b> (0.4)	3.4(0.1)	45(68)	163(104)	11/15
BSif	<b>2.9</b> (0.5)	<b>1.4</b> (0.2)	<b>1.6</b> (0.2)	88(7)	$\infty$ 9e4	0/15
BSqi	<b>2.9</b> (0.7)	<b>1.4</b> (0.3)	<b>1.6</b> (0.2)	34(96)	207(193)	8/15
BSrr	<b>2.9</b> (1.0)	<b>1.4</b> (0.1)	<b>1.5</b> (0.2)	35(52)	208(202)	8/15
CMA-CSA	4.5(2)	3.6(0.5)	4.6(2)	<b>3.0</b> (0.3)	<b>3.3</b> (2)	15/15
CMA-MSR	5.7(3)	4.3(2)	5.9(1)	3.4(0.8)	<b>2.7</b> (0.4)	15/15
CMA-TPA	6.5(3)	4.0(1)	4.7(0.9)	<b>2.7</b> (0.5)	3.6(2)	15/15
GP1-CMAES	3.7(1)	<b>2.5</b> (0.6)	3.1(0.5)	<b>1.9</b> (0.5)	5.9(4)	8/15
GP5-CMAES	<b>2.6</b> (1)	<b>1.6</b> (0.3)	<b>1.7</b> (0.4)	<b>0.91</b> (0.1)	3.9(3)	10/15
IPOPCMAv3p	4.5(3)	3.5(3)	5.0(1)	3.2(0.6)	5.3(4)	9/15
LHD-10xDef	14(7)	7.0(0.2)	5.8(0.2)	<b>2.2</b> (0.2)	$\infty$ 500	0/15
LHD-2xDefa	3.7(1)	<b>2.2</b> (0.7)	<b>2.5</b> (0.8)	<b>1.6</b> (0.4)	<b>3.4</b> (3)	4/15
RAND-2xDef	3.6(2)	<b>2.1</b> (0.5)	<b>2.2</b> (0.6)	<b>1.6</b> (0.4)	7.2(13)	2/15
RF1-CMAES	3.4(1.0)	3.0(1)	3.5(0.9)	3.1(1)	16(20)	4/15
RF5-CMAES	3.8(2)	3.4(2)	11(16)	245(241)	$\infty$ 2514	0/15
Sifeg	<b>2.9</b> (0.5)	<b>1.4</b> (0.2)	<b>1.4</b> (0.3)	16(56)	75(153)	13/15
Sif	<b>2.9</b> (1)	<b>1.4</b> (0.2)	<b>1.4</b> (0.1)	17(56)	97(132)	11/15
Srr	<b>2.9</b> (1)	<b>1.4</b> (0.2)	<b>1.4</b> (0.1)	21(0.6)	76(103)	13/15

Table 87: 10-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion



Table 88: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>2.5e+2:9.0</i>	<i>1.6e+2:72</i>	<i>1.0e+2:186</i>	<i>6.3e+1:450</i>	<i>4.0e+1:872</i>	15/15
BSifeg	3.5(1)	88(161)	78(251)	267(366)	1489(1436)	1/15
BSif	<b>3.5</b> (3)	72(0.8)	49(112)	198(356)	722(809)	2/15
BSqi	3.5(0.8)	83(300)	68(179)	277(480)	702(460)	2/15
BSrr	3.5(2)	46(12)	94(122)	163(100)	236(176)	5/15
CMA-CSA	4.9(2)	<b>1.4</b> (0.7)	<b>0.95</b> (0.5)	<b>1.1</b> (0.5)	<b>1.2</b> (0.4)	15/15
CMA-MSR	5.6(2)	<b>1.5</b> (0.7)	<b>1.2</b> (0.2)	<b>0.81</b> (0.2)	<b>0.57</b> (0.1)	15/15
CMA-TPA	6.9(4)	<b>1.8</b> (0.6)	<b>1.1</b> (0.3)	<b>0.94</b> (0.3)	<b>1.2</b> (0.7)	15/15
GP1-CMAES	4.3(5)	<b>1.1</b> (0.2)	<b>0.78</b> (0.3)	<b>0.79</b> (0.5)	<b>2.2</b> (2)	11/15
GP5-CMAES	<b>3.4</b> (2)	<b>0.75</b> (0.3)	<b>0.70</b> (0.4)	<b>3.0</b> (3)	41(65)	1/15
IPOPCMAv3p	3.9(3)	<b>1.3</b> (0.8)	<b>0.94</b> (0.4)	<b>0.92</b> (0.5)	<b>1.3</b> (2)	14/15
LHD-10xDef	10(10)	3.1(0.2)	<b>1.5</b> (0.2)	<b>0.83</b> (0.2)	<b>0.98</b> (0.6)	8/15
LHD-2xDefa	4.0(3)	<b>0.97</b> (0.4)	<b>0.71</b> (0.2)	<b>0.75</b> (1)	<b>0.97</b> (1)	7/15
RAND-2xDef	4.7(2)	<b>0.98</b> (0.4)	<b>0.71</b> (0.3)	<b>0.91</b> (1)	<b>1.9</b> (3)	4/15
RF1-CMAES	<b>3.2</b> (2)	<b>1.0</b> (0.5)	<b>0.83</b> (0.1)	<b>0.89</b> (0.4)	<b>0.99</b> (0.3)	14/15
RF5-CMAES	5.6(4)	3.3(0.5)	3.2(6)	4.4(5)	20(22)	2/15
Sifeg	3.8(2)	61(233)	56(43)	51(37)	138(134)	8/15
Sif	3.8(1)	61(114)	59(92)	76(154)	195(181)	6/15
Srr	3.7(3)	59(221)	65(130)	102(134)	153(115)	7/15

Table 89: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>4.0e+1:12</i>	<i>2.5e+1:47</i>	<i>1.6e+1:88</i>	<i>1.0e+1:425</i>	<i>4.0e+0:989</i>	15/15
BSifeg	<b>1.9</b> (2)	<b>1.0</b> (0.4)	13(33)	36(39)	105(92)	9/15
BSif	<b>1.9</b> (2)	<b>1.1</b> (0.7)	17(32)	38(45)	90(126)	9/15
BSqi	<b>1.9</b> (2)	<b>1.1</b> (0.6)	42(60)	60(96)	122(95)	8/15
BSrr	<b>1.9</b> (2)	<b>1.1</b> (0.6)	23(77)	18(27)	109(80)	8/15
CMA-CSA	<b>1.8</b> (1)	4.6(3)	6.9(4)	<b>1.8</b> (0.6)	<b>1.5</b> (3)	15/15
CMA-MSR	<b>2.5</b> (3)	<b>2.7</b> (2)	6.3(14)	<b>1.5</b> (0.4)	<b>2.5</b> (5)	15/15
CMA-TPA	4.5(5)	4.8(5)	10(8)	3.1(2)	<b>2.6</b> (3)	15/15
GP1-CMAES	<b>1.1</b> (0.8)	<b>2.4</b> (2)	3.2(3)	<b>1.1</b> (0.3)	<b>1.5</b> (2)	12/15
GP5-CMAES	<b>1.4</b> (2)	<b>1.6</b> (1.0)	<b>1.4</b> (0.4)	<b>0.39</b> (0.1)	<b>0.89</b> (1)	13/15
IPOPCMAv3p	<b>1.1</b> (1)	3.3(3)	7.7(3)	<b>2.4</b> (0.9)	<b>1.6</b> (1)	14/15
LHD-10xDef	<b>1.7</b> (2)	3.6(2)	3.7(3)	<b>1.6</b> (1)	$\infty$ 500	0/15
LHD-2xDefa	<b>1.4</b> (1)	<b>1.8</b> (0.7)	6.9(7)	5.4(4)	$\infty$ 500	0/15
RAND-2xDef	<b>1.3</b> (0.9)	<b>2.6</b> (3)	3.6(4)	<b>1.8</b> (2)	7.3(6)	1/15
RF1-CMAES	<b>1.6</b> (1)	3.1(2)	4.5(3)	<b>1.3</b> (0.8)	4.4(3)	6/15
RF5-CMAES	<b>1.5</b> (2)	<b>2.0</b> (2)	<b>2.4</b> (1)	3.6(6)	17(21)	2/15
Sifeg	<b>2.0</b> (3)	<b>1.5</b> (0.8)	<b>1.4</b> (0.8)	5.9(18)	28(12)	15/15
Sif	<b>2.0</b> (2)	<b>1.5</b> (1)	8.9(30)	4.2(4)	39(29)	14/15
Srr	<b>2.0</b> (3)	<b>1.5</b> (0.9)	12(54)	4.5(6)	21(27)	15/15

Table 90: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.0e+1:26</i>	<i>6.3e+0:85</i>	<i>4.0e+0:155</i>	<i>2.5e+0:238</i>	<i>6.3e-1:585</i>	15/15
BSifeg	<b>1.4</b> (1)	301(1177)	982(1814)	2734(4204)	$\infty$ <i>1e5</i>	0/15
BSif	<b>1.4</b> (0.9)	237(464)	965(1440)	1182(1806)	$\infty$ <i>1e5</i>	0/15
BSqi	<b>1.4</b> (0.6)	205(661)	740(647)	1684(1788)	$\infty$ <i>1e5</i>	0/15
BSrr	<b>1.4</b> (0.7)	296(592)	761(1122)	1812(1492)	$\infty$ <i>1e5</i>	0/15
CMA-CSA	3.4(2)	<b>2.1</b> (1.0)	<b>1.7</b> (0.7)	<b>1.6</b> (0.7)	<b>1.7</b> (3)	15/15
CMA-MSR	<b>2.0</b> (0.9)	<b>1.4</b> (0.6)	<b>1.2</b> (0.7)	<b>1.1</b> (0.3)	<b>2.8</b> (2)	15/15
CMA-TPA	<b>2.4</b> (2)	<b>1.4</b> (0.3)	<b>1.1</b> (0.3)	<b>1.0</b> (0.4)	<b>1.2</b> (0.2)	15/15
GP1-CMAES	<b>1.7</b> (0.8)	<b>1.0</b> (0.6)	<b>0.88</b> (0.3)	<b>0.80</b> (0.3)	<b>1.0</b> (0.2)	14/15
GP5-CMAES	<b>1.7</b> (1)	<b>1.1</b> (0.5)	<b>0.99</b> (0.8)	<b>2.4</b> (6)	18(26)	3/15
IPOPCMAv3p	<b>2.4</b> (2)	<b>1.4</b> (1)	<b>1.4</b> (0.4)	<b>1.3</b> (0.6)	<b>1.0</b> (0.2)	15/15
LHD-10xDef	3.5(4)	<b>2.7</b> (0.4)	<b>2.1</b> (0.6)	4.4(6)	$\infty$ <i>500</i>	0/15
LHD-2xDefa	<b>1.6</b> (0.8)	<b>0.99</b> (0.6)	<b>2.4</b> (2)	6.9(7)	$\infty$ <i>500</i>	0/15
RAND-2xDef	<b>1.8</b> (0.7)	<b>1.2</b> (0.8)	<b>1.7</b> (0.7)	3.7(3)	$\infty$ <i>500</i>	0/15
RF1-CMAES	<b>1.7</b> (2)	<b>1.3</b> (0.6)	<b>1.2</b> (0.4)	<b>3.0</b> (0.7)	13(17)	4/15
RF5-CMAES	<b>1.6</b> (0.2)	<b>2.6</b> (0.2)	5.0(6)	10(10)	64(29)	1/15
Sifeg	<b>1.3</b> (0.7)	208(202)	402(557)	440(736)	1223(2308)	2/15
Sif	<b>1.3</b> (0.8)	194(337)	490(1441)	834(1353)	$\infty$ <i>1e5</i>	0/15
Srr	<b>1.3</b> (0.4)	182(4)	429(1444)	487(629)	$\infty$ <i>1e5</i>	0/15

Table 91: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>4.0e+1</i> :11	<i>2.5e+1</i> :56	<i>1.6e+1</i> :172	<i>1.6e+1</i> :172	<i>2.5e+0</i> :561	15/15
BSifeg	3.2(5)	382(511)	354(420)	354(544)	2408(1070)	1/15
BSif	3.5(7)	362(748)	317(415)	317(529)	$\infty$ 1e5	0/15
BSqi	81(589)	223(397)	281(731)	281(287)	2341(1144)	1/15
BSrr	<b>3.0</b> (2)	305(691)	528(814)	528(532)	$\infty$ 9e4	0/15
CMA-CSA	6.7(6)	<b>2.5</b> (0.5)	<b>1.2</b> (0.7)	<b>1.2</b> (0.4)	<b>1.0</b> (0.2)	15/15
CMA-MSR	4.9(4)	<b>1.8</b> (0.3)	<b>0.99</b> (0.4)	<b>0.99</b> (0.3)	<b>1.9</b> (4)	15/15
CMA-TPA	5.1(4)	<b>2.1</b> (0.9)	<b>1.1</b> (0.3)	<b>1.1</b> (0.2)	<b>1.5</b> (0.3)	15/15
GP1-CMAES	4.4(5)	<b>1.7</b> (0.8)	<b>0.85</b> (0.5)	<b>0.85</b> (0.5)	<b>1.6</b> (1)	13/15
GP5-CMAES	3.7(6)	<b>1.3</b> (0.5)	<b>0.71</b> (0.2)	<b>0.71</b> (0.4)	6.0(10)	7/15
IPOPCMAv3p	4.7(3)	<b>2.1</b> (1)	<b>1.2</b> (0.6)	<b>1.2</b> (0.4)	<b>1.5</b> (0.3)	14/15
LHD-10xDef	8.2(9)	4.0(0.2)	<b>2.0</b> (2)	<b>2.0</b> (0.4)	$\infty$ 500	0/15
LHD-2xDefa	4.2(3)	<b>1.8</b> (1)	<b>1.8</b> (2)	<b>1.8</b> (2)	$\infty$ 500	0/15
RAND-2xDef	<b>3.0</b> (2)	<b>1.5</b> (0.6)	<b>1.6</b> (2)	<b>1.6</b> (3)	$\infty$ 500	0/15
RF1-CMAES	<b>2.8</b> (2)	<b>1.4</b> (0.8)	<b>0.95</b> (0.4)	<b>0.95</b> (0.5)	3.2(2)	10/15
RF5-CMAES	4.0(2)	4.5(22)	3.8(10)	3.8(10)	66(54)	1/15
Sifeg	8.3(2)	83(7)	171(286)	171(236)	1179(1377)	2/15
Sif	320(3)	194(671)	223(324)	223(553)	$\infty$ 1e5	0/15
Srr	6.7(2)	137(290)	184(432)	184(327)	$\infty$ 9e4	0/15

