

Bounding the population size of IPOP-CMA-ES  
on the Noiseless BBOB Testbed  
+ Testing impact of tuning  
+ Expensive optimization scenarios

Tianjun Liao and Thomas Stützle

IRIDIA, CoDE, Université Libre de Bruxelles (ULB)

## bounding population size

- IPOP-CMA-ES increases population size exponentially
- Question: are very large population useful?
- particular motivation:
  - Chen et al., 2012: large pop. size can be unhelpful in EAs
  - Wessing et al., 2011: when parameter tuning actually is parameter control

↳ examine bounds on maximum population size

## bounding population size

- IPOP-CMA-ES increases population size exponentially
- Question: are very large population useful?
- particular motivation:
  - Chen et al., 2012: large pop. size can be unhelpful in EAs
  - Wessing et al., 2011: when parameter tuning actually is parameter control

↳ examine bounds on maximum population size

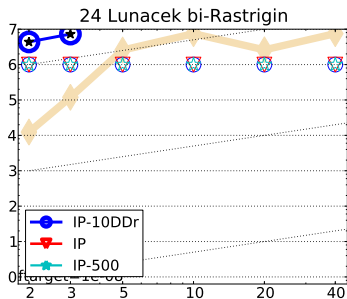
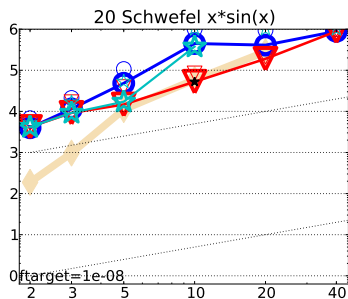
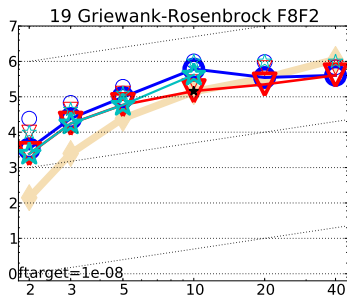
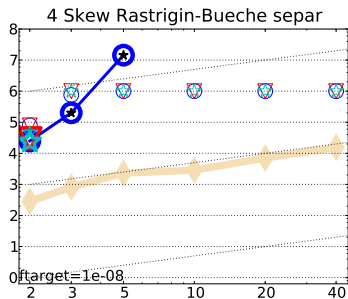
## tuning, expensive

- tuning incurs only very light effort (in our case here)
- expensive functions: different look at data

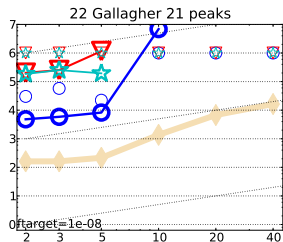
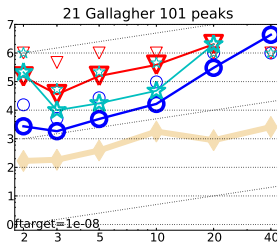
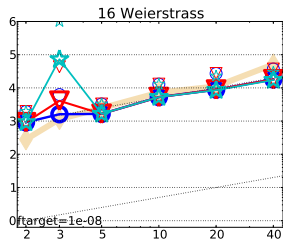
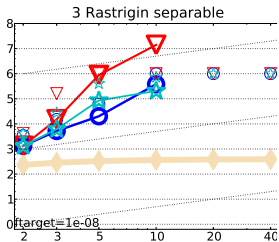
## Experimental setup

- IPOP-CMA-ES default version (C version, 10/16/10), modified to clamp bounds and limit maximum pop. size
- Recall pop-size settings of IPOP-CMA-ES
  - initial:  $\lambda = 4 + \lfloor 3 \ln(D) \rfloor$
  - restart:  $\lambda = 2 \cdot \lambda \mapsto \lambda_j = 2^j \cdot \lambda_0$
- population size bounds (limited experience, ad hoc)
  - fixed maximum to 500
  - dimension-dependent maximum of  $10D^2$
- once maximum is reached, restart scheme at initial value

