

Comparison Tables: CEC BBOB 2015 Testbed in 20-D (Expensive Setting)

The BBOBies

May 27, 2015

Abstract

This document provides tabular results of the special session on Black-Box Optimization Benchmarking at CEC 2015 with a focus on benchmarking black-box algorithms for small function evaluation budgets (“expensive setting”), see <http://coco.gforge.inria.fr/doku.php?id=cec-bbob-2015>. Overall, eight algorithms have been tested on 24 benchmark functions in dimensions between 2 and 20. A description of the used objective functions can be found in [6, 4]. The experimental set-up is described in [5].

The performance measure provided in the following tables is the expected number of objective function evaluations to reach a given target function value (ERT, expected running time), divided by the respective value for the best algorithm in BBOB-2009 (see [1]) if an algorithm from BBOB-2009 reached the given target function value. The ERT value is given otherwise (ERT_{best} is noted as infinite). See [5] for details on how ERT is obtained. Bold entries in the table correspond to values below 3 or the top-three best values. Table 1 gives an overview on all algorithms submitted to the noise-free testbed at CEC 2015.

Table 1: Names and references of all algorithms submitted for the noise-free testbed

algorithm name	short	paper	reference
MATSuMoTo		Comparison of the MATSuMoTo Library for Expensive Optimization on the Noiseless Black-Box Optimization Benchmarking Testbed	[2]
R-DE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-DE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-SHADE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
R-SHADE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
RL-SHADE-10e2		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
RL-SHADE-10e5		Parameter Tuning for Differential Evolution for Cheap, Medium, and Expensive Computational Budgets	[7]
SOO		Simultaneous Optimistic Optimization on the Noiseless BBOB Testbed	[3]

Table 2: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_1 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

↻

#FEs/D	0.5	1.2	3	10	50	#succ
f1	<i>6.3e+1:24</i>	<i>4.0e+1:42</i>	<i>1.0e-8:43</i>	<i>1.0e-8:43</i>	<i>1.0e-8:43</i>	15/15
MATSUMOTO-	2.5 _(0.3)	2.0 _{(0.3)⁺²}	∞	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	3.7 ₍₂₎	3.2 ₍₁₎	∞	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	10 ₍₃₎	10 ₍₁₎	230 ₍₆₎	230 ₍₅₎	230 ₍₆₎	15/15
RL-SHADE-1	11 _(0.5)	7.1 _(0.8)	∞	∞	∞ <i>2000</i>	0/15
RL-SHADE-1	53 ₍₁₇₎	47 ₍₁₅₎	1041 ₍₁₅₎	1041 ₍₁₇₎	1041 ₍₁₀₎	15/15
R-SHADE-10	6.8 ₍₃₎	5.5 ₍₁₎	∞	∞	∞ <i>2000</i>	0/15
R-SHADE-10	12 ₍₄₎	12 ₍₃₎	294 ₍₁₈₎	294 ₍₂₀₎	294 ₍₃₂₎	15/15
SOO-Derbel	3.6 ₍₂₎	4.3 ₍₁₎	1042 ₍₂₃₎	1042 ₍₂₆₎	1042 ₍₁₉₎	15/15

Table 3: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_2 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f2	<i>4.0e+6:29</i>	<i>2.5e+6:42</i>	<i>1.0e+5:65</i>	<i>1.0e+4:207</i>	<i>1.0e-8:412</i>	15/15
MATSUMOTO	0.79 ₍₁₎	1.3 ₍₁₎	9.3 ₍₆₎	71 ₍₁₄₅₎	∞ 1000	0/15
R-DE-10e2-	0.87 _(0.8)	0.95 _(0.3)	3.8 ₍₂₎ * ²	2.6 ₍₁₎	∞ 2000	0/15
R-DE-10e5-	1.4 ₍₂₎	2.0 ₍₂₎	12 ₍₂₎	6.9 _(0.7)	32 _(0.9)	15/15
RL-SHADE-1	1.3 ₍₁₎	1.3 ₍₂₎	6.1 ₍₁₎	4.2 ₍₂₎	∞ 2000	0/15
RL-SHADE-1	1.5 ₍₁₎	3.0 ₍₁₎	85 ₍₁₀₎	61 ₍₄₎	152 ₍₂₎	15/15
R-SHADE-10	1.9 ₍₂₎	2.0 ₍₁₎	6.2 ₍₁₎	3.6 _(0.3)	∞ 2000	0/15
R-SHADE-10	1.0 ₍₁₎	2.1 ₍₁₎	16 ₍₃₎	10 ₍₂₎	44 ₍₂₎	15/15
SOO-Derbel	8.8 ₍₃₎	12 ₍₁₂₎	43 ₍₉₎	24 ₍₇₎	3.3e4 _(2e4)	2/15