Table 92: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:618</i>	<i>1.0e-1:10609</i>	<i>6.3e-2:10623</i>	<i>4.0e-2:10625</i>	<i>2.5e-2:10644</i>	15/15
BSifeg	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
BSif	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
BSqi	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
BSrr	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
CMA-CSA	<b>171</b> <sup>(101)</sup>	<b>12</b> <sup>(5)</sup>	<b>19</b> <sup>(12)</sup>	<b>23</b> <sup>(10)</sup>	<b>26</b> <sup>(25)</sup>	15/15
CMA-MSR	<b>237</b> <sup>(437)</sup>	<b>21</b> <sup>(31)</sup>	<b>35</b> <sup>(55)</sup>	<b>62</b> <sup>(128)</sup>	<b>290</b> <sup>(257)</sup>	4/15
CMA-TPA	<b>156</b> <sup>(83)</sup>	<b>12</b> <sup>(5)</sup>	<b>18</b> <sup>(11)</sup>	<b>24</b> <sup>(13)</sup>	<b>34</b> <sup>(18)</sup>	15/15
GP1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2504</i>	0/15
GP5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2528</i>	0/15
IPOPCMAv3p	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2504</i>	0/15
LHD-10xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
LHD-2xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
RAND-2xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
RF1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2502</i>	0/15
RF5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2516</i>	0/15
Sifeg	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
Sif	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15
Srr	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1e5</i>	0/15

Table 93: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f20</b>	<i>1.0e+4:17</i>	<i>6.3e+3:21</i>	<i>6.3e+1:30</i>	<i>2.5e+0:122</i>	<i>1.0e+0:15426</i>	13/15
BSifeg	<b>1.9</b> (0.6)	<b>1.9</b> (0.1)	<b>1.7</b> (0.8)	<b>1.9</b> (2)	3.2(4)	12/15
BSif	<b>1.9</b> (0.1)	<b>1.9</b> (0.1)	<b>1.8</b> (1)	<b>1.8</b> (2)	3.5(3)	12/15
BSqi	<b>1.9</b> (0.1)	<b>1.9</b> (0.1)	<b>1.7</b> (0.5)	<b>1.1</b> (1)	3.4(7)	12/15
BSrr	<b>1.9</b> (1)	<b>1.9</b> (0.1)	<b>1.7</b> (0.4)	<b>1.4</b> (0.3)	<b>2.8</b> (3)	13/15
CMA-CSA	<b>2.3</b> (1)	<b>2.4</b> (2)	5.2(1)	5.5(2)	<b>1.8</b> (0.9)	15/15
CMA-MSR	3.1(3)	3.5(2)	5.7(2)	23(2)	$\infty$ <i>1e6</i>	0/15
CMA-TPA	3.1(2)	3.2(2)	5.1(0.9)	3.0(1)	18(0.3)	14/15
GP1-CMAES	<b>1.9</b> (2)	<b>2.0</b> (1)	3.8(1.0)	8.3(9)	$\infty$ <i>2502</i>	0/15
GP5-CMAES	<b>2.1</b> (1.0)	<b>1.9</b> (0.8)	<b>2.4</b> (0.6)	25(23)	$\infty$ <i>2526</i>	0/15
IPOPCMAv3p	3.2(3)	3.3(2)	5.4(2)	5.1(3)	<b>2.3</b> (5)	1/15
LHD-10xDef	3.6(6)	6.0(5)	7.7(0.3)	14(14)	$\infty$ <i>500</i>	0/15
LHD-2xDefa	<b>2.9</b> (0.7)	<b>2.9</b> (0.6)	<b>2.9</b> (0.7)	6.2(5)	$\infty$ <i>500</i>	0/15
RAND-2xDef	<b>1.8</b> (2)	<b>2.2</b> (0.5)	<b>2.9</b> (2)	4.9(3)	$\infty$ <i>500</i>	0/15
RF1-CMAES	<b>2.6</b> (1)	3.0(2)	5.4(2)	4.4(2)	$\infty$ <i>2502</i>	0/15
RF5-CMAES	<b>2.4</b> (2)	<b>2.5</b> (2)	21(32)	35(65)	$\infty$ <i>2514</i>	0/15
Sifeg	<b>1.9</b> (1)	<b>1.9</b> (0.2)	<b>2.0</b> (0.6)	<b>0.72</b> (0.4)	<b>1.4</b> (2)	15/15
Sif	<b>1.9</b> (0.7)	<b>1.9</b> (0.1)	<b>1.9</b> (0.7)	<b>0.76</b> (0.4)	<b>0.87</b> (1)	15/15
Srr	<b>1.9</b> (0.7)	<b>1.9</b> (0.2)	<b>1.9</b> (0.4)	<b>0.76</b> (0.2)	<b>1.9</b> (3)	14/15

Table 94: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f21</b>	<i>4.0e+1:30</i>	<i>2.5e+1:46</i>	<i>1.6e+1:56</i>	<i>1.0e+1:130</i>	<i>6.3e+0:639</i>	15/15
BSifeg	<b>2.3</b> (0.5)	263(547)	374(0.5)	171(317)	116(123)	10/15
BSif	5.7(0.7)	354(54)	520(656)	331(768)	226(279)	7/15
BSqi	<b>2.5</b> (8)	217(557)	333(33)	151(29)	92(121)	11/15
BSrr	4.1(0.7)	222(762)	338(25)	159(282)	95(147)	11/15
CMA-CSA	4.7(3)	7.6(16)	11(25)	7.7(11)	5.0(10)	15/15
CMA-MSR	3.5(2)	3.7(3)	15(30)	10(13)	8.4(3)	15/15
CMA-TPA	3.3(1)	3.0(0.8)	8.4(12)	4.8(5)	<b>1.4</b> (2)	15/15
GP1-CMAES	<b>2.1</b> (1)	<b>2.1</b> (0.9)	<b>2.0</b> (0.6)	<b>2.4</b> (10)	<b>1.2</b> (3)	12/15
GP5-CMAES	<b>1.8</b> (0.5)	<b>2.6</b> (4)	7.1(8)	3.7(13)	<b>1.3</b> (2)	13/15
IPOPCMAv3p	3.5(3)	8.1(15)	17(37)	10(10)	3.2(5)	9/15
LHD-10xDef	6.5(3)	4.7(0.2)	4.6(0.3)	<b>2.7</b> (2)	<b>1.0</b> (2)	9/15
LHD-2xDefa	<b>2.1</b> (2)	<b>1.8</b> (0.3)	<b>2.1</b> (0.8)	<b>1.3</b> (1)	<b>0.52</b> (0.2)	11/15
RAND-2xDef	<b>2.0</b> (0.3)	<b>1.7</b> (0.4)	<b>2.2</b> (0.3)	<b>1.2</b> (0.2)	<b>0.39</b> (0.3)	12/15
RF1-CMAES	9.1(2)	7.5(15)	11(2)	9.1(11)	4.0(9)	8/15
RF5-CMAES	<b>2.9</b> (2)	6.2(0.8)	6.9(12)	13(20)	12(14)	4/15
Sifeg	<b>1.6</b> (0.9)	216(1297)	177(612)	79(385)	88(100)	11/15
Sif	<b>1.6</b> (0.6)	256(1092)	210(284)	110(384)	109(150)	10/15
Srr	<b>1.6</b> (0.7)	197(0.8)	162(4)	78(78)	65(59)	12/15

Table 95: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f22</i></b>	<i>6.3e+1:18</i>	<i>4.0e+1:30</i>	<i>4.0e+1:30</i>	<i>6.3e+0:155</i>	<i>4.0e+0:631</i>	14/15
BSifeg	404(1)	737(829)	737(1656)	530(487)	135(475)	9/15
BSif	404(1405)	1042(2485)	1042(2927)	813(798)	251(673)	6/15
BSqi	404(2810)	713(1339)	713(828)	434(647)	109(119)	10/15
BSrr	404(0.8)	802(3787)	802(1302)	469(416)	116(116)	10/15
CMA-CSA	3.3(4)	3.9(1)	3.9(1)	303(900)	183(249)	13/15
CMA-MSR	5.1(3)	11(25)	11(2)	428(2713)	349(1667)	12/15
CMA-TPA	4.7(3)	4.1(3)	4.1(3)	604(1968)	148(2)	13/15
GP1-CMAES	<b>3.2</b> (2)	<b>3.1</b> (2)	<b>3.1</b> (0.7)	<b>3.9</b> (13)	<b>1.3</b> (2)	12/15
GP5-CMAES	<b>2.9</b> (1)	4.0(1)	4.0(12)	12(14)	3.4(8)	9/15
IPOPCMAv3p	4.5(3)	4.7(2)	4.7(5)	17(21)	5.6(3)	7/15
LHD-10xDef	6.2(6)	7.7(0.1)	7.7(0.3)	5.7(4)	<b>1.4</b> (2)	7/15
LHD-2xDefa	3.4(1.0)	<b>3.1</b> (2)	<b>3.1</b> (2)	<b>4.4</b> (6)	<b>1.3</b> (1)	7/15
RAND-2xDef	3.4(2)	<b>2.8</b> (2)	<b>2.8</b> (0.7)	<b>4.6</b> (3)	<b>1.4</b> (4)	7/15
RF1-CMAES	<b>3.2</b> (3)	10(23)	10(65)	16(24)	8.3(8)	5/15
RF5-CMAES	3.9(3)	4.4(2)	4.4(2)	36(52)	9.0(12)	5/15
Sifeg	8.0(22)	442(1261)	442(699)	280(380)	83(125)	11/15
Sif	404(0.5)	772(1364)	772(1968)	611(835)	151(88)	8/15
Srr	404(1406)	672(1655)	672(1655)	389(317)	109(195)	10/15



Table 96: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>6.3e+0:10</i>	<i>4.0e+0:62</i>	<i>2.5e+0:162</i>	<i>2.5e+0:162</i>	<i>1.0e+0:915</i>	15/15
BSifeg	<b>2.9</b> (4)	<b>1.5</b> (0.7)	<b>1.7</b> (2)	<b>1.7</b> (2)	13(11)	15/15
BSif	<b>2.9</b> (2)	<b>1.2</b> (0.9)	<b>1.6</b> (2)	<b>1.6</b> (2)	12(24)	15/15
BSqi	<b>2.9</b> (4)	<b>1.2</b> (0.5)	<b>1.1</b> (2)	<b>1.1</b> (1)	13(10)	15/15
BSrr	<b>2.9</b> (4)	<b>1.2</b> (1)	<b>1.5</b> (2)	<b>1.5</b> (2)	11(16)	15/15
CMA-CSA	6.3(5)	6.0(6)	18(14)	18(14)	23(16)	15/15
CMA-MSR	4.8(3)	3.2(3)	<b>2.8</b> (2)	<b>2.8</b> (0.8)	<b>2.9</b> (4)	15/15
CMA-TPA	3.4(4)	3.9(2)	16(23)	16(19)	12(5)	15/15
GP1-CMAES	<b>2.0</b> (3)	<b>1.7</b> (1)	5.3(4)	5.3(4)	<b>2.7</b> (2)	10/15
GP5-CMAES	3.6(4)	<b>1.7</b> (2)	<b>1.6</b> (0.3)	<b>1.6</b> (4)	<b>0.92</b> (0.4)	13/15
IPOPCMAv3p	<b>2.3</b> (0.8)	<b>2.8</b> (2)	4.4(3)	4.4(2)	$\infty$ 2514	0/15
LHD-10xDef	<b>2.1</b> (2)	<b>2.3</b> (2)	5.9(4)	5.9(2)	$\infty$ 500	0/15
LHD-2xDefa	<b>2.0</b> (1)	<b>1.6</b> (2)	8.3(11)	8.3(17)	$\infty$ 500	0/15
RAND-2xDef	<b>2.0</b> (2)	3.8(9)	10(13)	10(5)	$\infty$ 500	0/15
RF1-CMAES	<b>1.7</b> (1)	3.5(4)	7.1(5)	7.1(10)	$\infty$ 2506	0/15
RF5-CMAES	<b>1.6</b> (3)	3.1(3)	10(8)	10(7)	$\infty$ 2548	0/15
Sifeg	<b>2.5</b> (3)	<b>1.9</b> (2)	3.5(3)	3.5(4)	4.6(9)	15/15
Sif	<b>2.5</b> (3)	<b>1.9</b> (2)	3.7(4)	3.7(4)	6.4(11)	15/15
Srr	<b>2.5</b> (3)	<b>1.9</b> (2)	3.7(2)	3.7(2)	5.7(4)	15/15

Table 97: 10-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f</i>24</b>	<i>1.0e+2:66</i>	<i>6.3e+1:596</i>	<i>4.0e+1:3181</i>	<i>2.5e+1:7668</i>	<i>1.6e+1:14353</i>	15/15
BSifeg	22(16)	50(73)	34(31)	87(130)	$\infty$ <i>9e4</i>	0/15
BSif	37(13)	37(13)	72(62)	$\infty$	$\infty$ <i>9e4</i>	0/15
BSqi	18(10)	71(104)	55(63)	174(352)	$\infty$ <i>9e4</i>	0/15
BSrr	19(18)	39(56)	41(40)	162(215)	$\infty$ <i>8e4</i>	0/15
CMA-CSA	<b>2.6</b> (0.9)	<b>1.1</b> (1)	<b>1.2</b> (1)	<b>0.62</b> (0.5)	<b>1.2</b> (0.9)	15/15
CMA-MSR	<b>2.6</b> (1)	<b>0.84</b> (0.3)	<b>0.45</b> (0.6)	<b>0.50</b> (0.4)	<b>0.83</b> (0.6)	15/15
CMA-TPA	<b>2.6</b> (1)	<b>1.0</b> (0.5)	<b>0.67</b> (0.2)	<b>0.70</b> (0.8)	<b>0.94</b> (0.6)	15/15
GP1-CMAES	<b>1.7</b> (0.8)	<b>0.90</b> (0.5)	<b>2.6</b> (3)	<b>1.1</b> (0.9)	$\infty$ <i>2514</i>	0/15
GP5-CMAES	<b>1.2</b> (0.3)	<b>0.81</b> (0.9)	$\infty$	$\infty$	$\infty$ <i>2528</i>	0/15
IPOPCMAv3p	<b>2.7</b> (1)	<b>1.4</b> (0.9)	<b>2.7</b> (1)	4.8(4)	$\infty$ <i>2504</i>	0/15
LHD-10xDef	4.8(1)	<b>2.9</b> (3)	<b>2.4</b> (2)	$\infty$	$\infty$ <i>500</i>	0/15
LHD-2xDefa	8.3(8)	$\infty$	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
RAND-2xDef	4.8(2)	$\infty$	$\infty$	$\infty$	$\infty$ <i>500</i>	0/15
RF1-CMAES	<b>2.2</b> (0.9)	<b>1.1</b> (0.9)	<b>1.2</b> (2)	<b>2.3</b> (2)	$\infty$ <i>2502</i>	0/15
RF5-CMAES	<b>2.4</b> (1)	3.4(3)	$\infty$	$\infty$	$\infty$ <i>2514</i>	0/15
Sifeg	3.0(3)	5.9(13)	9.0(7)	26(33)	$\infty$ <i>9e4</i>	0/15
Sif	3.0(2)	10(16)	13(19)	35(33)	44(21)	2/15
Srr	<b>2.8</b> (2)	<b>1.5</b> (2)	8.8(5)	22(27)	46(55)	2/15