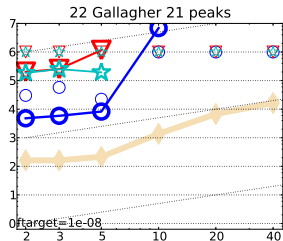
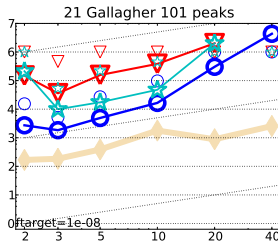
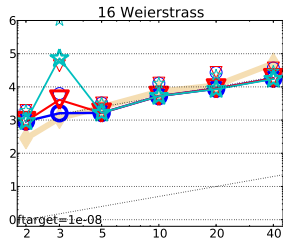
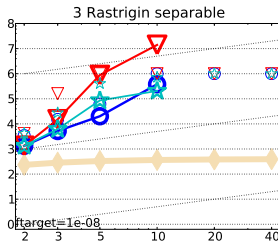
# Significant differences ERT



# "Visible" differences



# “Visible” differences



On many functions population-size bounds too loose to make an effect (apparently  $f_1, f_2, f_4 - f_{15}, f_{17}, f_{18}$ )

## Tuning setup

- use  $D = 10$  functions from SOCO special issue
- removed Sphere, Rosenbrock, Rastrigin, Schwefel 1.2 from SOCO set *error :-( Schaffer, f17*
- default version of `irace`
- tuning budget: 5000 runs of IPOP-CMA-ES each of  $100D = 1000$  function evaluations
- short runs because same tuned version is used for expensive scenario
- measured cost function: evaluation function value at end of trial



## Tuning setup

- use  $D = 10$  functions from SOCO special issue
- removed Sphere, Rosenbrock, Rastrigin, Schwefel 1.2 from SOCO set *error :-( Schaffer, f17*
- default version of irace
- tuning budget: 5000 runs of IPOP-CMA-ES each of  $100D = 1000$  function evaluations
- short runs because same tuned version is used for expensive scenario
- measured cost function: evaluation function value at end of trial

*we are aware: wrong target for BBOB, not many parameters tuned, maybe wrong algorithm overall, etc.*

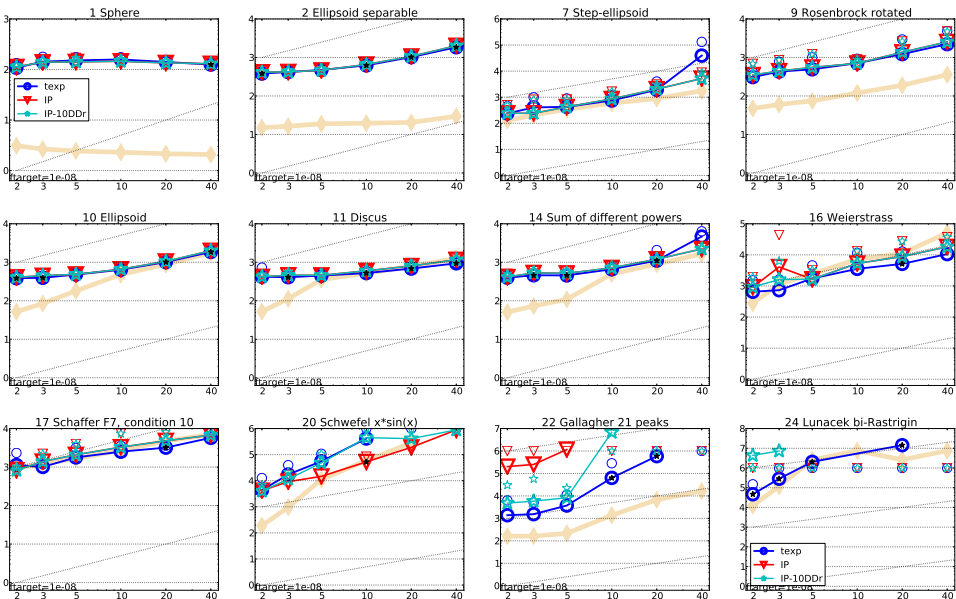
Parameter	Internal parameter	default	tuned
$a$	Init pop size: $\lambda_0 = 4 + \lfloor a \ln(D) \rfloor$	3	2.675
$b$	Parent size: $\mu = \lfloor \lambda/b \rfloor$	2	1.351
$c$	Init step size: $\sigma_0 = c \cdot (B - A)$	0.5	0.102
$d$	IPOP factor: $ipop = d$	2	2.88
$e$	$stopTolFun = 10^e$	-12	-8.607
$f$	$stopTolFunHist = 10^f$	-20	-14.77
$g$	$stopTolX = 10^g$	-12	-9.529