Table 4: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_3 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f3	<i>6.3e+2:33</i>	<i>4.0e+2:44</i>	<i>1.6e+2:109</i>	<i>1.0e+2:255</i>	<i>2.5e+1:3277</i>	15/15
MATSUMOTO-	1.9 _(0.6)	2.5 _(0.7)	8.0 ₍₅₎	10 ₍₉₎	∞ <i>1000</i>	0/15
R-DE-10e2-	1.4 _(0.9)	2.5 ₍₁₎	5.4 ₍₉₎	4.3 ₍₁₎	9.1 ₍₁₃₎	1/15
R-DE-10e5-	4.3 ₍₂₎	6.8 ₍₂₎	10 ₍₂₎	8.7 ₍₃₎	2.8 _(0.6)	15/15
RL-SHADE-1	5.2 ₍₃₎	6.4 _(0.6)	5.1 ₍₃₎	5.9 ₍₅₎	8.9 ₍₁₀₎	1/15
RL-SHADE-1	10 ₍₇₎	36 ₍₈₎	75 ₍₁₁₎	91 ₍₂₂₎	28 ₍₂₎	15/15
R-SHADE-10	2.8 ₍₂₎	4.0 ₍₁₎	5.2 _(0.4)	3.9 _(0.7)	3.0 ₍₅₎	3/15
R-SHADE-10	3.8 ₍₃₎	7.7 ₍₂₎	20 ₍₈₎	33 ₍₆₎	7.7 _(0.6)	15/15
SOO-Derbel	5.0 ₍₃₎	5.8 ₍₂₎	12 ₍₅₎	12 ₍₃₎	234 ₍₆₅₅₎	12/15

Table 5: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_4 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f_4	<i>6.3e+2:22</i>	<i>4.0e+2:91</i>	<i>2.5e+2:250</i>	<i>1.6e+2:332</i>	<i>6.3e+1:1927</i>	15/15
MATSUMOTO	7.6(8)	5.1(4)	10(7)	∞	∞ 1000	0/15
R-DE-10e2-	4.4 (3)	2.0 (0.4)	1.5 (0.4)*	2.2 (0.7)	∞ 2000	0/15
R-DE-10e5-	13(4)	6.1(0.8)	4.0(0.4)	5.0(1)	2.6 (0.3)	15/15
RL-SHADE-1	12(2)	3.6(0.5)	1.9 (0.4)	4.2(3)	7.4(10)	2/15
RL-SHADE-1	40(19)	30(3)	25(3)	38(6)	29(3)	15/15
R-SHADE-10	7.9(2)	3.2(0.5)	2.1 (0.3)	2.4 (0.5)	0.84 (0.1)	15/15
R-SHADE-10	11(4)	6.6(2)	5.5(0.8)	13(3)	9.0(1)	15/15
SOO-Derbel	1.1 (2)*	2.7 (0.8)	3.9(3)	7.0(1.0)	47(1)	15/15

Table 6: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_5 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f5	<i>2.5e+2</i> :19	<i>1.6e+2</i> :34	<i>1.0e-8</i> :41	<i>1.0e-8</i> :41	<i>1.0e-8</i> :41	15/15
MATSUMOTO	1.8 (0.6)	1.3 (0.1) ^{*4}	2.4 (0.1) ^{*4}	2.4 (1) ^{*4}	2.4 (0.1) ^{*4}	15/15
R-DE-10e2-	2.2 (0.7)	3.1 (0.8)	∞	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	4.3(3)	10(2)	332(7)	332(5)	332(8)	15/15
RL-SHADE-1	6.3(5)	7.9(0.5)	242 (173)	242 (333)	242 (209)	3/15
RL-SHADE-1	8.0(23)	57(13)	1574(45)	1574(34)	1574(44)	15/15
R-SHADE-10	3.5(3)	4.8(0.6)	∞	∞	∞ <i>2000</i>	0/15
R-SHADE-10	6.1(5)	19(4)	959(45)	959(33)	959(31)	15/15
SOO-Derbel	10(0.0)	8.7(0.0)	4928(0.0)	4928(0.0)	4928(0.0)	15/15

Table 7: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_6 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