Table 98: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>6.3e+1:24</i>	<i>4.0e+1:42</i>	<i>1.0e-8:43</i>	<i>1.0e-8:43</i>	<i>1.0e-8:43</i>	15/15
BSifeg	<b>2.2</b> (1.0)	<b>1.7</b> (0.1)	<b>2.5</b> (0.2)	<b>2.5</b> (0.2)	<b>2.5</b> (0.3)	15/15
BSif	<b>2.2</b> (0.9)	<b>1.7</b> (0.1)	<b>2.5</b> (0.3)	<b>2.5</b> (0.2)	<b>2.5</b> (0.3)	15/15
BSqi	<b>2.2</b> (0.9)	<b>1.7</b> (0.1)	<b>2.5</b> (0.2)	<b>2.5</b> (0.3)	<b>2.5</b> (0.2)	15/15
BSrr	<b>2.2</b> (0.4)	<b>1.7</b> (0.1)	<b>2.5</b> (0.2)	<b>2.5</b> (0.2)	<b>2.5</b> (0.2)	15/15
CMA-CSA	4.7(2)	4.4(1)	64(4)	64(3)	64(5)	15/15
CMA-MSR	6.0(2)	5.1(2)	75(4)	75(3)	75(3)	15/15
CMA-TPA	5.4(2)	4.0(0.9)	46(3)	46(4)	46(1)	15/15
GP1-CMAES	3.9(2)	3.1(0.6)	58(6)	58(10)	58(7)	15/15
GP5-CMAES	<b>2.9</b> (0.9)	<b>2.0</b> (0.2)	$\infty$	$\infty$	$\infty$ <i>5034</i>	0/15
IPOPCMAv3p	4.8(2)	4.6(1)	64(2)	64(2)	64(2)	15/15
LHD-10xDef	17(0.1)	10(0.1)	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	3.9(0.2)	<b>2.5</b> (0.2)	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
RAND-2xDef	4.0(0.5)	<b>2.8</b> (0.4)	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
RF1-CMAES	3.9(1)	3.5(0.8)	73(20)	73(18)	73(18)	15/15
RF5-CMAES	3.7(2)	3.0(0.9)	$\infty$	$\infty$	$\infty$ <i>5006</i>	0/15
Sifeg	<b>2.2</b> (0.6)	<b>1.7</b> (0.2)	16(0.9)	16(0.9)	16(1)	15/15
Sif	<b>2.2</b> (0.7)	<b>1.7</b> (0.1)	16(1)	16(1)	16(2)	15/15
Srr	<b>2.2</b> (0.8)	<b>1.7</b> (0.1)	16(1)	16(1)	16(0.7)	15/15

Table 99: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>4.0e+6</i> :29	<i>2.5e+6</i> :42	<i>1.0e+5</i> :65	<i>1.0e+4</i> :207	<i>1.0e-8</i> :412	15/15
BSifeg	<b>2.3</b> (1.0)	<b>1.8</b> (0.2)	<b>1.5</b> (0.2)	<b>0.54</b> (0.1)	<b>1.2</b> (0.1)	15/15
BSif	<b>2.3</b> (1.0)	<b>1.8</b> (0.2)	<b>1.5</b> (0.0)	<b>0.55</b> (0.1)	<b>1.2</b> (0.1)	15/15
BSqi	<b>2.3</b> (0.0)	<b>1.8</b> (0.2)	<b>1.5</b> (0.1)	<b>0.53</b> (0.1)	<b>1.3</b> (0.2)	15/15
BSrr	<b>2.3</b> (1)	<b>1.8</b> (0.3)	<b>1.5</b> (0.1)	<b>0.54</b> (0.1)	<b>1.3</b> (0.2)	15/15
CMA-CSA	<b>1.2</b> (0.6)	<b>1.1</b> (0.8)	14(3)	11(3)	33(1)	15/15
CMA-MSR	<b>1.0</b> (0.4)	<b>1.6</b> (2)	11(5)	7.9(3)	38(3)	15/15
CMA-TPA	<b>1.4</b> (1)	<b>1.5</b> (0.7)	11(4)	9.5(3)	36(2)	15/15
GP1-CMAES	<b>1.5</b> (0.9)	<b>1.6</b> (1)	8.9(5)	8.0(3)	$\infty$ 5006	0/15
GP5-CMAES	<b>0.90</b> (0.9)	<b>1.3</b> (1)	5.4(2)	3.9(0.8)	$\infty$ 5006	0/15
IPOPCMAv3p	<b>0.93</b> (0.6)	<b>1.4</b> (1)	14(4)	11(2)	$\infty$ 5006	0/15
LHD-10xDef	<b>1.6</b> (1)	4.1(4)	30(19)	$\infty$	$\infty$ 1000	0/15
LHD-2xDefa	<b>1.1</b> (0.8)	<b>1.9</b> (0.8)	8.5(5)	72(67)	$\infty$ 1000	0/15
RAND-2xDef	<b>1.3</b> (2)	<b>1.6</b> (2)	7.8(4)	70(116)	$\infty$ 1000	0/15
RF1-CMAES	<b>1.1</b> (0.8)	<b>1.2</b> (1)	11(3)	29(27)	$\infty$ 5006	0/15
RF5-CMAES	<b>1.2</b> (1)	<b>1.3</b> (0.9)	184(149)	$\infty$	$\infty$ 5006	0/15
Sifeg	<b>2.3</b> (0.9)	<b>1.9</b> (0.3)	<b>1.9</b> (0.2)	<b>0.77</b> (0.1)	<b>2.2</b> (0.2)	15/15
Sif	<b>2.3</b> (0.5)	<b>1.9</b> (0.5)	<b>1.9</b> (0.2)	<b>0.82</b> (0.2)	<b>2.2</b> (0.3)	15/15
Srr	<b>2.3</b> (1)	<b>1.9</b> (0.5)	<b>1.9</b> (0.3)	<b>0.76</b> (0.1)	<b>2.2</b> (0.3)	15/15

Table 100: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>6.3e+2:33</i>	<i>4.0e+2:44</i>	<i>1.6e+2:109</i>	<i>1.0e+2:255</i>	<i>2.5e+1:3277</i>	15/15
BSifeg	<b>1.7</b> (0.2)	<b>1.6</b> (0.2)	<b>0.92</b> (0.1)	<b>0.52</b> (0.0)	<b>0.12</b> (0.0)	15/15
BSif	<b>1.7</b> (0.2)	<b>1.6</b> (0.2)	<b>0.92</b> (0.0)	<b>0.52</b> (0.0)	<b>0.12</b> (0.0)	15/15
BSqi	<b>1.7</b> (0.2)	<b>1.6</b> (0.2)	<b>0.92</b> (0.1)	<b>0.52</b> (0.1)	<b>0.11</b> (0.0)	15/15
BSrr	<b>1.7</b> (0.2)	<b>1.6</b> (0.1)	<b>0.92</b> (0.1)	<b>0.52</b> (0.1)	<b>0.11</b> (0.0)	15/15
CMA-CSA	<b>1.9</b> (2)	4.0(0.5)	7.4(2)	7.0(3)	3.5(1.0)	15/15
CMA-MSR	<b>2.9</b> (2)	4.5(0.8)	5.2(1.0)	<b>3.0</b> (0.3)	3.5(1)	15/15
CMA-TPA	3.1(1)	4.0(1.0)	6.0(4)	4.4(1)	<b>2.5</b> (1)	15/15
GP1-CMAES	<b>2.3</b> (1)	3.2(1.0)	5.9(1)	4.2(2)	22(34)	1/15
GP5-CMAES	<b>1.9</b> (0.9)	<b>2.9</b> (1)	15(23)	43(50)	$\infty$ 5034	0/15
IPOPCMAv3p	<b>1.9</b> (1)	3.6(2)	7.6(4)	7.0(2)	22(30)	1/15
LHD-10xDef	9.1(4)	10(0.3)	8.7(0.7)	9.0(6)	$\infty$ 1000	0/15
LHD-2xDefa	<b>2.5</b> (0.5)	3.0(0.5)	8.6(7)	18(40)	$\infty$ 1000	0/15
RAND-2xDef	<b>2.7</b> (0.3)	<b>2.8</b> (0.4)	5.7(5)	10(24)	$\infty$ 1000	0/15
RF1-CMAES	<b>2.0</b> (1)	3.7(0.9)	6.4(2)	4.0(0.8)	22(41)	1/15
RF5-CMAES	<b>1.7</b> (0.8)	<b>2.6</b> (0.5)	18(17)	82(128)	$\infty$ 5006	0/15
Sifeg	<b>1.7</b> (0.2)	<b>1.6</b> (0.1)	<b>0.97</b> (0.1)	<b>0.54</b> (0.1)	<b>0.14</b> (0.0)	15/15
Sif	<b>1.7</b> (0.4)	<b>1.6</b> (0.2)	<b>0.97</b> (0.1)	<b>0.55</b> (0.1)	<b>0.15</b> (0.0)	15/15
Srr	<b>1.7</b> (0.2)	<b>1.6</b> (0.2)	<b>0.97</b> (0.2)	<b>0.54</b> (0.1)	<b>0.13</b> (0.0)	15/15

Table 101: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>6.3e+2:22</i>	<i>4.0e+2:91</i>	<i>2.5e+2:250</i>	<i>1.6e+2:332</i>	<i>6.3e+1:1927</i>	15/15
BSifeg	<b>2.8</b> (1)	<b>0.98</b> (0.1)	<b>0.58</b> (0.3)	<b>0.66</b> (0.3)	<b>0.20</b> (0.0)	15/15
BSif	<b>2.8</b> (0.9)	<b>0.98</b> (0.1)	<b>0.59</b> (0.3)	<b>0.68</b> (0.4)	<b>0.21</b> (0.0)	15/15
BSqi	<b>2.8</b> (1)	<b>0.98</b> (0.2)	<b>0.62</b> (0.5)	<b>0.70</b> (0.3)	<b>0.24</b> (0.0)	15/15
BSrr	<b>2.8</b> (0.5)	<b>0.98</b> (0.2)	<b>0.60</b> (0.3)	<b>0.69</b> (0.3)	<b>0.21</b> (0.0)	15/15
CMA-CSA	7.1(3)	3.1(0.4)	<b>2.1</b> (0.4)	3.7(1)	<b>2.2</b> (1)	15/15
CMA-MSR	8.5(3)	3.3(0.8)	<b>2.0</b> (0.8)	3.6(5)	5.4(6)	15/15
CMA-TPA	8.2(2)	<b>2.9</b> (0.8)	<b>1.9</b> (0.5)	<b>2.9</b> (0.6)	3.5(2)	15/15
GP1-CMAES	9.2(8)	4.5(2)	11(4)	42(88)	39(22)	1/15
GP5-CMAES	7.5(2)	5.5(9)	13(45)	215(159)	$\infty$ <i>5022</i>	0/15
IPOPCMAv3p	7.4(3)	3.3(1)	<b>2.3</b> (0.6)	4.1(1)	<b>2.4</b> (2)	10/15
LHD-10xDef	22(10)	18(12)	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	9.1(3)	6.8(1)	58(71)	$\infty$	$\infty$ <i>1000</i>	0/15
RAND-2xDef	10(8)	8.4(8)	13(11)	$\infty$	$\infty$ <i>1000</i>	0/15
RF1-CMAES	8.1(2)	3.4(1)	<b>2.5</b> (0.6)	7.7(13)	$\infty$ <i>5006</i>	0/15
RF5-CMAES	8.9(3)	13(2)	57(110)	$\infty$	$\infty$ <i>5006</i>	0/15
Sifeg	<b>2.8</b> (0.8)	<b>1.1</b> (0.3)	<b>0.56</b> (0.2)	<b>0.60</b> (0.1)	<b>0.17</b> (0.0)	15/15
Sif	<b>2.8</b> (1)	<b>1.1</b> (0.2)	<b>0.58</b> (0.1)	<b>0.61</b> (0.1)	<b>0.17</b> (0.0)	15/15
Srr	<b>2.8</b> (1)	<b>1.1</b> (0.2)	<b>0.56</b> (0.1)	<b>0.59</b> (0.1)	<b>0.16</b> (9e-3)	15/15

Table 102: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f5</i></b>	<i>2.5e+2:19</i>	<i>1.6e+2:34</i>	<i>1.0e-8:41</i>	<i>1.0e-8:41</i>	<i>1.0e-8:41</i>	15/15
BSifeg	<b>2.1</b> (0.3)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSif	<b>2.1</b> (0.3)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSqi	<b>2.1</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
BSrr	<b>2.1</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
CMA-CSA	<b>1.5</b> (0.7)	<b>1.8</b> (0.5)	6.0(0.8)	6.0(1)	6.0(1)	15/15
CMA-MSR	<b>1.9</b> (0.6)	<b>1.9</b> (0.7)	5.6(1)	5.6(1)	5.6(1)	15/15
CMA-TPA	<b>1.3</b> (1)	<b>1.4</b> (0.4)	4.9(2)	4.9(1)	4.9(1)	15/15
GP1-CMAES	<b>1.6</b> (0.8)	<b>1.9</b> (0.5)	92(115)	92(62)	92(85)	11/15
GP5-CMAES	<b>1.7</b> (0.9)	<b>1.7</b> (0.4)	4.8(0.7)	4.8(2)	4.8(1)	15/15
IPOPCMAv3p	<b>2.0</b> (2)	<b>2.0</b> (0.9)	36(13)	36(15)	36(19)	15/15
LHD-10xDef	8.1(9)	12(0.0)	11(0.4)	11(0.2)	11(0.3)	15/15
LHD-2xDefa	3.7(2)	<b>2.5</b> (0.0)	<b>3.0</b> (0.1)	<b>3.0</b> (0.2)	<b>3.0</b> (0.2)	15/15
RAND-2xDef	3.4(2)	<b>2.6</b> (0.1)	3.4(2)	3.4(3)	3.4(3)	15/15
RF1-CMAES	<b>1.8</b> (1)	<b>2.3</b> (0.8)	50(22)	50(26)	50(24)	15/15
RF5-CMAES	<b>2.0</b> (0.9)	<b>2.0</b> (0.6)	265(451)	265(361)	265(330)	6/15
Sifeg	<b>2.1</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
Sif	<b>2.1</b> (0.3)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15
Srr	<b>2.1</b> (0.2)	<b>1.5</b> (0.1)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	<b>1.5</b> (0.0)	15/15