Parameter	Internal parameter	default	tuned
$a$	Init pop size: $\lambda_0 = 4 + \lfloor a \ln(D) \rfloor$	3	2.675
$b$	Parent size: $\mu = \lfloor \lambda/b \rfloor$	2	1.351
$c$	Init step size: $\sigma_0 = c \cdot (B - A)$	0.5	0.102
$d$	IPOP factor: $ipop = d$	2	2.88
$e$	$stopTolFun = 10^e$	-12	-8.607
$f$	$stopTolFunHist = 10^f$	-20	-14.77
$g$	$stopTolX = 10^g$	-12	-9.529

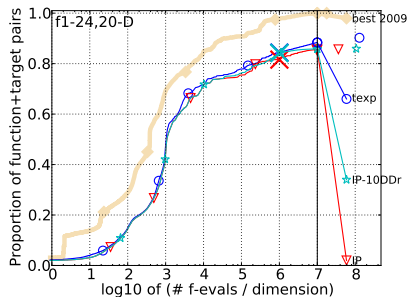
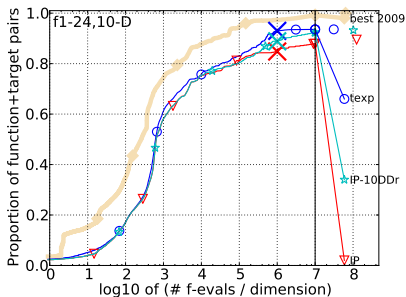
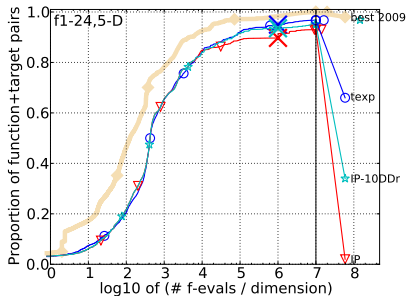
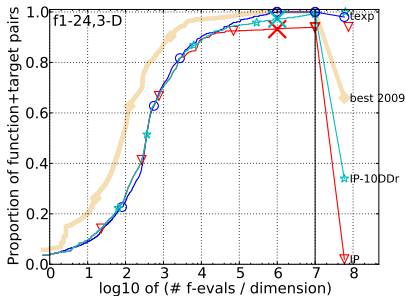
Following comparison

- default IPOP-CMA-ES
- IPOP-CMA-ES with pop. size bound  $10D^2$
- IPOP-CMA-ES with pop. size bound  $10D^2$ , tuned

# Significant differences ERT



# General scenario



*no changes, same algorithm (tuned IPOP-CMA-ES with maximum population size bound (here not effective))*

*no changes, same algorithm (tuned IPOP-CMA-ES with maximum population size bound (here not effective))*

*just a different look at the same data*

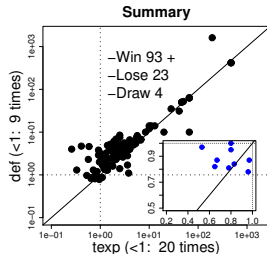
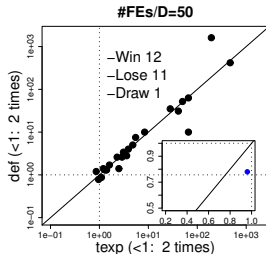
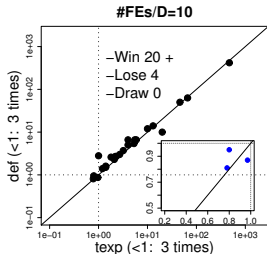
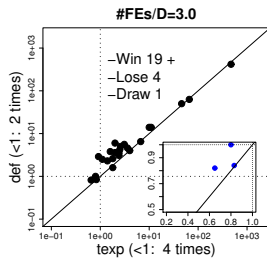
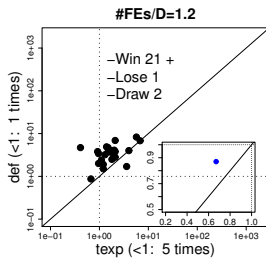
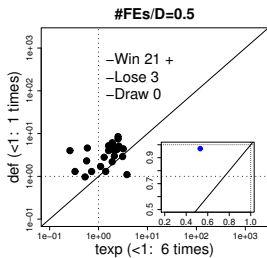
*no changes, same algorithm (tuned IPOP-CMA-ES with maximum population size bound (here not effective))*