∞

#FEs/D	0.5	1.2	3	10	50	#succ
f6	<i>2.5e+5:16</i>	<i>6.3e+4:43</i>	<i>1.6e+4:62</i>	<i>1.6e+2:353</i>	<i>1.6e+1:1078</i>	15/15
MATSUMOTO	2.4 (0.2)	1.4 (0.4)	1.4 (0.7)*	9.5(21)	∞ 1000	0/15
R-DE-10e2-	2.9 (2)	2.2 (1)	2.4 (1)	3.4 (2)	27(44)	1/15
R-DE-10e5-	6.8(7)	7.2(5)	8.8(2)	4.9(1.0)	12 (3)	15/15
RL-SHADE-1	8.0(9)	6.3(1)	5.1(1)	3.9(2)	∞ 2000	0/15
RL-SHADE-1	16(22)	32(19)	36(23)	19(5)	20(0.7)	15/15
R-SHADE-10	4.0(3)	4.0(2)	4.1(2)	2.5 (1)	∞ 2000	0/15
R-SHADE-10	7.7(10)	9.0(7)	11(6)	4.3(1)	4.3 (0.4)	15/15
SOO-Derbel	2.9 (3)	4.2(3)	5.3(2)	6.9(3)	1.3e4(2e4)	2/15

Table 8: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_7 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f_7	<i>1.0e+3:11</i>	<i>4.0e+2:39</i>	<i>2.5e+2:74</i>	<i>6.3e+1:319</i>	<i>1.0e+1:1351</i>	15/15
MATSUMOTO	1.2 (2)	2.2 (2)	2.0 (0.5)	5.6(6)	∞ 1000	0/15
R-DE-10e2-	1.9 (1)	2.1 (1)	2.0 (2)	3.0 (2)	11 (6)	2/15
R-DE-10e5-	1.9 (3)	4.9(3)	5.0(3)	5.0(2)	12(6)	15/15
RL-SHADE-1	2.0 (4)	5.6(1)	4.1(0.3)	3.5(6)	∞ 2000	0/15
RL-SHADE-1	2.5 (2)	22(1.6)	25(3)	22(6)	11(0.5)	15/15
R-SHADE-10	2.1 (2)	3.0(1)	3.2(2)	2.2 (0.7)	11(7)	2/15
R-SHADE-10	3.4(5)	4.5(2)	5.2(1)	3.1(0.4)	2.0 (0.7)	15/15
SOO-Derbel	1.3 (0.5)	2.0 (1)	1.9 (1)	5.7(5)	59(85)	15/15

Table 9: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_8 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f8	<i>4.0e+4:19</i>	<i>2.5e+4:35</i>	<i>4.0e+3:67</i>	<i>2.5e+2:231</i>	<i>1.6e+1:1470</i>	15/15
MATSUMOTO-	4.5 (1)	2.9 (0.8)	3.3 (1)	4.0 (7)	∞ 1000	0/15
R-DE-10e2-	5.1(1)	3.6 (1)	4.7 (1)	6.9(2)	∞ 2000	0/15
R-DE-10e5-	15(5)	11(2)	12(3)	9.1(2)	51(5)	15/15
RL-SHADE-1	14(2)	8.2(0.9)	7.2(2)	22(20)	∞ 2000	0/15
RL-SHADE-1	67 (28)	50(14)	61(11)	48(4)	22(3)	15/15
R-SHADE-10	8.6(2)	5.4(1)	5.8(1)	3.5 (1)	20 (25)	1/15
R-SHADE-10	16(5)	9.3(3)	12(3)	8.3(1)	7.0 (3)	15/15
SOO-Derbel	3.8 (5)	4.5(5)	8.2(6)	12(4)	2107(3738)	6/15

Table 10: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_9 for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f9	<i>1.0e+2:357</i>	<i>6.3e+1:560</i>	<i>4.0e+1:684</i>	<i>2.5e+1:756</i>	<i>1.0e+1:1716</i>	15/15
MATSUMOTO-	7.9(9)	∞	∞	∞	∞ 1000	0/15
R-DE-10e2-	7.0(3)	12(15)	14(12)	19(19)	∞ 2000	0/15
R-DE-10e5-	20(7)	18(6)	16(7)	16(3)	3022(3021)	5/15
RL-SHADE-1	20(48)	∞	∞	∞	∞ 2000	0/15
RL-SHADE-1	37(2)	26(2)	24(1)	25(1)	33 (2)	15/15
R-SHADE-10	5.3 (3)	4.2 (4)	5.3 (4)	6.1 (5)	∞ 2000	0/15
R-SHADE-10	5.7 (0.5)	4.3 (0.3)	4.1 (0.4)	4.6 (0.3)	16 (2)	15/15
SOO-Derbel	10(3)	11(3)	15(5)	21(6)	5000(4642)	3/15