Table 103: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>2.5e+5:16</i>	<i>6.3e+4:43</i>	<i>1.6e+4:62</i>	<i>1.6e+2:353</i>	<i>1.6e+1:1078</i>	15/15
BSifeg	<b>2.3</b> (1)	<b>1.3</b> (0.8)	<b>1.2</b> (0.4)	39(42)	713(1132)	3/15
BSif	<b>2.3</b> (2)	<b>1.3</b> (0.3)	<b>1.2</b> (0.5)	159(199)	2558(3325)	1/15
BSqi	<b>1.9</b> (2)	<b>1.1</b> (0.7)	<b>1.1</b> (0.3)	34(59)	419(453)	2/7
BSrr	<b>2.3</b> (1)	<b>1.3</b> (0.7)	<b>1.2</b> (0.4)	36(47)	210(81)	8/15
CMA-CSA	3.6(2)	<b>2.5</b> (1)	<b>2.4</b> (1)	<b>2.8</b> (0.8)	<b>1.8</b> (0.3)	15/15
CMA-MSR	3.6(2)	<b>2.4</b> (0.6)	<b>2.4</b> (0.9)	<b>1.9</b> (0.8)	<b>1.5</b> (0.6)	15/15
CMA-TPA	3.1(2)	<b>2.2</b> (2)	<b>2.0</b> (0.7)	<b>2.3</b> (0.7)	<b>1.6</b> (0.5)	15/15
GP1-CMAES	<b>2.8</b> (2)	<b>2.0</b> (0.9)	<b>2.0</b> (0.8)	<b>1.7</b> (1)	4.2(4)	11/15
GP5-CMAES	<b>2.6</b> (2)	<b>1.6</b> (0.5)	<b>1.5</b> (0.4)	19(24)	$\infty$ <i>5024</i>	0/15
IPOPCMAv3p	<b>2.9</b> (2)	<b>2.3</b> (1)	<b>2.3</b> (2)	<b>2.0</b> (0.5)	<b>1.5</b> (0.2)	15/15
LHD-10xDef	17(12)	10(1)	7.1(0.2)	4.3(4)	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	4.6(2)	<b>2.3</b> (0.3)	<b>1.9</b> (0.4)	6.8(6)	$\infty$ <i>1000</i>	0/15
RAND-2xDef	4.8(0.2)	<b>2.3</b> (0.3)	<b>1.8</b> (0.5)	5.7(9)	$\infty$ <i>1000</i>	0/15
RF1-CMAES	<b>2.7</b> (2)	<b>2.1</b> (0.7)	<b>2.3</b> (1)	<b>2.9</b> (1)	66(118)	1/15
RF5-CMAES	<b>2.1</b> (2)	<b>1.6</b> (0.6)	<b>1.8</b> (0.4)	32(28)	$\infty$ <i>5006</i>	0/15
Sifeg	<b>2.3</b> (2)	<b>1.2</b> (0.5)	<b>1.2</b> (0.4)	7.4(9)	151(146)	10/15
Sif	<b>2.3</b> (2)	<b>1.2</b> (0.7)	<b>1.2</b> (0.5)	37(71)	294(301)	7/15
Srr	<b>2.3</b> (2)	<b>1.2</b> (0.7)	<b>1.2</b> (0.3)	10(5)	94(67)	12/15



Table 104: 20-D, running time excess  $ERT/ERT_{\text{best}} 2009$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best}} 2009$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f7</i></b>	<i>1.0e+3:11</i>	<i>4.0e+2:39</i>	<i>2.5e+2:74</i>	<i>6.3e+1:319</i>	<i>1.0e+1:1351</i>	15/15
BSifeg	<b>1.4</b> (0.7)	<b>1.5</b> (0.5)	<b>1.0</b> (0.5)	187(162)	$\infty$ 2e5	0/15
BSif	<b>1.4</b> (2)	<b>1.5</b> (0.5)	7.0(0.4)	258(349)	$\infty$ 2e5	0/15
BSqi	<b>1.4</b> (2)	<b>1.5</b> (0.5)	<b>1.0</b> (0.4)	288(335)	$\infty$ 2e5	0/15
BSrr	<b>1.4</b> (1)	<b>1.5</b> (0.6)	<b>1.0</b> (0.5)	174(69)	$\infty$ 2e5	0/15
CMA-CSA	<b>2.7</b> (2)	3.5(2)	3.1(1)	<b>1.7</b> (0.4)	<b>1.7</b> (2)	15/15
CMA-MSR	3.5(2)	3.1(0.6)	<b>2.7</b> (1.0)	<b>1.4</b> (0.4)	<b>2.1</b> (1)	15/15
CMA-TPA	3.2(3)	3.7(1)	<b>2.6</b> (0.7)	<b>1.3</b> (0.3)	<b>2.1</b> (1)	15/15
GP1-CMAES	<b>2.1</b> (2)	<b>2.2</b> (1)	<b>1.7</b> (0.7)	<b>0.92</b> (0.4)	3.0(3)	10/15
GP5-CMAES	<b>2.4</b> (2)	<b>1.8</b> (0.6)	<b>1.3</b> (0.1)	<b>0.58</b> (0.0)*	<b>1.6</b> (0.8)	14/15
IPOPCMAv3p	<b>1.3</b> (1)	<b>2.2</b> (2)	<b>2.5</b> (0.8)	<b>1.6</b> (0.2)	<b>1.3</b> (0.7)	15/15
LHD-10xDef	<b>2.4</b> (2)	10(3)	5.7(0.8)	8.1(13)	$\infty$ 1000	0/15
LHD-2xDefa	<b>1.5</b> (1)	<b>2.6</b> (0.3)	<b>1.9</b> (0.5)	8.1(4)	$\infty$ 1000	0/15
RAND-2xDef	<b>2.2</b> (3)	<b>2.8</b> (2)	<b>2.1</b> (0.7)	6.4(6)	$\infty$ 1000	0/15
RF1-CMAES	<b>2.0</b> (1)	<b>2.6</b> (2)	<b>2.3</b> (0.9)	<b>1.5</b> (0.7)	54(73)	1/15
RF5-CMAES	<b>1.8</b> (2)	<b>1.9</b> (0.9)	<b>1.8</b> (0.4)	7.0(7)	$\infty$ 5034	0/15
Sifeg	<b>1.4</b> (2)	<b>1.5</b> (0.6)	<b>3.0</b> (0.4)	48(6)	$\infty$ 2e5	0/15
Sif	<b>1.4</b> (1)	<b>1.5</b> (0.5)	<b>1.1</b> (0.4)	<b>1.1</b> (0.4)	<b>1.02924</b>	15/15

0 81007.11 1 55100.4 44 401.1

(7.0)07.1

1.1 0 40050.1

(5)47

1.104 44 4.981322511.5648 0 1.02924 0/15 1.14686 . 0.901807 7 1.1466

Table 105: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>4.0e+4:19</i>	<i>2.5e+4:35</i>	<i>4.0e+3:67</i>	<i>2.5e+2:231</i>	<i>1.6e+1:1470</i>	15/15
BSifeg	<b>3.3</b> (0.4)	<b>2.0</b> (0.3)	<b>1.2</b> (0.1)	4.2(6)	65(107)	12/15
BSif	<b>3.3</b> (0.7)	<b>2.0</b> (0.4)	<b>1.2</b> (0.1)	4.9(14)	518(422)	3/15
BSqi	<b>3.1</b> (0.5)	<b>1.9</b> (0.4)	<b>1.2</b> (0.1)	<b>1.6</b> (2)	32(16)	7/8
BSrr	<b>3.3</b> (1)	<b>2.0</b> (0.3)	<b>1.2</b> (0.1)	3.7(0.2)	75(77)	10/15
CMA-CSA	7.3(5)	5.8(2)	4.9(1)	<b>2.9</b> (0.5)	<b>2.4</b> (0.7)	15/15
CMA-MSR	8.7(3)	5.9(1)	5.0(1.0)	<b>2.9</b> (0.7)	<b>2.5</b> (0.9)	15/15
CMA-TPA	7.2(2)	4.3(1)	3.8(0.8)	<b>2.2</b> (0.5)	<b>1.9</b> (0.5)	15/15
GP1-CMAES	5.5(2)	3.4(0.7)	3.1(0.8)	<b>2.3</b> (0.3)	3.0(2)	12/15
GP5-CMAES	4.4(0.6)	<b>2.6</b> (0.2)	<b>2.2</b> (0.4)	11(22)	8.2(9)	5/15
IPOPCMAv3p	6.3(3)	4.8(1.0)	4.4(0.3)	<b>2.8</b> (1.0)	<b>2.9</b> (2)	12/15
LHD-10xDef	23(0.2)	12(0.1)	6.7(0.4)	3.8(2)	$\infty$ 1000	0/15
LHD-2xDefa	5.5(0.7)	3.2(0.6)	3.1(0.7)	<b>2.8</b> (0.7)	$\infty$ 1000	0/15
RAND-2xDef	5.4(0.5)	3.2(0.4)	<b>2.8</b> (0.4)	<b>2.5</b> (0.7)	$\infty$ 1000	0/15
RF1-CMAES	5.8(1)	4.0(0.6)	4.0(1)	<b>2.7</b> (0.8)	25(19)	2/15
RF5-CMAES	5.8(2)	3.7(2)	4.2(2)	96(108)	$\infty$ 5006	0/15
Sifeg	3.3(1)	<b>2.0</b> (0.3)	<b>1.2</b> (0.1)	<b>0.98</b> (0.6)	49(53)	14/15
Sif	3.3(0.6)	<b>2.0</b> (0.1)	<b>1.2</b> (0.1)	<b>1.1</b> (0.8)	75(113)	12/15
Srr	3.3(0.7)	<b>2.0</b> (0.2)	<b>1.2</b> (0.1)	<b>0.95</b> (0.2)	77(55)	10/15

Table 106: 20-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f9</b>	<i>1.0e+2:357</i>	<i>6.3e+1:560</i>	<i>4.0e+1:684</i>	<i>2.5e+1:756</i>	<i>1.0e+1:1716</i>	15/15
BSifeg	19(39)	66(100)	59(81)	57(78)	$\infty$ 2e5	0/15
BSif	73(20)	115(91)	147(295)	181(258)	$\infty$ 2e5	0/15
BSqi	7.4(3)	26(26)	25(45)	27(24)	$\infty$ 2e5	0/5
BSrr	16(11)	65(100)	57(4)	55(107)	$\infty$ 2e5	0/15
CMA-CSA	<b>2.2</b> (1)	<b>2.0</b> (4)	<b>1.8</b> (2)	<b>1.9</b> (0.1)	<b>3.8</b> (0.6)	15/15
CMA-MSR	<b>2.0</b> (0.2)	<b>2.4</b> (1)	<b>2.1</b> (4)	<b>2.1</b> (1)	<b>3.8</b> (0.9)	15/15
CMA-TPA	<b>1.5</b> (0.3)	<b>1.0</b> (0.3)	<b>0.97</b> (0.2)	<b>1.0</b> (0.4)	<b>3.8</b> (0.7)	15/15
GP1-CMAES	<b>2.1</b> (0.8)	<b>1.6</b> (0.5)	<b>1.4</b> (0.4)	<b>1.5</b> (0.4)	$\infty$ 5006	0/15
GP5-CMAES	12(7)	12(14)	13(9)	12(24)	$\infty$ 5020	0/15
IPOPCMAv3p	3.6(4)	3.6(0.9)	3.1(5)	<b>3.0</b> (3)	$\infty$ 5006	0/15
LHD-10xDef	8.0(4)	27(35)	$\infty$	$\infty$	$\infty$ 1000	0/15
LHD-2xDefa	5.3(6)	13(8)	22(21)	$\infty$	$\infty$ 1000	0/15
RAND-2xDef	5.3(6)	13(23)	22(24)	$\infty$	$\infty$ 1000	0/15
RF1-CMAES	3.8(1)	5.8(8)	5.3(4)	5.8(4)	$\infty$ 5006	0/15
RF5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ 5006	0/15
Sifeg	3.4(5)	19(28)	16(45)	15(6)	$\infty$ 2e5	0/15
Sif	16(6)	29(76)	26(29)	25(45)	$\infty$ 2e5	0/15
Srr	<b>1.9</b> (3)	16(3)	14(27)	13(19)	$\infty$ 2e5	0/15