*just a different look at the same data*

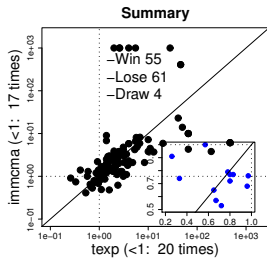
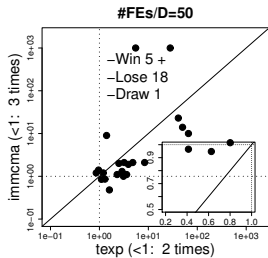
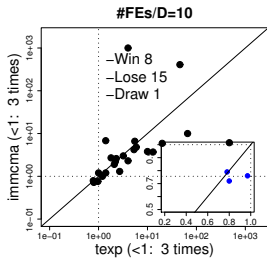
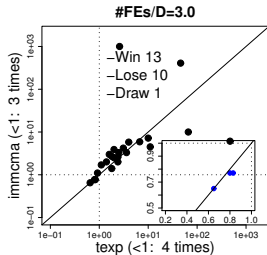
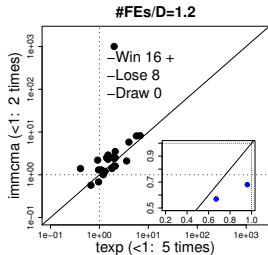
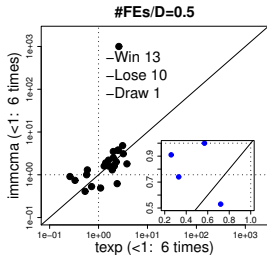
*Motivation: direct search may not be so bad after all . . .*



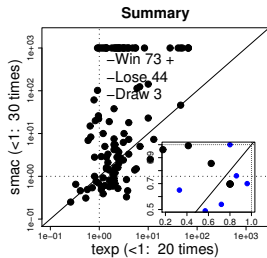
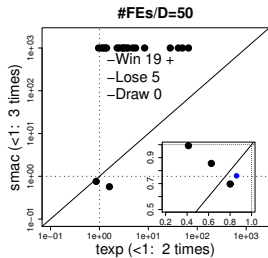
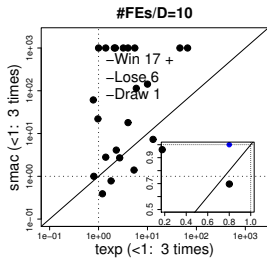
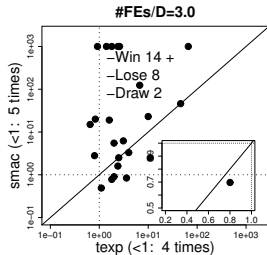
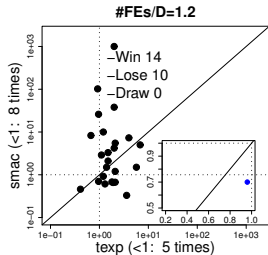
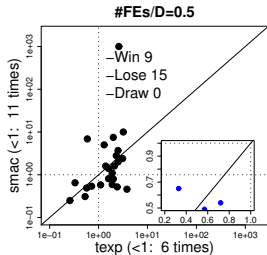
# Expensive scenario, comparison to default IPOP-CMA-ES



# Expensive scenario, comparison to ImmCMA-ES



# Expensive scenario, comparison to SMAC-BBOB



- limiting max. population size of IPOP-CMA-ES can help
- tuning can further improve performance
  - main differences on weakly structured multi-modal functions (also other benchmarks such as CEC'05 / '13)
- IPOP-CMA-ES anyway rather robust