Table 11: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_{10} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f10	<i>1.6e+6:15</i>	<i>1.0e+6:27</i>	<i>4.0e+5:70</i>	<i>6.3e+4:231</i>	<i>4.0e+3:1015</i>	15/15
MATSUMOTO-	4.4 (1)	3.1 (1)	3.4 (8)	9.1(8)	∞ 1000	0/15
R-DE-10e2-	4.6(4)	4.2(0.8)	4.1 (2)	12(13)	∞ 2000	0/15
R-DE-10e5-	9.2(11)	10(6)	12(9)	70(21)	∞ 2e6	0/15
RL-SHADE-1	12(4)	8.9(1)	5.9(3)	10(9)	∞ 2000	0/15
RL-SHADE-1	32(15)	31(15)	38(12)	57(8)	20 (2)	15/15
R-SHADE-10	6.9(3)	5.8(2)	5.8(3)	5.6 (2)	29(27)	1/15
R-SHADE-10	10(6)	8.8(4)	8.0(2)	6.4 (1.0)	3.8 (2)	15/15
SOO-Derbel	2.9 (4)	3.1 (2)	4.8(4)	14(12)	1743(1348)	10/15

Table 12: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{11} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f11	<i>4.0e+4</i> :11	<i>2.5e+3</i> :27	<i>1.6e+2</i> :313	<i>1.0e+2</i> :481	<i>1.0e+1</i> :1002	15/15
MATSUMOTO	1.7 ^(0.7)	2.5 ⁽²⁾	21 ⁽¹⁷⁾	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	1.7 ⁽¹⁾	2.0 ⁽¹⁾	13 ⁽¹⁰⁾	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	1.7 ^(1.0)	2.2 ⁽²⁾	11 ⁽¹¹⁾	51 ⁽⁸³⁾	∞ <i>2e6</i>	0/15
RL-SHADE-1	2.1 ⁽⁴⁾	3.8 ⁽²⁾	11 ⁽²³⁾	60 ⁽⁵²⁾	∞ <i>2000</i>	0/15
RL-SHADE-1	1.9 ⁽²⁾	3.4 ⁽²⁾	14 ⁽¹²⁾	22 ⁽¹⁷⁾	27 ⁽²⁾	15/15
R-SHADE-10	1.6 ⁽¹⁾	1.6 ^(0.8)	10 ⁽⁷⁾	61 ⁽³¹⁾	∞ <i>2000</i>	0/15
R-SHADE-10	1.8 ⁽¹⁾	2.6 ⁽²⁾	2.3 ⁽¹⁾	2.9 ⁽¹⁾	7.6 ⁽⁶⁾	15/15
SOO-Derbel	1.4 ^(1.0)	2.0 ⁽²⁾	11 ^(0.9)	343 ⁽¹⁴³⁰⁾	∞ <i>2e6</i>	0/15

Table 13: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{12} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f12	<i>1.0e+8:23</i>	<i>6.3e+7:39</i>	<i>2.5e+7:76</i>	<i>4.0e+6:209</i>	<i>1.0e+1:1042</i>	15/15
MATSUMOTO-	3.1 (0.7)	2.9 (0.4)	3.0 (0.5)	3.6(3)	∞ 1000	0/15
R-DE-10e2-	3.1 (2)	3.1 (2)	3.3 (1)	3.0 (2)	∞ 2000	0/15
R-DE-10e5-	9.4(4)	8.1(2)	9.5(2)	7.1(0.5)	31 (36)	15/15
RL-SHADE-1	11(1)	7.5(0.8)	5.0(0.4)	6.1(7)	∞ 2000	0/15
RL-SHADE-1	37(19)	38(16)	44(7)	44(6)	37(9)	15/15
R-SHADE-10	7.8(2)	6.3(2)	5.0(1)	3.2 (0.5)	∞ 2000	0/15
R-SHADE-10	11(5)	9.1(3)	10(3)	8.1(1)	8.5 (0.7)	15/15
SOO-Derbel	3.6(5)	5.0(4)	6.0(3)	11(9)	1110(972)	10/15