Table 107: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>1.6e+6:15</i>	<i>1.0e+6:27</i>	<i>4.0e+5:70</i>	<i>6.3e+4:231</i>	<i>4.0e+3:1015</i>	15/15
BSifeg	<b>2.4</b> (2)	<b>2.0</b> (0.9)	<b>1.6</b> (1)	479(636)	$\infty$ 2e5	0/15
BSif	<b>2.4</b> (2)	<b>2.0</b> (1)	<b>1.6</b> (0.4)	494(497)	$\infty$ 2e5	0/15
BSqi	<b>2.4</b> (2)	<b>2.0</b> (1)	<b>1.5</b> (0.6)	221(501)	$\infty$ 2e5	0/15
BSrr	<b>2.4</b> (2)	<b>2.0</b> (1)	<b>1.5</b> (0.6)	204(583)	$\infty$ 9e4	0/15
CMA-CSA	7.8(4)	8.3(8)	7.5(4)	5.8(1)	<b>3.0</b> (0.5)	15/15
CMA-MSR	8.1(4)	5.8(3)	4.0(2)	<b>3.4</b> (1)	<b>2.7</b> (0.7)	15/15
CMA-TPA	7.5(6)	6.5(2)	4.7(1)	<b>3.3</b> (1)	<b>2.6</b> (0.6)	15/15
GP1-CMAES	5.4(4)	5.4(3)	4.2(0.8)	3.5(0.7)	<b>2.3</b> (0.9)	15/15
GP5-CMAES	4.8(1)	3.6(2)	3.1(0.7)	<b>2.0</b> (0.4)*	<b>1.1</b> (0.4)	15/15
IPOPCMAv3p	4.8(5)	4.3(4)	5.1(2)	5.0(1.0)	3.2(0.7)	15/15
LHD-10xDef	15(10)	12(8)	7.5(0.9)	21(19)	$\infty$ 1000	0/15
LHD-2xDefa	6.7(4)	4.8(3)	3.3(2)	5.8(4)	$\infty$ 1000	0/15
RAND-2xDef	6.4(2)	4.6(3)	3.6(1)	6.9(9)	$\infty$ 1000	0/15
RF1-CMAES	5.9(3)	5.3(3)	4.1(0.9)	3.9(1)	74(110)	1/15
RF5-CMAES	5.1(4)	5.2(3)	10(19)	145(184)	$\infty$ 5006	0/15
Sifeg	<b>2.5</b> (2)	<b>2.0</b> (2)	<b>1.9</b> (1)	21(30)	$\infty$ 1e5	0/15
Sif	<b>2.5</b> (1.0)	<b>2.0</b> (1)	<b>1.7</b> (1)	32(15)	$\infty$ 1e5	0/15
Srr	<b>2.5</b> (2)	<b>2.0</b> (2)	<b>1.6</b> (1.0)	14(18)	$\infty$ 7e4	0/15

Table 108: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f11</b>	<i>4.0e+4:11</i>	<i>2.5e+3:27</i>	<i>1.6e+2:313</i>	<i>1.0e+2:481</i>	<i>1.0e+1:1002</i>	15/15
BSifeg	<b>1.2</b> (1.0)	<b>1.3</b> (0.5)	796(1249)	4369(6014)	$\infty$ <i>1e5</i>	0/15
BSif	<b>1.2</b> (1)	<b>1.3</b> (0.6)	1191(1314)	$\infty$	$\infty$ <i>2e5</i>	0/15
BSqi	<b>1.2</b> (0.5)	<b>1.3</b> (1)	462(666)	2574(3002)	$\infty$ <i>2e5</i>	0/15
BSrr	<b>1.2</b> (0.8)	<b>1.3</b> (1)	1822(2282)	2506(3240)	$\infty$ <i>8e4</i>	0/15
CMA-CSA	<b>2.2</b> (2)	3.3(4)	12(1)	<b>8.1</b> (1.0)	<b>4.6</b> (0.3)	15/15
CMA-MSR	<b>2.0</b> (2)	<b>2.9</b> (2)	<b>9.2</b> (2)	<b>6.9</b> (1)	<b>4.7</b> (0.5)	15/15
CMA-TPA	<b>2.2</b> (2)	<b>2.5</b> (2)	10(1)	<b>7.2</b> (0.8)	<b>4.5</b> (0.3)	15/15
GP1-CMAES	<b>1.3</b> (1.0)	<b>1.8</b> (3)	14(14)	15(5)	$\infty$ <i>5006</i>	0/15
GP5-CMAES	<b>1.8</b> (1)	<b>2.3</b> (2)	<b>5.2</b> (3)	17(12)	$\infty$ <i>5008</i>	0/15
IPOPCMAv3p	<b>1.5</b> (0.9)	<b>2.5</b> (2)	52(91)	74(55)	$\infty$ <i>5006</i>	0/15
LHD-10xDefa	<b>2.6</b> (2)	4.0(4)	22(30)	$\infty$	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	<b>1.9</b> (1)	<b>2.6</b> (3)	22(10)	$\infty$	$\infty$ <i>1000</i>	0/15
RAND-2xDef	3.0(1)	<b>2.5</b> (3)	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
RF1-CMAES	<b>1.5</b> (0.6)	3.2(3)	<b>8.6</b> (5)	12(7)	$\infty$ <i>5006</i>	0/15
RF5-CMAES	<b>1.9</b> (2)	<b>2.8</b> (2)	105(152)	146(174)	$\infty$ <i>5008</i>	0/15
Sifeg	<b>1.2</b> (1)	<b>1.3</b> (1)	478(717)	3784(2685)	$\infty$ <i>1e5</i>	0/15
Sif	<b>1.2</b> (1)	<b>1.3</b> (0.5)	668(1268)	$\infty$	$\infty$ <i>1e5</i>	0/15
Srr	<b>1.2</b> (1)	<b>1.3</b> (1)	529(1045)	2003(2431)	$\infty$ <i>7e4</i>	0/15

Table 109: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>1.0e+8:23</i>	<i>6.3e+7:39</i>	<i>2.5e+7:76</i>	<i>4.0e+6:209</i>	<i>1.0e+1:1042</i>	15/15
BSifeg	3.5(0.9)	11(0.6)	16(38)	25(62)	$\infty$ <i>1e5</i>	0/15
BSif	<b>3.4</b> (2)	9.3(28)	29(130)	39(27)	$\infty$ <i>1e5</i>	0/15
BSqi	<b>3.2</b> (0.7)	12(36)	47(64)	63(231)	173(106)	9/15
BSrr	<b>3.3</b> (2)	11(33)	89(48)	69(211)	677(608)	2/15
CMA-CSA	5.4(2)	4.5(2)	<b>3.7</b> (0.7)	<b>2.3</b> (0.4)	<b>3.6</b> (3)	15/15
CMA-MSR	6.2(2)	4.9(2)	3.8(0.8)	<b>2.5</b> (0.2)	3.7(3)	15/15
CMA-TPA	7.2(3)	5.2(1)	3.8(0.6)	<b>2.0</b> (0.5)	3.8(4)	15/15
GP1-CMAES	4.7(3)	3.9(3)	3.7(0.9)	<b>2.8</b> (0.9)	<b>2.4</b> (4)	13/15
GP5-CMAES	18(82)	22(40)	38(31)	74(142)	21(12)	3/15
IPOPCMAv3p	5.1(3)	4.7(0.4)	3.8(1)	<b>2.5</b> (0.3)	3.8(2)	11/15
LHD-10xDef	17(7)	12(0.7)	8.9(4)	17(14)	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	4.6(2)	4.1(0.7)	3.8(0.8)	3.2(1)	$\infty$ <i>1000</i>	0/15
RAND-2xDef	5.0(1)	4.0(2)	<b>3.7</b> (1)	3.8(3)	$\infty$ <i>1000</i>	0/15
RF1-CMAES	3.9(2)	3.9(1)	<b>3.1</b> (0.5)	<b>1.8</b> (0.1)	<b>3.0</b> (2)	12/15
RF5-CMAES	5.2(2)	4.6(1)	9.4(2)	39(108)	$\infty$ <i>5006</i>	0/15
Sifeg	3.7(0.6)	<b>3.0</b> (0.3)	8.1(20)	26(19)	$\infty$ <i>4e4</i>	0/15
Sif	3.7(3)	<b>3.2</b> (4)	12(37)	23(12)	$\infty$ <i>5e4</i>	0/15
Srr	4.6(0.6)	<b>3.8</b> (3)	28(19)	20(28)	$\infty$ <i>4e4</i>	0/15

Table 110: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>1.6e+3:28</i>	<i>1.0e+3:64</i>	<i>6.3e+2:79</i>	<i>4.0e+1:211</i>	<i>2.5e+0:1724</i>	15/15
BSifeg	<b>2.2</b> (0.3)	<b>1.3</b> (0.1)	<b>1.5</b> (0.1)	125(442)	99(70)	11/15
BSif	<b>2.2</b> (0.7)	<b>1.3</b> (0.2)	<b>1.5</b> (0.1)	1842(1760)	$\infty$ 2e5	0/15
BSqi	<b>2.2</b> (0.6)	<b>1.3</b> (0.2)	<b>1.4</b> (0.2)	71(9)	106(67)	9/15
BSrr	<b>2.2</b> (0.5)	<b>1.3</b> (0.1)	<b>1.4</b> (0.2)	67(143)	88(62)	11/15
CMA-CSA	4.3(2)	3.6(0.7)	4.7(0.8)	<b>5.4</b> (0.4)	<b>2.8</b> (2)	15/15
CMA-MSR	5.6(1)	4.3(1)	4.9(0.4)	6.1(0.3)	<b>2.8</b> (1)	15/15
CMA-TPA	3.9(1.0)	3.0(0.9)	3.7(0.6)	<b>5.3</b> (0.3)	<b>4.0</b> (3)	15/15
GP1-CMAES	<b>2.5</b> (0.9)	<b>2.4</b> (0.4)	<b>2.9</b> (0.5)	49(26)	42(52)	1/15
GP5-CMAES	<b>2.4</b> (0.4)	<b>1.5</b> (0.3)	<b>1.6</b> (0.3)	<b>2.9</b> (0.8) <sup>*2</sup>	4.5(14)	7/15
IPOPCMAv3p	3.3(2)	3.9(1)	5.5(0.8)	8.0(3)	9.1(7)	4/15
LHD-10xDef	15(0.1)	6.9(0.1)	6.3(0.2)	8.5(7)	$\infty$ 1000	0/15
LHD-2xDefa	3.3(1)	<b>2.2</b> (0.2)	<b>2.8</b> (2)	9.4(9)	$\infty$ 1000	0/15
RAND-2xDef	3.5(0.5)	<b>2.2</b> (0.3)	<b>2.9</b> (0.5)	7.1(6)	$\infty$ 1000	0/15
RF1-CMAES	3.2(1)	<b>3.0</b> (1)	3.9(1)	7.1(1)	7.3(5)	5/15
RF5-CMAES	3.4(2)	<b>3.0</b> (0.7)	4.2(1)	343(659)	$\infty$ 5006	0/15
Sifeg	<b>2.2</b> (0.7)	<b>1.3</b> (0.1)	<b>1.4</b> (0.1)	19(41)	43(29)	15/15
Sif	<b>2.2</b> (0.8)	<b>1.3</b> (0.1)	<b>1.4</b> (0.1)	23(84)	81(59)	11/15
Srr	<b>2.2</b> (0.6)	<b>1.3</b> (0.1)	<b>1.4</b> (0.1)	16(77)	64(111)	13/15

Table 111: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>2.5e+1:15</i>	<i>1.6e+1:42</i>	<i>1.0e+1:75</i>	<i>1.6e+0:219</i>	<i>6.3e-4:1106</i>	15/15
BSifeg	3.3(2)	<b>1.7</b> (0.4)	<b>1.5</b> (0.6)	10(9)	$\infty$ 2e5	0/15
BSif	3.3(2)	<b>1.7</b> (0.7)	<b>1.5</b> (0.8)	9.1(10)	$\infty$ 2e5	0/15
BSqi	3.9(1)	<b>2.0</b> (0.3)	<b>1.5</b> (0.3)	4.7(3)	$\infty$ 2e5	0/4
BSrr	3.3(2)	<b>1.7</b> (1.0)	<b>1.4</b> (0.6)	6.4(5)	$\infty$ 2e5	0/15
CMA-CSA	9.1(7)	4.8(2)	4.2(1)	<b>2.9</b> (0.3)	<b>3.1</b> (0.4)	15/15
CMA-MSR	8.7(2)	4.7(2)	4.2(0.8)	<b>2.7</b> (0.4)	<b>2.7</b> (0.2)	15/15
CMA-TPA	8.9(8)	4.8(3)	3.5(2)	<b>2.4</b> (0.3)	<b>2.6</b> (0.4)	15/15
GP1-CMAES	7.9(5)	3.9(1)	<b>3.0</b> (0.7)	<b>2.3</b> (0.6)	4.6(2)	13/15
GP5-CMAES	5.7(2)	<b>2.6</b> (0.6)	<b>2.1</b> (0.3)	<b>1.7</b> (0.5)	67(23)	1/15
IPOPCMAv3p	10(3)	4.6(1)	3.7(1)	<b>2.9</b> (0.3)	3.9(0.4)	15/15
LHD-10xDef	25(7)	11(0.8)	6.9(0.4)	7.7(6)	$\infty$ 1000	0/15
LHD-2xDefa	8.1(2)	3.7(1)	3.1(1)	3.8(3)	$\infty$ 1000	0/15
RAND-2xDef	8.8(2)	4.1(0.8)	3.3(0.9)	7.3(6)	$\infty$ 1000	0/15
RF1-CMAES	7.1(3)	4.4(2)	3.5(0.9)	3.1(0.9)	33(32)	2/15
RF5-CMAES	6.5(7)	3.9(2)	3.7(1)	153(104)	$\infty$ 5006	0/15
Sifeg	<b>3.3</b> (2)	<b>1.8</b> (0.5)	<b>1.3</b> (0.4)	<b>1.4</b> (0.7)	$\infty$ 2e5	0/15
Sif	<b>3.3</b> (2)	<b>1.8</b> (0.8)	<b>1.3</b> (0.4)	<b>1.5</b> (0.9)	$\infty$ 2e5	0/15
Srr	<b>3.3</b> (2)	<b>1.8</b> (0.7)	<b>1.3</b> (0.5)	<b>1.1</b> (0.7)	$\infty$ 2e5	0/15