Table 14: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{13} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f13	<i>1.6e+3:28</i>	<i>1.0e+3:64</i>	<i>6.3e+2:79</i>	<i>4.0e+1:211</i>	<i>2.5e+0:1724</i>	15/15
MATSUMOTO-	2.6 _(0.6)	1.8 _(0.6) ^{*2}	2.6 ₍₂₎ ^{*2}	8.0 ₍₉₎	∞ <i>1000</i>	0/15
R-DE-10e2-	2.9 _(1.0)	3.6 _(0.9)	5.1 _(1.0)	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	7.1 ₍₂₎	7.8 ₍₂₎	12 ₍₂₎	27 ₍₃₎	43 ₍₄₆₎	15/15
RL-SHADE-1	8.8 _(0.7)	5.2 _(0.2)	7.4 _(0.7)	∞	∞ <i>2000</i>	0/15
RL-SHADE-1	30 ₍₁₃₎	41 ₍₅₎	65 ₍₅₎	93 ₍₂₎	18 _(0.5)	15/15
R-SHADE-10	5.5 ₍₂₎	4.8 ₍₁₎	6.2 _(0.6)	11 ₍₃₎	∞ <i>2000</i>	0/15
R-SHADE-10	8.5 ₍₃₎	9.3 ₍₂₎	13 ₍₁₎	21 ₍₄₎	7.4 ₍₅₎	15/15
SOO-Derbel	2.4 ₍₃₎	4.9 ₍₄₎	11 ₍₄₎	1339 ₍₁₈₉₀₎	5103 ₍₄₈₃₀₎	3/15

Table 15: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{14} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f14	<i>2.5e+1:15</i>	<i>1.6e+1:42</i>	<i>1.0e+1:75</i>	<i>1.6e+0:219</i>	<i>6.3e-4:1106</i>	15/15
MATSUMOTO	5.7 (2)	3.1 (1)	2.9 (1)	9.5(11)	∞ 1000	0/15
R-DE-10e2-	7.3(5)	4.5 (1)	4.5 (4)	6.1 (7)	∞ 2000	0/15
R-DE-10e5-	13(7)	10(4)	9.4(4)	9.3(2)	∞ 2e6	0/15
RL-SHADE-1	17(6)	7.7(0.7)	5.8(1)	31(43)	∞ 2000	0/15
RL-SHADE-1	58(27)	45(10)	40(15)	47(4)	30 (1)	15/15
R-SHADE-10	12(5)	6.0(2)	4.8(1)	3.7 (0.6)	∞ 2000	0/15
R-SHADE-10	13(4)	8.4(1)	8.2(2)	9.0(2)	10 (2)	15/15
SOO-Derbel	3.9 (6)	4.7(3)	5.7(3)	34(8)	∞ 2e6	0/15

Table 16: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{15} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f15	<i>6.3e+2:15</i>	<i>4.0e+2:67</i>	<i>2.5e+2:292</i>	<i>1.6e+2:846</i>	<i>1.0e+2:1671</i>	15/15
MATSUMOTO	3.5 (1)	1.7 (0.4)	1.1 (1.0)	2.0 (2)	8.8(12)	1/15
R-DE-10e2-	3.7(2)	2.3 (2)	2.2 (3)	11(12)	∞ 2000	0/15
R-DE-10e5-	7.2(3)	5.0(2)	3.0(0.5)	4.5(3)	32(44)	15/15
RL-SHADE-1	12(4)	4.4(0.4)	1.9 (0.8)	3.2(1)	18(37)	1/15
RL-SHADE-1	16(25)	24(13)	13(3)	13(3)	23(10)	15/15
R-SHADE-10	6.7(4)	3.5(1)	1.6 (0.6)	1.3 (0.4)	2.8 (6)	6/15
R-SHADE-10	7.1(5)	5.2(1)	2.6 (0.5)	2.9 (0.7)	6.3(2)	15/15
SOO-Derbel	1.4 (3)*	2.6 (3)	2.0 (0.8)	3.6(2)	3.2 (0.8)	15/15

Table 17: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{16} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f16	<i>4.0e+1:26</i>	<i>2.5e+1:127</i>	<i>1.6e+1:540</i>	<i>1.6e+1:540</i>	<i>1.0e+1:1384</i>	15/15
MATSUMOTO	3.4(3)	4.9(4)	3.3(2)	3.3(2)	11(15)	1/15
R-DE-10e2-	2.1 (4)	39(29)	∞	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	3.4(3)	18(24)	50(30)	50(50)	236(346)	15/15
RL-SHADE-1	3.8(3)	3.8(1)	2.8 (2)	2.8 (2)	6.8 (13)	3/15
RL-SHADE-1	3.8(5)	38(47)	92(45)	92(22)	73(22)	15/15
R-SHADE-10	1.8 (1)	3.4 (1)	3.2(1)	3.2(3)	22(20)	1/15
R-SHADE-10	4.1(4)	23(16)	23(7)	23(6)	27(21)	15/15
SOO-Derbel	2.3 (3)	3.6 (2)	2.2 (1.0)	2.2 (1)	1.6 (0.4)	15/15

Table 18: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{17} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f17	<i>1.6e+1:11</i>	<i>1.0e+1:63</i>	<i>6.3e+0:305</i>	<i>4.0e+0:468</i>	<i>1.0e+0:1030</i>	15/15
MATSUMOTO	3.3(2)	2.2 (0.6)	1.3 (0.5)	32(46)	∞ 1000	0/15
R-DE-10e2-	2.3 (2)	2.1 (2)	1.7 (0.8)	4.1(2)	∞ 2000	0/15
R-DE-10e5-	4.4(4)	4.1(1.0)	2.7 (1)	4.3(1)	12 (6)	15/15
RL-SHADE-1	5.5(10)	3.9(2)	2.2 (2)	11(6)	∞ 2000	0/15
RL-SHADE-1	4.6(13)	13(8)	10(3)	13(2)	18(2)	15/15
R-SHADE-10	6.0(6)	3.7(1)	1.7 (0.7)	3.3 (2)	29(39)	1/15
R-SHADE-10	5.3(13)	3.7(2)	1.9 (0.9)	2.3 (0.9)	3.4 (0.8)	15/15
SOO-Derbel	0.99 (3)*2	1.3 (0.9)	1.6 (1)	3.5(2)	16(6)	15/15

Table 19: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{18} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f18	<i>4.0e+1:116</i>	<i>2.5e+1:252</i>	<i>1.6e+1:430</i>	<i>1.0e+1:621</i>	<i>4.0e+0:1090</i>	15/15
MATSUMOTO	1.0 _(0.4)	2.4 ₍₅₎	8.3 ₍₁₂₎	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	0.78 _(0.6)	1.2 _(0.7)	2.1 ₍₁₎	8.4 ₍₁₃₎	∞ <i>2000</i>	0/15
R-DE-10e5-	1.8 _(0.7)	2.4 _(0.6)	4.1 ₍₂₎	6.2 ₍₂₎	28 ₍₄₄₎	15/15
RL-SHADE-1	2.0 ₍₁₎	2.2 ₍₃₎	4.2 _(0.7)	11 ₍₁₃₎	∞ <i>2000</i>	0/15
RL-SHADE-1	5.3 ₍₂₎	10 ₍₄₎	13 ₍₂₎	17 ₍₂₎	18 ₍₁₎	15/15
R-SHADE-10	1.4 _(0.6)	2.0 ₍₁₎	3.0 ₍₁₎	5.6 ₍₇₎	28 ₍₄₄₎	1/15
R-SHADE-10	1.8 _(0.6)	2.0 _(0.8)	2.7 _(0.8)	3.1 _(0.7)	3.4 _(0.8)	15/15
SOO-Derbel	0.54 _(0.5)	1.6 ₍₂₎	3.2 ₍₂₎	5.0 ₍₂₎	11 ₍₅₎	15/15

Table 20: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best 2009}}$ on f_{19} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best 2009}}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f19	<i>1.6e-1:2.5e5</i>	<i>1.0e-1:3.4e5</i>	<i>6.3e-2:3.4e5</i>	<i>4.0e-2:3.4e5</i>	<i>2.5e-2:3.4e5</i>	3/15
MATSUMOTO	∞	∞	∞	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	∞	∞	∞	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	∞	∞	∞	∞	∞ <i>2e6</i>	0/15
RL-SHADE-1	∞	∞	∞	∞	∞ <i>2000</i>	0/15
RL-SHADE-1	115 ⁽⁹⁹⁾	∞	∞	∞	∞ <i>2e6</i>	0/15
R-SHADE-10	∞	∞	∞	∞	∞ <i>2000</i>	0/15
R-SHADE-10	55 ⁽⁵⁹⁾	∞	∞	∞	∞ <i>2e6</i>	0/15
SOO-Derbel	0.55 ⁽²⁾	3.2 ⁽³⁾	26 ⁽²⁴⁾	83 ⁽⁹⁵⁾	∞ <i>2e6</i>	0/15