Table 112: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>6.3e+2:15</i>	<i>4.0e+2:67</i>	<i>2.5e+2:292</i>	<i>1.6e+2:846</i>	<i>1.0e+2:1671</i>	15/15
BSifeg	<b>2.2</b> (2)	18(0.6)	274(399)	525(570)	1563(1672)	1/15
BSif	<b>2.2</b> (2)	76(563)	296(322)	943(1318)	1581(3030)	1/15
BSqi	<b>2.1</b> (1)	15(0.3)	224(291)	346(493)	$\infty$ 2e5	0/11
BSrr	<b>2.2</b> (1)	5.7(33)	272(279)	450(534)	1391(3523)	1/15
CMA-CSA	4.9(2)	<b>2.5</b> (0.6)	<b>1.1</b> (0.2)	<b>0.86</b> (0.2)	<b>1.5</b> (0.6)	15/15
CMA-MSR	6.2(4)	<b>2.8</b> (1)	<b>1.1</b> (0.3)	<b>0.68</b> (0.1)	<b>0.44</b> (0.1)	15/15
CMA-TPA	6.1(3)	<b>2.3</b> (0.4)	<b>0.87</b> (0.3)	<b>0.70</b> (0.2)	<b>0.72</b> (0.1)	15/15
GP1-CMAES	3.6(2)	<b>1.9</b> (0.8)	<b>0.81</b> (0.2)	<b>0.78</b> (0.4)	<b>0.64</b> (0.2)	15/15
GP5-CMAES	3.7(3)	<b>1.5</b> (0.3)	<b>0.60</b> (0.2)	<b>2.2</b> (8)	3.9(3)	7/15
IPOPCMAv3p	4.5(3)	<b>2.6</b> (1)	<b>1.2</b> (0.3)	<b>1.2</b> (0.4)	<b>1.4</b> (2)	14/15
LHD-10xDef	16(14)	6.4(0.1)	<b>1.9</b> (0.4)	<b>1.1</b> (0.2)	<b>1.2</b> (0.5)	7/15
LHD-2xDefa	5.5(2)	<b>2.0</b> (0.9)	<b>1.1</b> (0.9)	<b>1.5</b> (1)	8.7(6)	1/15
RAND-2xDef	5.1(2)	<b>1.9</b> (0.5)	<b>1.1</b> (0.5)	<b>1.6</b> (0.4)	8.8(6)	1/15
RF1-CMAES	4.5(2)	<b>2.2</b> (1)	<b>0.93</b> (0.2)	<b>0.92</b> (0.2)	<b>0.70</b> (0.1)	15/15
RF5-CMAES	3.6(2)	<b>1.9</b> (0.4)	<b>0.95</b> (0.5)	<b>1.7</b> (2)	6.5(6)	5/15
Sifeg	<b>2.2</b> (1)	46(168)	49(91)	126(362)	774(620)	2/15
Sif	<b>2.2</b> (2)	52(0.5)	74(144)	170(170)	703(1812)	2/15
Srr	<b>2.2</b> (2)	52(190)	72(135)	100(124)	352(371)	4/15

Table 113: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>4.0e+1:26</i>	<i>2.5e+1:127</i>	<i>1.6e+1:540</i>	<i>1.6e+1:540</i>	<i>1.0e+1:1384</i>	15/15
BSifeg	<b>1.7</b> (1)	<b>0.92</b> (0.2)	44(119)	44(89)	123(354)	9/15
BSif	<b>1.7</b> (1)	<b>0.92</b> (0.2)	42(89)	42(88)	178(188)	8/15
BSqi	<b>1.7</b> (1)	<b>0.93</b> (0.2)	21(42)	21(0.7)	98(223)	10/13
BSrr	<b>1.7</b> (0.9)	<b>0.93</b> (0.2)	40(46)	40(134)	119(89)	10/15
CMA-CSA	7.8(10)	16(6)	4.3(2)	4.3(1)	<b>1.9</b> (0.6)	15/15
CMA-MSR	5.2(2)	<b>2.1</b> (0.4)	<b>0.81</b> (0.3)	<b>0.81</b> (0.4)	<b>0.80</b> (1)	15/15
CMA-TPA	4.5(8)	8.4(6)	<b>2.2</b> (1)	<b>2.2</b> (1)	<b>1.2</b> (0.7)	15/15
GP1-CMAES	3.3(2)	4.3(2)	<b>1.4</b> (0.3)	<b>1.4</b> (0.2)	<b>0.90</b> (0.1)	14/15
GP5-CMAES	3.4(3)	<b>1.6</b> (0.6)	<b>0.54</b> (0.2)	<b>0.54</b> (0.2)	<b>0.57</b> (0.2)	15/15
IPOPCMAv3p	3.4(4)	10(4)	3.2(1)	3.2(1)	<b>1.4</b> (0.4)	15/15
LHD-10xDef	6.5(7)	5.4(2)	4.8(3)	4.8(3)	3.4(4)	3/15
LHD-2xDefa	3.2(3)	3.6(2)	<b>2.6</b> (3)	<b>2.6</b> (3)	5.1(8)	2/15
RAND-2xDef	3.8(3)	6.4(8)	5.0(8)	5.0(8)	11(16)	1/15
RF1-CMAES	<b>2.8</b> (4)	4.6(3)	<b>1.6</b> (0.5)	<b>1.6</b> (0.4)	<b>0.79</b> (0.2)	15/15
RF5-CMAES	4.2(4)	<b>2.2</b> (2)	<b>0.83</b> (0.2)	<b>0.83</b> (0.3)	<b>1.0</b> (3)	13/15
Sifeg	<b>1.9</b> (2)	<b>1.5</b> (0.6)	10(9)	10(7)	15(22)	15/15
Sif	<b>1.9</b> (2)	<b>1.6</b> (1)	6.1(6)	6.1(6)	12(12)	15/15
Srr	<b>1.9</b> (1)	<b>1.8</b> (3)	3.3(12)	3.3(0.9)	14(10)	15/15

Table 114: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.6e+1:11</i>	<i>1.0e+1:63</i>	<i>6.3e+0:305</i>	<i>4.0e+0:468</i>	<i>1.0e+0:1030</i>	15/15
BSifeg	22(2)	493(0.8)	1042(852)	$\infty$	$\infty$ 2e5	0/15
BSif	35(3)	488(791)	2637(4581)	$\infty$	$\infty$ 2e5	0/15
BSqi	<b>2.6</b> (1)	<b>1.7</b> (0.6)	346(328)	$\infty$	$\infty$ 2e5	0/3
BSrr	27(3)	476(1)	1359(2006)	$\infty$	$\infty$ 2e5	0/15
CMA-CSA	7.5(5)	<b>3.0</b> (2)	<b>1.1</b> (0.2)	<b>1.0</b> (0.2)	<b>1.0</b> (0.2)	15/15
CMA-MSR	7.9(3)	<b>2.7</b> (0.6)	<b>0.90</b> (0.2)	<b>1.0</b> (0.2)	6.5(3)	15/15
CMA-TPA	8.8(7)	<b>2.7</b> (0.7)	<b>0.93</b> (0.1)	<b>0.95</b> (0.3)	<b>1.4</b> (0.4)	15/15
GP1-CMAES	<b>2.4</b> (3)	<b>1.4</b> (0.8)	<b>0.73</b> (0.3)	<b>0.79</b> (0.3)	3.4(10)	10/15
GP5-CMAES	3.3(2)	<b>1.6</b> (0.8)	<b>0.79</b> (0.4)	<b>0.87</b> (0.6)	11(27)	5/15
IPOPCMAv3p	<b>2.8</b> (2)	<b>2.0</b> (2)	<b>0.89</b> (0.3)	<b>0.95</b> (0.3)	<b>0.99</b> (0.2)	15/15
LHD-10xDef	12(9)	7.3(2)	<b>2.2</b> (0.4)	5.7(2)	$\infty$ 1000	0/15
LHD-2xDefa	3.3(4)	<b>2.6</b> (0.8)	<b>1.4</b> (2)	10(8)	$\infty$ 1000	0/15
RAND-2xDef	5.0(4)	<b>2.7</b> (2)	<b>2.1</b> (2)	31(38)	$\infty$ 1000	0/15
RF1-CMAES	3.1(3)	<b>1.9</b> (0.7)	<b>0.78</b> (0.3)	<b>0.83</b> (0.3)	4.2(10)	9/15
RF5-CMAES	4.0(2)	<b>2.7</b> (0.8)	3.6(5)	17(13)	$\infty$ 5006	0/15
Sifeg	3.8(6)	230(797)	797(1392)	5983(5449)	$\infty$ 2e5	0/15
Sif	3.6(5)	7.1(18)	750(822)	5964(6604)	$\infty$ 2e5	0/15
Srr	3.6(3)	3.8(6)	979(1795)	5963(5002)	$\infty$ 2e5	0/15

Table 115: 20-D, running time excess  $ERT/ERT_{\text{best } 2009}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>4.0e+1:116</i>	<i>2.5e+1:252</i>	<i>1.6e+1:430</i>	<i>1.0e+1:621</i>	<i>4.0e+0:1090</i>	15/15
BSifeg	5.9(13)	468(752)	5872(6811)	$\infty$	$\infty$ 2e5	0/14
BSif	123(7)	758(760)	$\infty$	$\infty$	$\infty$ 2e5	0/15
BSqi	<b>0.80</b> (0.3)	368(889)	$\infty$	$\infty$	$\infty$ 2e5	0/4
BSrr	26(0.2)	649(989)	$\infty$	$\infty$	$\infty$ 2e5	0/15
CMA-CSA	<b>1.3</b> (0.3)	<b>1.0</b> (0.3)	<b>0.96</b> (0.1)	<b>0.96</b> (0.3)	<b>0.96</b> (0.3)	15/15
CMA-MSR	<b>1.3</b> (0.5)	<b>1.0</b> (0.3)	<b>0.97</b> (0.6)	<b>2.8</b> (0.2)	4.8(13)	15/15
CMA-TPA	<b>1.3</b> (0.7)	<b>1.0</b> (0.7)	<b>0.92</b> (0.3)	<b>1.6</b> (3)	<b>1.3</b> (0.3)	15/15
GP1-CMAES	<b>0.81</b> (0.3)	<b>0.84</b> (0.3)	<b>0.85</b> (0.3)	<b>0.93</b> (0.5)	5.2(6)	8/15
GP5-CMAES	<b>0.95</b> (0.9)	<b>0.85</b> (0.6)	<b>1.7</b> (3)	<b>2.8</b> (4)	19(22)	3/15
IPOPCMAv3p	<b>0.94</b> (0.7)	<b>1.1</b> (0.2)	<b>1.1</b> (0.4)	<b>1.1</b> (0.4)	<b>1.1</b> (0.2)	15/15
LHD-10xDef	3.5(0.5)	<b>2.7</b> (0.8)	5.2(3)	$\infty$	$\infty$ 1000	0/15
LHD-2xDefa	<b>1.00</b> (0.6)	<b>1.6</b> (0.7)	11(6)	$\infty$	$\infty$ 1000	0/15
RAND-2xDef	<b>0.99</b> (0.4)	<b>1.6</b> (1)	16(11)	$\infty$	$\infty$ 1000	0/15
RF1-CMAES	<b>0.87</b> (0.4)	<b>0.82</b> (0.2)	<b>0.87</b> (0.2)	<b>1.0</b> (0.2)	10(9)	5/15
RF5-CMAES	<b>1.3</b> (0.4)	<b>2.7</b> (1)	5.4(3)	53(99)	$\infty$ 5006	0/15
Sifeg	48(9)	217(303)	1821(1148)	$\infty$	$\infty$ 2e5	0/15
Sif	91(59)	367(370)	1063(2314)	4564(4318)	$\infty$ 2e5	0/15
Srr	30(8)	132(7)	801(1299)	$\infty$	$\infty$ 2e5	0/15

Table 116: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:2.5e5</i>	<i>1.0e-1:3.4e5</i>	<i>6.3e-2:3.4e5</i>	<i>4.0e-2:3.4e5</i>	<i>2.5e-2:3.4e5</i>	3/15
BSifeg	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
BSif	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
BSqi	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/8
BSrr	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
CMA-CSA	<b>0.89</b> <sup>(0.5)</sup>	<b>0.82</b> <sup>(0.5)</sup>	<b>0.87</b> <sup>(0.5)</sup>	<b>2.9</b> <sup>(2)</sup>	<b>5.6</b> <sup>(4)</sup>	11/15
CMA-MSR	<b>1.2</b> <sup>(0.5)</sup>	<b>1.2</b> <sup>(0.4)</sup>	<b>1.7</b> <sup>(0.9)</sup>	<b>3.0</b> <sup>(5)</sup>	<b>15</b> <sup>(28)</sup>	5/15
CMA-TPA	<b>1.3</b> <sup>(0.6)</sup>	<b>1.6</b> <sup>(0.6)</sup>	<b>2.3</b> <sup>(0.9)</sup>	<b>3.4</b> <sup>(2)</sup>	<b>7.9</b> <sup>(8)</sup>	9/15
GP1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5006</i>	0/15
GP5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5020</i>	0/15
IPOPCMAv3p	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5008</i>	0/15
LHD-10xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
LHD-2xDefa	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
RAND-2xDef	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>1000</i>	0/15
RF1-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5008</i>	0/15
RF5-CMAES	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>5034</i>	0/15
Sifeg	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
Sif	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15
Srr	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$ <i>2e5</i>	0/15

Table 117: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f20</b>	<i>1.6e+4:38</i>	<i>1.0e+4:42</i>	<i>2.5e+2:62</i>	<i>2.5e+0:250</i>	<i>1.6e+0:2536</i>	15/15
BSifeg	<b>1.8</b> (0.6)	<b>1.8</b> (0.6)	<b>1.6</b> (0.6)	<b>2.1</b> (4)	3.2(0.8)	15/15
BSif	<b>1.8</b> (1)	<b>1.8</b> (0.3)	<b>1.6</b> (0.8)	<b>1.6</b> (0.8)	<b>1.4</b> (1)	15/15
BSqi	<b>1.1</b> (1)	<b>1.5</b> (1)	<b>1.5</b> (0.5)	<b>1.0</b> (0.3)	<b>1.3</b> (0.3)	4/4
BSrr	<b>1.8</b> (0.5)	<b>1.8</b> (1)	<b>1.6</b> (0.5)	<b>1.1</b> (0.5)	4.8(14)	15/15
CMA-CSA	3.2(1)	3.7(0.6)	5.5(2)	7.6(9)	18(13)	15/15
CMA-MSR	3.8(0.8)	4.2(1)	5.9(1)	3.2(0.5)	4477(3623)	2/15
CMA-TPA	3.4(0.7)	3.8(0.4)	4.3(0.9)	5.8(0.6)	432(576)	10/15
GP1-CMAES	<b>2.8</b> (1)	3.2(1)	3.6(0.2)	4.0(2)	$\infty$ 5006	0/15
GP5-CMAES	<b>2.3</b> (0.5)	<b>2.2</b> (0.2)	<b>2.5</b> (0.4)	284(618)	$\infty$ 5022	0/15
IPOPCMAv3p	3.5(1)	4.3(2)	6.1(0.9)	5.9(0.5)	6.2(6)	4/15
LHD-10xDef	11(2)	10(0.2)	8.7(0.5)	7.9(10)	$\infty$ 1000	0/15
LHD-2xDefa	3.3(0.6)	3.3(0.6)	4.4(2)	<b>2.8</b> (2)	5.7(4)	1/15
RAND-2xDef	3.1(0.6)	3.1(0.7)	4.8(3)	4.9(2)	$\infty$ 1000	0/15
RF1-CMAES	3.5(0.7)	3.9(0.6)	5.2(1)	3.4(1)	6.1(7)	4/15
RF5-CMAES	<b>2.6</b> (0.8)	<b>2.9</b> (1)	6.6(4)	134(150)	$\infty$ 5006	0/15
Sifeg	<b>1.8</b> (0.6)	<b>1.8</b> (0.3)	<b>1.9</b> (0.3)	<b>0.75</b> (0.1)	<b>0.55</b> (0.6)	15/15
Sif	<b>1.8</b> (1)	<b>1.8</b> (0.6)	<b>1.9</b> (0.7)	<b>0.82</b> (0.4)	<b>0.64</b> (0.5)	15/15
Srr	<b>1.8</b> (0.6)	<b>1.8</b> (0.7)	<b>1.9</b> (0.4)	<b>0.71</b> (0.1)	<b>0.51</b> (0.3)	15/15