Table 21: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{20} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f_{20}	<i>1.6e+4</i> :38	<i>1.0e+4</i> :42	<i>2.5e+2</i> :62	<i>2.5e+0</i> :250	<i>1.6e+0</i> :2536	15/15
MATSUMOTO	2.2 (0.5)	2.4 (0.9)	4.6 (2)	4.1 (5)	∞ 1000	0/15
R-DE-10e2-	1.9 (0.9)	2.3 (1)	4.9 (7)	2.9 (0.6)	1.0 (0.6)	9/15
R-DE-10e5-	6.4(4)	8.4(2)	15(2)	13(2)	4.5(2)	15/15
RL-SHADE-1	7.1(0.5)	6.9(1.0)	8.8(2)	7.4(6)	12(16)	1/15
RL-SHADE-1	22(11)	30(11)	68(15)	133(61)	35(5)	15/15
R-SHADE-10	4.4(1)	4.8(2)	7.7(0.5)	4.3(0.4)	1.8 (2)	6/15
R-SHADE-10	5.0(2)	5.7(2)	10(3)	44(22)	13(3)	15/15
SOO-Derbel	4.8(0.0)	5.6(0.0)	51(8e-3)	13(2e-3)	3.6(2e-4)	15/15

Table 22: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{21} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f21	<i>6.3e+1:36</i>	<i>4.0e+1:77</i>	<i>4.0e+1:77</i>	<i>1.6e+1:456</i>	<i>4.0e+0:1094</i>	15/15
MATSUMOTO	2.7 _(0.5)	1.9 ₍₁₎ *	1.9 _(0.4) *	0.56 _(0.5)	0.97 ₍₂₎	9/15
R-DE-10e2-	3.7 ₍₂₎	3.1 ₍₁₎	3.1 _(0.9)	1.2 _(0.4)	2.2 ₍₃₎	8/15
R-DE-10e5-	14 ₍₇₎	12 ₍₅₎	12 ₍₆₎	7.3 ₍₃₎	41 ₍₅₇₎	15/15
RL-SHADE-1	9.1 ₍₂₎	6.6 ₍₂₎	6.6 ₍₃₎	4.5 ₍₅₎	6.1 ₍₂₎	4/15
RL-SHADE-1	56 ₍₁₆₎	52 ₍₁₄₎	52 ₍₁₄₎	15 ₍₃₎	169 ₍₆₄₂₎	14/15
R-SHADE-10	8.4 ₍₄₎	7.0 ₍₂₎	7.0 ₍₂₎	3.5 ₍₃₎	5.0 ₍₄₎	5/15
R-SHADE-10	13 ₍₆₎	11 ₍₃₎	11 ₍₃₎	3.0 _(0.9)	17 ₍₈₎	15/15
SOO-Derbel	3.8 ₍₁₎	4.6 ₍₅₎	4.6 ₍₅₎	2.4 ₍₂₎	8.7 ₍₄₀₎	15/15

Table 23: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{22} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f22	<i>6.3e+1:45</i>	<i>4.0e+1:68</i>	<i>4.0e+1:68</i>	<i>1.6e+1:231</i>	<i>6.3e+0:1219</i>	15/15
MATSUMOTO-	2.2 _(0.6)	2.1 _(0.6) ⁺²	2.1 ₍₂₎ ⁺²	1.5 ₍₂₎ [*]	0.58 _(0.7) [*]	11/15
R-DE-10e2-	4.4 ₍₂₎	4.7 ₍₂₎	4.7 ₍₂₎	6.9 ₍₉₎	5.2 ₍₃₎	4/15
R-DE-10e5-	12 ₍₈₎	13 ₍₅₎	13 ₍₉₎	81 ₍₆₆₎	25 ₍₄₇₎	15/15
RL-SHADE-1	7.7 ₍₂₎	7.2 ₍₄₎	7.2 ₍₂₎	7.2 ₍₁₃₎	2.5 ₍₂₎	8/15
RL-SHADE-1	49 ₍₁₇₎	59 ₍₁₂₎	59 ₍₉₎	493 ₍₁₇₄₂₎	221 ₍₂₎	14/15
R-SHADE-10	8.1 ₍₅₎	10 ₍₃₎	10 ₍₃₎	5.1 ₍₄₎	2.1 ₍₂₎	9/15
R-SHADE-10	12 ₍₇₎	12 ₍₃₎	12 ₍₁₀₎	28 ₍₁₆₁₎	14 ₍₂₉₎	15/15
SOO-Derbel	4.7 ₍₂₎	6.8 ₍₄₎	6.8 ₍₅₎	180 ₍₆₅₆₎	69 ₍₂₄₇₎	15/15