Table 118: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f21</i></b>	<i>6.3e+1:36</i>	<i>4.0e+1:77</i>	<i>4.0e+1:77</i>	<i>1.6e+1:456</i>	<i>4.0e+0:1094</i>	15/15
BSifeg	<b>2.0</b> (0.1)	<b>1.2</b> (0.2)	<b>1.2</b> (0.2)	87(219)	98(149)	11/15
BSif	<b>2.0</b> (0.3)	<b>1.2</b> (0.2)	<b>1.2</b> (0.2)	93(158)	146(109)	9/15
BSqi	<b>2.1</b> (0.1)	<b>1.4</b> (0.5)	<b>1.4</b> (0.5)	187(401)	79(117)	3/4
BSrr	<b>2.0</b> (0.1)	<b>1.2</b> (0.1)	<b>1.2</b> (0.6)	80(44)	162(230)	8/15
CMA-CSA	5.6(2)	3.4(0.9)	3.4(0.5)	<b>2.5</b> (3)	99(520)	14/15
CMA-MSR	5.0(1)	3.1(0.8)	3.1(0.9)	<b>1.6</b> (0.2)	234(2)	13/15
CMA-TPA	4.9(2)	3.3(1)	3.3(1)	17(4)	198(577)	13/15
GP1-CMAES	3.8(2)	6.3(0.4)	6.3(0.6)	<b>1.8</b> (5)	3.4(1)	10/15
GP5-CMAES	3.2(1.0)	<b>2.9</b> (0.4)	<b>2.9</b> (8)	<b>1.8</b> (2)	7.7(10)	6/15
IPOPCMAv3p	5.8(5)	5.5(4)	5.5(2)	3.2(4)	7.8(7)	6/15
LHD-10xDef	13(0.8)	6.6(0.6)	6.6(0.9)	<b>2.0</b> (2)	<b>2.4</b> (4)	5/15
LHD-2xDefa	3.6(0.6)	<b>2.6</b> (1)	<b>2.6</b> (3)	<b>0.88</b> (0.3)	<b>1.2</b> (0.8)	9/15
RAND-2xDef	3.4(0.6)	<b>1.9</b> (0.4)	<b>1.9</b> (0.5)	<b>0.46</b> (0.1)	<b>0.57</b> (0.5)	12/15
RF1-CMAES	5.2(2)	3.7(1)	3.7(1)	5.5(6)	8.0(10)	6/15
RF5-CMAES	7.6(2)	6.1(2)	6.1(1)	8.7(6)	14(7)	4/15
Sifeg	<b>2.0</b> (0.3)	<b>1.3</b> (0.3)	<b>1.3</b> (0.5)	65(164)	87(267)	12/15
Sif	<b>2.0</b> (0.5)	<b>1.3</b> (0.5)	<b>1.3</b> (0.1)	106(141)	136(259)	9/15
Srr	<b>2.0</b> (0.3)	<b>1.3</b> (0.6)	<b>1.3</b> (0.3)	67(103)	160(92)	8/15

Table 119: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f22</b>	<i>6.3e+1:45</i>	<i>4.0e+1:68</i>	<i>4.0e+1:68</i>	<i>1.6e+1:231</i>	<i>6.3e+0:1219</i>	15/15
BSifeg	<b>1.6</b> (0.2)	4.4(24)	4.4(12)	166(86)	156(297)	8/15
BSif	<b>1.6</b> (0.3)	6.1(0.3)	6.1(0.1)	196(144)	225(246)	7/15
BSqi	<b>1.6</b> (0.0)	6.6(14)	6.6(0.0)	228(445)	230(456)	2/5
BSrr	<b>1.6</b> (0.3)	3.5(9)	3.5(9)	167(263)	117(123)	10/15
CMA-CSA	4.6(1)	9.1(2)	9.1(17)	38(98)	230(458)	12/15
CMA-MSR	5.8(1)	14(18)	14(35)	7.9(11)	206(329)	13/15
CMA-TPA	4.0(1)	6.8(1)	6.8(1)	327(0.8)	428(431)	10/15
GP1-CMAES	12(29)	17(17)	17(20)	12(11)	<b>2.7</b> (1)	10/15
GP5-CMAES	<b>2.5</b> (0.3)	3.6(6)	3.6(12)	4.8(8)	<b>2.0</b> (7)	11/15
IPOPCMAv3p	4.6(2)	10(2)	10(2)	6.7(6)	4.6(5)	8/15
LHD-10xDef	10(0.4)	7.8(2)	7.8(2)	5.4(5)	<b>2.1</b> (1)	5/15
LHD-2xDefa	3.4(0.6)	3.3(3)	3.3(2)	<b>2.0</b> (3)	<b>1.2</b> (2)	8/15
RAND-2xDef	3.3(0.6)	3.2(2)	3.2(0.3)	<b>1.9</b> (2)	<b>1.1</b> (1)	8/15
RF1-CMAES	4.6(3)	5.2(3)	5.2(1)	<b>4.6</b> (6)	<b>3.0</b> (0.4)	10/15
RF5-CMAES	5.8(3)	11(38)	11(22)	11(17)	5.7(4)	7/15
Sifeg	<b>1.6</b> (0.4)	<b>1.7</b> (4)	<b>1.7</b> (0.2)	230(351)	159(287)	9/15
Sif	<b>1.6</b> (0.1)	<b>1.9</b> (6)	<b>1.9</b> (0.2)	118(156)	125(125)	10/15
Srr	<b>1.6</b> (0.4)	<b>1.5</b> (0.2)	<b>1.5</b> (3)	170(497)	133(101)	9/15



Table 120: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f23</i></b>	<i>6.3e+0:29</i>	<i>4.0e+0:118</i>	<i>2.5e+0:306</i>	<i>2.5e+0:306</i>	<i>1.0e+0:1614</i>	15/15
BSifeg	<b>2.3</b> (2)	<b>1.4</b> (0.4)	<b>1.9</b> (2)	<b>1.9</b> (2)	60(52)	14/15
BSif	<b>2.3</b> (2)	<b>1.4</b> (0.4)	<b>2.8</b> (10)	<b>2.8</b> (5)	37(39)	15/15
BSrr	<b>2.3</b> (2)	<b>1.4</b> (0.5)	<b>2.5</b> (2)	<b>2.5</b> (5)	54(25)	14/15
CMA-CSA	6.7(4)	8.1(5)	37(35)	37(45)	93(10)	15/15
CMA-MSR	4.1(3)	3.9(2)	4.3(0.6)	4.3(10)	<b>2.0</b> (6)	15/15
CMA-TPA	5.2(3)	12(10)	34(47)	34(50)	23(38)	15/15
GP1-CMAES	<b>2.1</b> (2)	6.4(4)	5.8(5)	5.8(2)	<b>1.6</b> (0.9)	14/15
GP5-CMAES	<b>2.2</b> (3)	<b>2.9</b> (2)	<b>1.9</b> (4)	<b>1.9</b> (0.2)	<b>0.84</b> (0.8)	15/15
IPOPCMAv3p	<b>1.5</b> (2)	6.7(4)	75(126)	75(72)	$\infty$ 5020	0/15
LHD-10xDef	<b>2.3</b> (3)	8.2(16)	48(43)	48(25)	$\infty$ 1000	0/15
LHD-2xDefa	<b>1.6</b> (2)	5.6(7)	23(20)	23(22)	$\infty$ 1000	0/15
RAND-2xDef	<b>2.1</b> (0.8)	6.2(5)	$\infty$	$\infty$	$\infty$ 1000	0/15
RF1-CMAES	<b>1.3</b> (0.9)	3.4(6)	244(139)	244(275)	$\infty$ 5010	0/15
RF5-CMAES	<b>1.8</b> (3)	4.5(6)	113(313)	113(144)	$\infty$ 5086	0/15
Sifeg	<b>2.3</b> (2)	4.7(3)	4.2(3)	4.2(2)	6.5(5)	15/15
Sif	<b>2.3</b> (2)	4.7(2)	4.4(2)	4.4(2)	11(9)	15/15
Srr	<b>2.3</b> (1)	4.8(3)	3.9(1)	3.9(2)	5.2(8)	15/15

Table 121: 20-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best } 2009}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best } 2009}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f24</b>	<i>2.5e+2</i> :208	<i>1.6e+2</i> :918	<i>1.0e+2</i> :6628	<i>6.3e+1</i> :9885	<i>4.0e+1</i> :31629	15/15
BSifeg	61(21)	73(139)	56(58)	$\infty$	$\infty$ 2e5	0/15
BSif	76(70)	187(223)	196(301)	$\infty$	$\infty$ 2e5	0/15
BSrr	63(152)	78(66)	75(81)	$\infty$	$\infty$ 2e5	0/15
CMA-CSA	<b>1.5</b> (0.2)	<b>1.4</b> (0.2)	<b>1.4</b> (0.5)	<b>0.99</b> (1)	<b>0.87</b> (0.8)	15/15
CMA-MSR	<b>1.3</b> (0.3)	<b>0.73</b> (0.1)	<b>0.21</b> (0.3)	<b>0.61</b> (0.4)	<b>0.34</b> (0.2)	15/15
CMA-TPA	<b>1.2</b> (0.3)	<b>1.7</b> (1.0)	<b>0.71</b> (0.3)	<b>0.67</b> (0.3)	<b>0.92</b> (0.3)	15/15
GP1-CMAES	<b>0.83</b> (0.3)	<b>0.84</b> (0.3)	<b>0.20</b> (0.0)	<b>0.24</b> (0.1)	<b>0.38</b> (0.6)	5/15
GP5-CMAES	<b>0.51</b> (0.1) $\uparrow_4$	<b>0.86</b> (0.2)	<b>0.37</b> (0.2)	<b>0.32</b> (0.3)	<b>1.1</b> (0.9)	2/15
IPOPCMAv3p	<b>1.4</b> (0.4)	<b>1.7</b> (1)	5.5(3)	7.5(9)	$\infty$ 5008	0/15
LHD-10xDef	3.0(3)	<b>1.6</b> (0.8)	<b>0.74</b> (0.8)	$\infty$	$\infty$ 1000	0/15
LHD-2xDefa	7.5(3)	7.8(10)	$\infty$	$\infty$	$\infty$ 1000	0/15
RAND-2xDef	9.3(12)	$\infty$	$\infty$	$\infty$	$\infty$ 1000	0/15
RF1-CMAES	<b>1.4</b> (0.3)	<b>2.5</b> (2)	<b>1.0</b> (1)	<b>2.4</b> (4)	<b>2.3</b> (3)	1/15
RF5-CMAES	<b>2.2</b> (1)	4.1(4)	11(21)	$\infty$	$\infty$ 5034	0/15
Sifeg	16(45)	19(27)	23(9)	258(219)	$\infty$ 2e5	0/15
Sif	19(16)	20(30)	28(44)	$\infty$	$\infty$ 2e5	0/15
Srr	17(12)	12(11)	13(17)	$\infty$	$\infty$ 2e5	0/15

Table 122: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_1$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f1</b>	<i>2.5e+2:48</i>	<i>1.6e+2:82</i>	<i>1.0e-8:83</i>	<i>1.0e-8:83</i>	<i>1.0e-8:83</i>	15/15
CMA-CSA	<b>2.0</b> (0.5)	2.3(0.9)	64(4)	64(2)	64(4)	15/15
CMA-MSR	2.6(0.9)	2.8(0.7)	66(3)	66(3)	66(2)	15/15
CMA-TPA	2.5(0.7)	<b>2.3</b> (0.4)	<b>43</b> (1) <sup>*4</sup>	<b>43</b> (2) <sup>*4</sup>	<b>43</b> (2) <sup>*4</sup>	15/15

Table 123: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_2$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f2</b>	<i>1.0e+7:39</i>	<i>6.3e+6:71</i>	<i>4.0e+5:121</i>	<i>2.5e+4:499</i>	<i>1.0e-8:1188</i>	15/15
CMA-CSA	<b>1.3</b> (0.9)	1.9(0.9)	17(8)	12(1)	<b>40</b> (1) <sup>*4</sup>	15/15
CMA-MSR	2.0(1)	<b>1.8</b> (1)	<b>8.0</b> (2)	<b>8.2</b> (2)	47(0.9)	15/15
CMA-TPA	2.1(2)	2.2(0.8)	8.5(2)	8.9(3)	46(0.9)	15/15

Table 124: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_3$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f3</b>	<i>1.6e+3:68</i>	<i>1.0e+3:222</i>	<i>6.3e+2:471</i>	<i>4.0e+2:662</i>	<i>6.3e+1:6332</i>	15/15
CMA-CSA	<b>1.8</b> (1)	1.4(0.4)	1.1(0.2)	1.8(0.3)	3.6(1)	15/15
CMA-MSR	2.3(1)	1.3(0.5)	1.1(0.2)	<b>1.3</b> (0.2)	4.0(1)	15/15
CMA-TPA	2.3(1)	<b>1.1</b> (0.3)	<b>0.83</b> (0.1)*	1.4(0.5)	<b>2.7</b> (2)	15/15

Table 125: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_4$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f4</b>	<i>1.0e+3:439</i>	<i>6.3e+2:670</i>	<i>4.0e+2:707</i>	<i>2.5e+2:735</i>	<i>1.0e+2:5369</i>	15/15
CMA-CSA	1.2(0.4)	1.5(0.2)	3.3(0.8)	4.5(0.8)	<b>3.6</b> (3)	15/15
CMA-MSR	1.1(0.2)	1.2(0.3)	<b>1.8</b> (0.4)	12(8)	8.1(3)	15/15
CMA-TPA	<b>0.94</b> (0.2)	<b>1.1</b> (0.1)	2.0(0.4)	<b>2.5</b> (0.4)	4.5(2)	15/15

Table 126: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_5$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f5</b>	<i>4.0e+2:51</i>	<i>2.5e+2:81</i>	<i>1.0e-1:120</i>	<i>1.0e-8:121</i>	<i>1.0e-8:121</i>	15/15
CMA-CSA	1.7(0.5)	1.8(0.4)	4.4(0.5)	4.4(0.3)	4.4(0.4)	15/15
CMA-MSR	1.7(0.9)	1.8(0.3)	3.6(0.3)	<b>3.6</b> (0.7)	<b>3.6</b> (0.5)	15/15
CMA-TPA	<b>1.2</b> (0.5)*	<b>1.2</b> (0.4)* <sup>2</sup>	<b>3.5</b> (0.5)	3.6(0.4)	3.6(0.3)	15/15

Table 127: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_6$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f6</b>	<i>6.3e+5:50</i>	<i>4.0e+5:82</i>	<i>4.0e+4:127</i>	<i>4.0e+2:734</i>	<i>6.3e+1:2121</i>	15/15
CMA-CSA	<b>1.6</b> (0.5)	<b>1.4</b> (0.7)	2.1(0.5)	2.9(0.2)	1.8(0.2)	15/15
CMA-MSR	1.8(0.8)	1.6(0.7)	<b>2.0</b> (0.5)	<b>1.7</b> (0.2)	1.7(0.9)	15/15
CMA-TPA	1.6(0.4)	1.9(0.5)	2.3(0.7)	1.9(0.3)	<b>1.5</b> (0.5)	15/15



Table 128: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_7$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f7</i></b>	<i>1.6e+3:35</i>	<i>1.0e+3:106</i>	<i>6.3e+2:165</i>	<i>2.5e+2:489</i>	<i>2.5e+1:2987</i>	15/15
CMA-CSA	<b>2.9</b> (1)	2.4(0.8)	2.7(1)	1.7(0.3)	<b>1.1</b> (0.8)	15/15
CMA-MSR	3.5(2)	2.2(0.2)	2.1(0.5)	1.2(0.3)	6.7(4)	15/15
CMA-TPA	3.4(1)	<b>2.0</b> (0.2)	<b>1.8</b> (0.4)	<b>1.1</b> (0.2)	10(30)	15/15

Table 129: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_8$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f8</b>	<i>1.0e+5:85</i>	<i>6.3e+4:111</i>	<i>4.0e+4:125</i>	<i>2.5e+3:430</i>	<i>6.3e+1:2106</i>	15/15
CMA-CSA	3.4(1)	3.2(0.3)	3.4(0.7)	1.9(0.2)	3.3(8)	15/15
CMA-MSR	3.4(0.9)	3.1(0.8)	3.1(0.5)	1.7(0.2)	3.3(4)	15/15
CMA-TPA	<b>2.6</b> (0.6)	<b>2.2</b> (0.5) <sup>*2</sup>	<b>2.3</b> (0.3) <sup>*2</sup>	<b>1.3</b> (0.1) <sup>*3</sup>	<b>1.4</b> (3)	15/15

Table 130: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_9$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f9</i></b>	<i>2.5e+2:676</i>	<i>1.6e+2:865</i>	<i>1.0e+2:1397</i>	<i>6.3e+1:1896</i>	<i>4.0e+1:2180</i>	15/15
CMA-CSA	2.1(0.3)	1.9(0.3)	1.6(0.4)	2.2(8)	2.2(4)	15/15
CMA-MSR	2.1(0.5)	1.9(0.5)	1.7(1)	2.5(5)	2.4(8)	15/15
CMA-TPA	<b>1.5(0.6)*</b>	<b>1.5(1)</b>	<b>1.1(0.6)</b>	<b>0.91(0.5)*</b>	<b>0.98(0.3)*</b>	15/15

Table 131: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{10}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f10</b>	<i>1.0e+7:44</i>	<i>6.3e+6:80</i>	<i>2.5e+6:126</i>	<i>2.5e+5:408</i>	<i>6.3e+3:2376</i>	15/15
CMA-CSA	1.5(0.3)	1.7(0.9)	5.3(2)	6.1(1)	4.2(0.7)	15/15
CMA-MSR	1.8(2)	<b>1.6</b> (0.7)	<b>2.3</b> (0.9)	<b>3.2</b> (1)	<b>3.2</b> (0.6)	15/15
CMA-TPA	<b>1.4</b> (1)	2.0(1)	2.7(0.4)	3.3(0.9)	3.3(0.7)	15/15

Table 132: 40-D, running time excess  $ERT/ERT_{\text{best 2009}}$  on  $f_{11}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $ERT_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-

Table 133: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{12}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f12</b>	<i>2.5e+8:54</i>	<i>1.6e+8:218</i>	<i>1.0e+8:284</i>	<i>1.0e+7:424</i>	<i>4.0e+1:2479</i>	15/15
CMA-CSA	<b>4.7</b> (2)	1.7(0.4)	1.7(0.2)	2.2(0.1)	<b>1.5</b> (0.1)	15/15
CMA-MSR	5.6(2)	1.8(0.5)	1.7(0.5)	2.2(0.3)	2.2(2)	15/15
CMA-TPA	4.8(2)	<b>1.5</b> (0.5)	<b>1.4</b> (0.3)	<b>1.7</b> (0.4) <sup>*2</sup>	1.9(2)	15/15

Table 134: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{13}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f13</b>	<i>2.5e+3:85</i>	<i>1.6e+3:121</i>	<i>1.6e+3:121</i>	<i>6.3e+1:429</i>	<i>1.0e+1:2029</i>	15/15
CMA-CSA	2.3(0.6)	3.7(0.6)	3.7(0.3)	5.0(0.6)	2.5(2)	15/15
CMA-MSR	2.4(0.8)	3.4(0.5)	3.4(0.5)	4.5(0.3)	2.8(3)	15/15
CMA-TPA	<b>2.2</b> (0.5)	<b>2.9</b> (0.5)	<b>2.9</b> (0.6)	<b>3.8</b> (0.4) <sup>*3</sup>	<b>2.3</b> (3)	15/15

Table 135: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{14}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f14</b>	<i>6.3e+1:34</i>	<i>4.0e+1:137</i>	<i>2.5e+1:176</i>	<i>4.0e+0:438</i>	<i>1.0e-3:2207</i>	15/15
CMA-CSA	<b>4.1</b> (1)	2.2(0.6)	3.0(0.4)	2.7(0.4)	3.6(0.2)	15/15
CMA-MSR	5.7(2)	2.3(0.5)	2.5(0.7)	2.2(0.4)	<b>2.5</b> (0.3)	15/15
CMA-TPA	6.0(1)	<b>2.1</b> (0.6)	<b>2.3</b> (0.6)	<b>2.1</b> (0.2)	2.6(0.1)	15/15



Table 136: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{15}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f15</b>	<i>1.0e+3:192</i>	<i>6.3e+2:458</i>	<i>4.0e+2:1170</i>	<i>2.5e+2:3875</i>	<i>2.5e+2:3875</i>	15/15
CMA-CSA	1.5(0.4)	1.1(0.3)	1.1(0.2)	1.0(0.2)	1.0(0.2)	15/15
CMA-MSR	1.4(0.6)	0.98(0.3)	<b>0.73</b> (0.1)	<b>0.30</b> (0.0) <sup>*4</sup>	<b>0.30</b> (0.0) <sup>*4</sup>	15/15
CMA-TPA	<b>1.2</b> (0.3)	<b>0.88</b> (0.2)	0.92(0.7)	0.57(0.1)	0.57(0.2)	15/15

Table 137: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{16}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f16</b>	<i>4.0e+1:117</i>	<i>2.5e+1:297</i>	<i>1.6e+1:4010</i>	<i>1.6e+1:4010</i>	<i>1.0e+1:5244</i>	15/15
CMA-CSA	25(17)	14(3)	1.2(0.3)	1.2(0.1)	1.0(0.5)	15/15
CMA-MSR	<b>2.4</b> (0.4) <sup>*4</sup>	<b>1.6</b> (0.4) <sup>*4</sup>	<b>0.17</b> (0.0) <sup>*4</sup>	<b>0.17</b> (0.0) <sup>*4</sup>	<b>0.43</b> (0.1) <sup>*2</sup>	15/15
CMA-TPA	11(4)	5.3(1)	0.48(0.1)	0.48(0.1)	1.3(1)	15/15

Table 138: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{17}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f17</b>	<i>1.6e+1:54</i>	<i>1.0e+1:399</i>	<i>6.3e+0:688</i>	<i>4.0e+0:1115</i>	<i>1.0e+0:4220</i>	15/15
CMA-CSA	5.4(3)	1.3(0.6)	1.1(0.3)	1.0(0.3)	<b>0.56</b> (0.1)	15/15
CMA-MSR	3.9(2)	0.96(0.3)	1.1(0.5)	9.1(4)	7.3(7)	15/15
CMA-TPA	<b>3.8</b> (1)	<b>0.93</b> (0.3)	<b>0.99</b> (0.3)	<b>1.0</b> (0.4)	5.0(9)	15/15

Table 139: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{18}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f18</b>	<i>6.3e+1:55</i>	<i>4.0e+1:329</i>	<i>4.0e+1:329</i>	<i>2.5e+1:579</i>	<i>6.3e+0:2006</i>	15/15
CMA-CSA	3.4(2)	1.2(0.4)	1.2(0.2)	1.2(0.3)	<b>0.97</b> (0.4)	15/15
CMA-MSR	3.2(0.9)	0.99(0.4)	0.99(0.2)	1.00(0.6)	10(15)	15/15
CMA-TPA	<b>2.7</b> (1)	<b>0.89</b> (0.2)	<b>0.89</b> (0.2)	<b>0.86</b> (0.4)	1.6(3)	15/15

Table 140: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{19}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f19</b>	<i>1.6e-1:8.6e5</i>	<i>1.0e-1:1.4e6</i>	<i>6.3e-2:3.1e6</i>	<i>4.0e-2:5.2e6</i>	<i>2.5e-2:8.7e6</i>	15/15
CMA-CSA	<b>1.2</b> (0.7)	<b>1.0</b> (0.6)	<b>0.56</b> (0.4)	<b>0.54</b> (0.2)	<b>0.66</b> (0.7)	9/15
CMA-MSR	1.8(0.9)	1.4(0.7)	0.76(0.3)	0.75(0.9)	1.3(2)	5/15
CMA-TPA	1.2(0.6)	1.0(0.2)	0.60(0.2)	0.62(0.4)	0.74(0.4)	8/15

Table 141: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{20}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f20</i></b>	<i>2.5e+4</i> :83	<i>1.6e+4</i> :86	<i>1.0e+3</i> :125	<i>2.5e+0</i> :515	<i>1.6e+0</i> :5582	15/15
CMA-CSA	4.4(0.8)	4.9(0.7)	5.6(0.9)	5.2(0.7)	<b>57</b> <sup>(24)*2</sup>	15/15
CMA-MSR	3.8(0.7)	4.2(0.7)	4.6(0.8)	2.6(0.2)	<i>∞ 3e6</i>	0/15
CMA-TPA	<b>3.1</b> (0.4)*	<b>3.4</b> (0.5)*2	<b>3.7</b> (0.5)*2	<b>2.3</b> (0.2)	9480(1e4)	1/15

Table 142: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{21}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f21</b>	<i>6.3e+1:160</i>	<i>4.0e+1:305</i>	<i>2.5e+1:380</i>	<i>1.6e+1:784</i>	<i>6.3e+0:2510</i>	30/30
CMA-CSA	2.8(0.5)	1.9(0.4)	1.8(0.5)	<b>1.1</b> (0.6)	2.4(3)	15/15
CMA-MSR	2.2(0.7)	1.5(0.4)	<b>1.6</b> (0.5)	2.9(0.1)	96(4)	14/15
CMA-TPA	<b>2.0</b> (0.2)	<b>1.4</b> (0.2)	2.9(13)	2.2(3)	<b>2.0</b> (4)	15/15

Table 143: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{22}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b><i>f22</i></b>	<i>6.3e+1</i> :160	<i>4.0e+1</i> :231	<i>2.5e+1</i> :687	<i>1.6e+1</i> :1392	<i>1.0e+1</i> :3090	15/15
CMA-CSA	2.9(1)	9.1(25)	4.2(9)	57(205)	87(211)	14/15
CMA-MSR	5.8(12)	<b>4.5</b> (0.9)	347(2415)	172(2)	77(0.8)	14/15
CMA-TPA	<b>2.4</b> (0.3)	7.2(0.3)	<b>3.2</b> (3)	<b>3.0</b> (7)	<b>1.6</b> (1)	15/15



Table 144: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{23}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f23</b>	<i>6.3e+0:68</i>	<i>4.0e+0:292</i>	<i>2.5e+0:603</i>	<i>2.5e+0:603</i>	<i>1.6e+0:2487</i>	15/15
CMA-CSA	12(6)	72(51)	108(79)	108(121)	27(11)	15/15
CMA-MSR	<b>7.0</b> (3)	<b>2.5</b> (0.2) <sup>*4</sup>	<b>1.4</b> (0.2) <sup>*4</sup>	<b>1.4</b> (0.2) <sup>*4</sup>	<b>0.41</b> (0.1) <sup>*4</sup>	15/15
CMA-TPA	12(6)	85(213)	86(205)	86(114)	27(51)	15/15

Table 145: 40-D, running time excess  $\text{ERT}/\text{ERT}_{\text{best 2009}}$  on  $f_{24}$  for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding  $\text{ERT}_{\text{best 2009}}$  (preceded by the target  $\Delta f$ -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with  $p = 0.05$  or  $p = 10^{-k}$  when the number  $k$  following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<b>f24</b>	<i>4.0e+2</i> :1404	<i>2.5e+2</i> :17825	<i>1.6e+2</i> :18980	<i>1.0e+2</i> :38677	<i>6.3e+1</i> :1.6e5	15/15
CMA-CSA	0.98(0.4)	1.4(0.9)	1.4(2)	1.2(0.5)	0.80(0.6)	15/15
CMA-MSR	<b>0.63</b> (0.1)	<b>0.07</b> (4e-3) <sup>*4</sup>	<b>0.43</b> (0.4)	<b>0.47</b> (0.2)	<b>0.31</b> (0.1)	15/15
CMA-TPA	0.76(0.4)	0.48(0.3)	0.48(0.3)	0.68(0.4)	0.60(0.5)	15/15

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