Table 24: 20-D, running time excess $ERT/ERT_{\text{best } 2009}$ on f_{23} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $ERT_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
f23	<i>6.3e+0:29</i>	<i>4.0e+0:118</i>	<i>2.5e+0:306</i>	<i>2.5e+0:306</i>	<i>1.0e+0:1614</i>	15/15
MATSUMOTO	2.0 (2)	10(15)	∞	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	2.1 (2)	6.2(6)	95(126)	95(110)	∞ <i>2000</i>	0/15
R-DE-10e5-	1.1 (2)	6.5(5)	81(17)	81(56)	∞ <i>2e6</i>	0/15
RL-SHADE-1	2.7 (3)	5.4(5)	48(61)	48(39)	∞ <i>2000</i>	0/15
RL-SHADE-1	1.0 (1)	4.0 (3)	57(11)	57(79)	116(25)	15/15
R-SHADE-10	2.4 (2)	6.7(6)	45 (81)	45 (46)	∞ <i>2000</i>	0/15
R-SHADE-10	1.7 (1)	4.8 (5)	68(100)	68(88)	95 (97)	15/15
SOO-Derbel	1.7 (4)	10(11)	12 (10)	12 (3)	3.9 (2)	15/15

Table 25: 20-D, running time excess $\text{ERT}/\text{ERT}_{\text{best } 2009}$ on f_{24} for given run-length based budgets (0.5D, 1.2D, 3D, 10D, and 50D function evaluations). The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding $\text{ERT}_{\text{best } 2009}$ (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries with succeeding star are statistically significantly better (according to the rank-sum test) compared to all other algorithms in the table, with $p = 0.05$ or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

#FEs/D	0.5	1.2	3	10	50	#succ
<i>f</i>24	<i>2.5e+2:208</i>	<i>1.6e+2:918</i>	<i>1.0e+2:6628</i>	<i>6.3e+1:9885</i>	<i>4.0e+1:31629</i>	15/15
MATSUMOTO	15(10)	∞	∞	∞	∞ <i>1000</i>	0/15
R-DE-10e2-	2.6 (3)	15(13)	∞	∞	∞ <i>2000</i>	0/15
R-DE-10e5-	4.8(1)	16(5)	592(369)	∞	∞ <i>2e6</i>	0/15
RL-SHADE-1	3.0(1)	5.7 (6)	∞	∞	∞ <i>2000</i>	0/15
RL-SHADE-1	16(5)	16(2)	15(2)	20(3)	9.4 (1.0)	15/15
R-SHADE-10	3.0(0.7)	32(39)	∞	∞	∞ <i>2000</i>	0/15
R-SHADE-10	2.7 (0.5)	2.7 (2)	3.2 (1)	5.4 (0.6)	6.1 (3)	15/15
SOO-Derbel	6.9(4)	7.3(5)	5.6 (3)	13 (17)	20(9)	15/15

References

- [1] Anne Auger, Steffen Finck, Nikolaus Hansen, and Raymond Ros. BBOB 2009: Comparison tables of all algorithms on all noiseless functions. Technical Report RT-0383, INRIA, April 2010.
- [2] Dimo Brockhoff. Comparison of the matsumoto library for expensive optimization on the noiseless black-box optimization benchmarking testbed. In *Proceedings of the IEEE Congress on Evolutionary Computation, CEC 2015, 25-28 May, Sendai, Japan, 2015*.
- [3] Bilel Derbel and Philippe Preux. Simultaneous optimistic optimization on the noiseless bbob testbed. In *Proceedings of the IEEE Congress on Evolutionary Computation, CEC 2015, 25-28 May, Sendai, Japan, 2015*.
- [4] S. Finck, N. Hansen, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Presentation of the noiseless functions. Technical Report 2009/20, Research Center PPE, 2009. Updated February 2010.
- [5] N. Hansen, A. Auger, S. Finck, and R. Ros. Real-parameter black-box optimization benchmarking 2012: Experimental setup. Technical report, INRIA, 2012.
- [6] N. Hansen, S. Finck, R. Ros, and A. Auger. Real-parameter black-box optimization benchmarking 2009: Noiseless functions definitions. Technical Report RR-6829, INRIA, 2009. Updated February 2010.
- [7] Ryoji Tanabe and Alex Fukunaga. Parameter tuning for differential evolution for cheap, medium, and expensive computational budgets. In *Proceedings of the IEEE Congress on Evolutionary Computation, CEC 2015, 25-28 May, Sendai, Japan, 2015*.